Expected insights into Type Ia supernovae from LISA's gravitational wave observations

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ABSTRACT

The nature of progenitors of Type Ia supernovae has long been debated, primarily due to the elusiveness of the progenitor systems to traditional electromagnetic observation methods. We argue that gravitational wave observations with the upcoming Laser Interferometer Space Antenna (LISA) offer the most promising way to test one of the leading progenitor scenarios - the double-degenerate scenario, which involves a binary system of two white dwarf stars. In this study we review published results, supplementing them with additional calculations for the context of Type Ia supernovae. We discuss the fact that LISA will be able to provide a complete sample of double white dwarf Type Ia supernova progenitors with orbital periods shorter than 16-11 minutes (gravitational wave frequencies above 2-3 millihertz). Such a sample will enable a statistical validation of the double-degenerate scenario by simply counting whether LISA detects enough double white dwarf binaries to account for the measured Type Ia merger rate in Milky Way-like galaxies. Additionally, we illustrate how LISA's capability to measure the chirp mass will set lower bounds on the primary mass, revealing whether detected double white dwarf binaries will eventually end up as a Type Ia supernova. We estimate that the expected LISA constraints on the Type Ia merger rate for the Milky Way will be 4-9%. We also discuss the potential gravitational wave signal from a Type Ia supernova assuming a double-detonation mechanism and explore how multi-messenger observations could significantly advance our understanding of these transient phenomena.

Key words. gravitational waves - binaries: close - supernovae: general - white dwarfs

1. Introduction

Type Ia supernovae (SNe Ia) are amongst the most energetic explosions in the Universe, producing a luminosity of about $10^{43} \text{ erg s}^{-1}$ near maximum light. They emerged as a distinct class based on spectral signatures: the absence of hydrogen and helium and the presence of broad features of silicon, calcium, and iron (e.g. see the review by Filippenko 1997). Notably, the light curve shapes of many SNe Ia closely resemble each other: peaking within 15-20 days and then declining rapidly. As a consequence, these standardisable (also referred to as 'normal') SNe Ia have been adopted as cosmological standard candles and provided the first evidence for the acceleration of cosmic expansion (Riess et al. 1998; Perlmutter et al. 1999). The luminosity that characterises the light curve of a (normal) SN Ia originates from the radioactive decay of ⁵⁶Ni to ⁵⁶Co and then to stable ⁵⁶Fe. The energetics and chemical composition imply that these SNe result from the thermonuclear combustion of a white dwarf (Hoyle & Fowler 1960). Despite SNe Ia being among the most studied transient phenomena, there is still no consensus on other fundamental aspects, such as the nature of the progenitor and explosion mechanisms, both from theoretical and observational perspectives (see recent reviews by Maoz et al. 2014; Ruiter 2020, and Liu et al. 2023).

There is a broad consensus that the white dwarf explosion in a SN Ia is triggered by the interaction with a companion star. Identifying the nature of the companion (and the nature of the explosion), however, has been a long-standing challenge (e.g. Livio & Mazzali 2018). Historically, the field has developed around two main progenitor scenarios: single-degenerate and double-degenerate¹. In the single-degenerate scenario, a white dwarf accretes matter from a non-degenerate companion (e.g. a main sequence star, sub-giant, or helium star) until it approaches the Chandrasekhar mass limit and explodes (Whelan & Iben 1973; Nomoto et al. 1984). In contrast, in the double-degenerate scenario, the companion is another white dwarf, and the two white dwarfs are brought together to interact or merge directly via gravitational wave (GW) radiation (Whelan & Iben 1973; Iben & Tutukov 1984). We refer the reader to the recent review by Soker (2024) for a more articulated picture of SN Ia progenitor scenarios. Each scenario offers a plausible explanation, and

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Here 'degenerate' refers to white dwarfs, which are supported by the pressure of degenerate electrons, in contrast to normal (non-degenerate) stars, which are supported by thermal pressure.

in the absence of definitive evidence, it is difficult to conclusively favour one over the other (e.g. Maoz et al. 2014).

There are significant challenges associated with detecting double-degenerate SN Ia progenitors through electromagnetic (EM) observations, primarily due to the intrinsic faintness of these binaries. So far very few binaries have been identified as potential double-degenerate SN Ia progenitors (see e.g. Munday et al. 2024, for a recent overview). Rebassa-Mansergas et al. (2019) highlighted that even with next-generation large-aperture telescopes, such as the Extremely Large Telescope (ELT), the estimated probability of identifying and validating SN Ia progenitors (by measuring the binary components' masses) will remain remarkably low. Here we discuss why GW observations with the Laser Interferometer Space Antenna (LISA) offer a promising alternative for determining the nature of SN Ia progenitor systems, overcoming the limitations faced by traditional EM observation methods.

In this study we explore the SN Ia progenitor question from the perspective of future GW observations. Specifically, we discuss the potential of LISA, an upcoming millihertz GW observatory that has recently been scheduled for launch by the European Space Agency in the mid-2030s (Colpi et al. 2024). Our arguments also hold for other space-based GW observatories such, as TianQin (Luo et al. 2016; Huang et al. 2020), Taiji (Ruan et al. 2018), and the Lunar Gravitational Wave Antenna (Harms et al. 2021; Branchesi et al. 2023; Ajith et al. 2024). LISA's sensitivity to the shortest-period (less than about 2 hours) double white dwarf (WD+WD) binaries in the Milky Way and its nearest satellite galaxies presents a unique opportunity to test the double-degenerate scenario directly (LISA Consortium Astrophysics Working Group 2023).

The structure of this paper is as follows. In Sect. 2 we review the constraints on double-degenerate WD+WD progenitors in the Milky Way that we will likely be able to place based on LISA observations (Colpi et al. 2024), including the incidence of these binaries (Sect. 2.1), chirp mass constraints (Sect. 2.2), and their overall merger rate (Sect. 2.3). In Sect. 3 we discuss the fortunate possibility of directly observing the final inspiral and a SN Ia explosion during LISA's operation time. We adopt a 3D hydrodynamical simulation, in which the primary white dwarf undergoes the double detonation mechanism, to illustrate the evolution of GW strain in frequency over the last few orbits prior to a SN Ia event (Sect. 3.1). We also discuss the implications of multi-messenger observations (Sect. 3.2), including expectations for neutrino signals (Sect. 3.3). Finally, we present a summary and the conclusions of our study in Sect. 4.

2. Constraints on the double-degenerate progenitor systems in the Milky Way

The dense and compact nature of white dwarf stars, while challenging for EM observations, offers advantages for the GW detection. In fact, in the following we argue that the best way of surveying double-degenerate SN Ia progenitors is via GW observations with a mission like LISA.

GW radiation from a circular WD+WD binaries can be modelled with a nearly monochromatic sinusoidal waveform (e.g. LISA Consortium Waveform Working Group 2023). Such a waveform can be described by eight key parameters: the GW amplitude \mathcal{A} , GW frequency f_{GW} , its derivative \dot{f}_{GW} , the binary's sky coordinates (λ, β) , inclination angle ι , polarisation angle ψ , and the initial phase ϕ_0 . For circular binaries, the GW frequency is exactly $f_{GW} = 2/P_{orb}$, with P_{orb} being the binary's orbital period. The strain amplitude of the signal is given by

$$\mathcal{A} = \frac{2(G\mathcal{M})^{5/3}}{c^4 d} (\pi f_{\rm GW})^{2/3},\tag{1}$$

and is determined by the binary's GW frequency, distance *d* and chirp mass $\mathcal{M} = (m_1m_2)^{3/5}/(m_1 + m_2)^{1/5}$, for component masses $m_1 \ge m_2$; *G* and *c* are respectively the gravitational constant and speed of light. Equation (1) reveals that binaries characterised by higher frequencies and larger masses produce GWs with larger amplitude, yielding signals with higher signal-to-noise ratios:

$$\rho \propto \mathcal{A} \sqrt{\frac{T_{\rm obs}}{S_n(f_{\rm GW})}},\tag{2}$$

where T_{obs} is the observation time and $S_n(f_{GW})$ is the noise power spectral density, a quantity describing the noise of the LISA detector as a function of frequency (e.g. Moore et al. 2015), at the binary's frequency (for the full derivation, see Appendix A of Finch et al. 2023). We note that, unlike EM observations – which are based on the measurement of energy flux and scale with $1/d^2$ – GW observations offer direct measurements of the signal's amplitude and thus scale with 1/d. Consequently, GW observations enable the detection of EM-dim sources (or even entirely invisible dormant binary black holes) at distances that are not directly accessible with EM observations (e.g. Korol et al. 2017; Sesana et al. 2020).

2.1. Probing the number of progenitor systems

To study the expected completeness of LISA's WD+WD sample, we utilised published mock catalogues assembled based on both theory-driven (Korol et al. 2017; Wilhelm et al. 2021) and observations-driven (Korol et al. 2022) population synthesis. Our theory-driven models are based on the SEBA stellar and binary evolution module (Portegies Zwart & Verbunt 1996; Nelemans et al. 2001; Toonen et al. 2012) with variations in the underlying assumptions for the binary interactions (for details see Toonen et al. 2012). While our observations-driven models are based on a statistical method developed to characterise the binarity of large spectroscopic samples of white dwarfs with sparsely sampled radial velocity data (Badenes & Maoz 2012; Maoz et al. 2012, 2018). Variations in our observations-driven models are due to different underlying assumptions for the binary fraction, WD+WD separation (at formation), and mass distributions (for details see Korol et al. 2022).

We assessed the completeness as the percentage of detectable binaries relative to the total underlying WD+WD population as a function of frequency. Importantly, the populations selected for this study are directly comparable, as they were analysed under the same mission specifications, including the noise model, a 4-year mission duration, and a detection threshold of ρ_{4yr} = 7. This analysis employed the same pipeline as Karnesis et al. (2021), which self-consistently estimates the unresolved stochastic foreground from the input population and resolves binaries with a signal-to-noise ratio above the threshold. The result is presented in the left panel of Fig. 1, where solid grey lines represent the family of observations-driven models and orange dashed lines represent the family of theory-driven models. In the right panel, we show the example of the spatial distribution within the Milky Way of WD+WD binaries with $\rho_{1\rm vr} \geq 7$ from Wilhelm et al. (2021), colour-coded by GW frequency. It is evident that binaries emitting at $f_{\rm GW} \geq$ 2-3 mHz (in pale orange to yellow) can be detected throughout the entire Galaxy. Although not strictly comparable due to

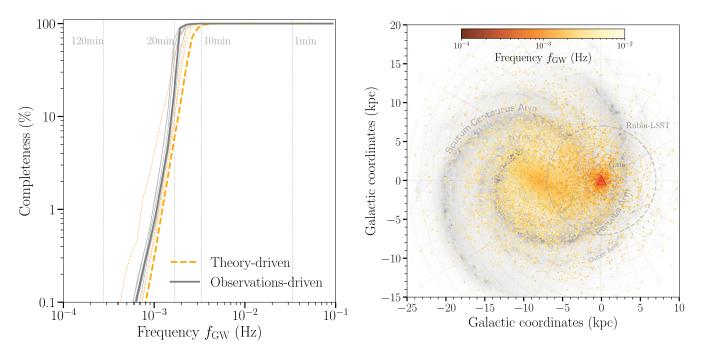


Fig. 1. LISA's capability to probe the Galactic WD+WD binary population. Left panel: Completeness of LISA's Galactic WD+WD sample as a function of frequency estimated based on sets of mock Galactic catalogues: theory-driven (dashed orange lines; Korol et al. 2017; Wilhelm et al. 2021) and observation-driven (solid grey lines; Korol et al. 2022). Thick lines represent the respective default models, and thin lines model variations within each set (e.g. different prescriptions for binary interactions in the theory-driven models). Vertical dotted lines mark the respective binary orbital periods. Right panel: Spatial distribution of binaries with $\rho_{1yr} \ge 7$ within the Galaxy adapted from Wilhelm et al. (2021), colour-coded by GW frequency. In the background we show an artist's impression of our current view of the Milky Way. The red triangle at (0,0) shows LISA's position, while the Galactic Centre is at (-8.2, 0). For comparison, we show estimated observational horizons for WD+WD binaries for *Gaia* and *Rubin*-LSST surveys (Korol et al. 2017).

differences in the WD+WD detection analysis, we expect that other recently published models will show similar results (e.g. Lamberts et al. 2019; Breivik et al. 2020; Li et al. 2020, 2023; Thiele et al. 2023; Tang et al. 2024)

Figure 1 illustrates that LISA is expected to achieve a complete sample of WD+WD binaries with GW frequencies above 2–3 mHz, corresponding to orbital periods shorter than 16 to 11 minutes. Thus, based on the LISA sample, we would be able to quantitatively assess the contribution of double-degenerate progenitors to the measured SN Ia merger rate from EM observations (see also Colpi et al. 2024). This could be achieved by simply counting whether LISA detects enough WD+WD binaries, importantly without concerns regarding selection effects.

2.2. Probing the masses of progenitor system

To identify potential SN Ia progenitors within LISA's sample, constraints on the binary components' masses are essential, particularly considering that only a subset of the most massive WD+WD binaries (with primary mass $m_1 > 0.8 \,\mathrm{M_{\odot}}$) are more likely to lead to SN Ia events. This is an essential requirement because lower-mass white dwarfs may not produce significant amounts of ⁵⁶Ni, even if they undergo a thermonuclear explosion (e.g. Sim et al. 2010). We also assumed that binaries $0.5 < m_1 < 0.8 \,\mathrm{M_{\odot}}$ result in thermonuclear explosions of lower luminosity than a normal SN Ia, while those with $m_1 < 0.5 \,\mathrm{M_{\odot}}$ fail to detonate (e.g. Morán-Fraile et al. 2024; Shen et al. 2024).

At GW frequencies greater than 2–3 mHz, LISA is expected to measure not only the GW frequency and amplitude of WD+WD signals but also the frequency derivative – the socalled chirp – resulting from GW radiation (e.g. Colpi et al. 2024). Through the measurement of f_{GW} and its derivative f_{GW} , it becomes possible to deduce the binary system's chirp mass. Under the assumptions that the binary is detached, non-interacting, and on a circular orbit, which are expected to hold for most of the LISA-detectable WD+WD population, the GW frequency derivative can be expressed as

$$\dot{f}_{\rm GW} = \frac{96}{5} \frac{(G\mathcal{M})^{5/3}}{\pi c^5} (\pi f_{\rm GW})^{11/3}.$$
 (3)

We note that the above expression ignores tidal effects, which could become important at higher frequencies for example, binaries considered below (e.g. Shah & Nelemans 2014; Wolz et al. 2021; Toubiana et al. 2024). We also note that ignoring these effects, especially at $f_{\rm GW} > 10$ mHz, can lead to non-negligible biases in the mass estimate (Fiacco et al. 2024).

To showcase LISA's potential for measuring the chirp mass of double-degenerate SN Ia progenitor systems, we considered three examples: $0.6\,M_\odot + 0.4\,M_\odot,\ 1.05\,M_\odot + 0.3\,M_\odot,$ and $1.05 \, M_{\odot} + 0.7 \, M_{\odot}$. These combinations yield chirp masses of $0.42\,M_{\odot},\,0.47\,M_{\odot},$ and $0.74\,M_{\odot},$ respectively. The binary with the lowest chirp mass is representative of a potential progenitor for thermonuclear transients of lower luminosity than a normal SN Ia, whereas the latter two configurations are representative of a normal SN Ia progenitor (e.g. Shen 2015). We generated GW signals and performed parameter estimations for these three example binaries within a Bayesian inference framework using BALROG (Buscicchio et al. 2019, 2021; Roebber et al. 2020; Klein et al. 2022; Finch et al. 2023). We simulated signals with initial frequencies of 2, 6, and 10 mHz, while bracketing dependence on the binaries' orientation with face-on and edge-on configurations. All sources are (arbitrarily) located in the Galactic centre, assuming a distance of 8.2 kpc (e.g. GRAVITY Collaboration 2021).

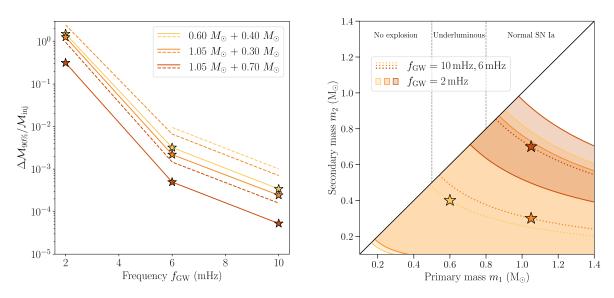


Fig. 2. LISA's capability to measure chirp masses and constrain binary component masses. Left panel: Fractional uncertainty on the chirp mass. Solid (dashed) lines represent face-on (edge-on) binary configurations, and stars denote representative simulated systems. Right panel: Constraints on component masses. The shaded areas between solid lines denote sources at 2 mHz. Dotted lines represent sources at 6 and 10 mHz. These constraints assume that the symmetric mass ratio (i.e. $m_1m_2/(m_1 + m_2)^2$) is unknown, and they are sampled from a uniform prior. Vertical dashed grey lines delimit three representative classes: configurations that produce no explosion ($m_1 < 0.5 M_{\odot}$), those likely resulting in a low-luminosity thermonuclear transient ($0.5 < m_1 < 0.8 M_{\odot}$), and those that will likely result in a normal SN Ia ($m_1 > 0.8 M_{\odot}$).

In Fig. 2 we showcase LISA's expected capability to measure the binary's chirp mass across different frequencies (left panel) and the corresponding constraints on the component masses (right panel). Our results reveal that at 2 mHz, the chirp mass measurement is constraining only for the most massive case among the considered examples. As the frequency increases beyond 4-5 mHz, the precision of the chirp mass measurements significantly improves for all three examples, dropping rapidly to 0.01–0.001% at 10 mHz. From the right panel, we observe that at 2 mHz (as indicated by coloured bands), the chirp mass measurement implies a minimum primary mass of $0.2 \, M_{\odot}$ for the binaries with chirp masses of $0.42\,M_{\odot}$ and the $0.47\,M_{\odot}$, and a minimum mass of 0.7 M_{\odot} for the one with a 0.74 M_{\odot} chirp mass. Consequently, for the latter example, we can predict an eventual SN Ia with a posterior probability of 96%, estimated by assuming a uniform prior in mass ratio and by counting posterior samples within the $m_1 > 0.8 \,\mathrm{M}_{\odot}$ region. As the frequency increases to 6 mHz and higher, the uncertainty in chirp mass measurement reduces to less than 1%; as a consequence, constraints on components' mass converge to a line. This precision translates to a lower bound for the primary mass of $0.49\,M_{\odot}$ for the $0.42\,M_{\odot}$ chirp mass binary, and $0.55\,M_\odot$ for the $0.47\,M_\odot$ chirp mass binary. For these two cases, the probability of eventually resulting in a thermonuclear transient is 100%, estimated by assuming a uniform prior in mass ratio and by counting posterior samples within the $m_1 > 0.5 \,\mathrm{M}_{\odot}$ region. For the most massive of the considered examples, the lower limit on the primary mass can be set to 0.87 M_{\odot} . This implies that LISA will be able to assign a 100% probability that this binary is a progenitor of a normal SN Ia (i.e. $m_1 > 0.8 \,\mathrm{M}_{\odot}$).

2.3. Probing the merger rate of progenitor systems

The measurement of the chirp mass offers a method for estimating the time until merger due to GW radiation. The time to merger, $\tau = t_{merger} - t$, can be estimated, in a first post-Newtonian approximation, by integrating Eq. (3) (e.g. Peters 1964):

$$\tau(f_{\rm GW}, \mathcal{M}) = \frac{5c^5}{256(G\mathcal{M})^{5/3}(\pi f_{\rm GW})^{8/3}},\tag{4}$$

which is valid under the same assumptions as used in Eq. (3). Given that the GW frequency of WD+WD binaries is measured with high precision ($\Delta f_{\rm GW}/f_{\rm GW} \ll 10^{-5}$; e.g. Karnesis et al. 2021; Finch et al. 2023; Colpi et al. 2024), the uncertainty in τ primarily depends on LISA's ability to constrain the chirp mass, with $\Delta \tau/\tau \approx 5/3 \Delta M/M$. We provide the estimate of this measurement for the three considered examples in Table 1.

Assuming that binaries in the LISA sample inspiral according to Eq. (4), their distribution in frequency will enable an estimate of the overall merger rate. To provide an order-of-magnitude estimate of LISA's ability to constrain the SN Ia merger rate, \mathcal{R}_{SNIa} , we considered a simplified scenario where all SN Ia progenitors consist of binaries with masses of $1.05 \text{ M}_{\odot} + 0.7 \text{ M}_{\odot}$ (corresponding chirp mass of 0.74 M_{\odot}). As illustrated in Sect. 2.2, binaries with similar chirp mass or higher can be identified as SN Ia progenitors with high confidence, starting at 2 mHz. Assuming that the WD+WD population is in a steady state, the spectral density of binaries resolved over the mission duration is given by

$$\frac{\mathrm{d}N_{\rm SNIa}}{\mathrm{d}f_{\rm GW}} = \frac{5c^5 \mathcal{R}_{\rm SNIa}}{96\pi^{8/3} (G\mathcal{M})^{5/3} f_{\rm GW}^{11/3}}.$$
(5)

The rate can be recovered by integrating Eq. (5) over frequency and solving for \mathcal{R}_{SNIa} :

$$\mathcal{R}_{\rm SNIa} = \frac{256(G\mathcal{M})^{5/3} (\pi f_{\rm GW})^{8/3}}{5c^5} N_{\rm SNIa} (> f_{\rm GW}), \tag{6}$$

where $N_{\text{SNIa}}(> f_{\text{GW}})$ is the total number of binaries emitting above a certain frequency threshold f_{GW} . From Eq. (6), it follows that the error on $\mathcal{R}_{\text{SNIa}}$ depends on the errors in the number count

Injection parameters							Posterior				Classification		
\mathcal{M}^{inj} [M_{\odot}]	$m_1^{ m inj}$ [$ m M_{\odot}$]	$m_2^{ m inj}$ [M $_{\odot}$]	f ^{inj} [Hz]	τ ^{inj} [Myr]	cos t ^{inj}	S/N	$\Delta \mathcal{M}^{90\%}$ $[M_{\odot}]$	$\Delta au^{90\%}$ [Myr]	$\Delta \mathcal{M}^{90\%}/\mathcal{M}^{ m inj}$	$\Delta \tau^{90\%}/\tau^{\rm inj}$	No expl. [%]	Underl. [%]	Normal [%]
0.42	0.60	0.40	0.002	1.345	0	5.1	5.57312	0.351	13.1211	0.2607	16.0	25.9	58.0
					1	15.0	0.64505	7.764	1.5187	5.7705	21.7	31.7	46.6
			0.006	0.072	0	57.4	0.00404	0.0011	0.0095	0.0159	3.4	56.0	40.6
					1	169.8	0.00137	0.0004	0.0032	0.0054	3.0	54.8	42.2
			0.010	0.018	0	82.0	0.00043	0.000031	0.0010	0.0017	3.1	55.3	41.6
					1	243.1	0.00015	0.00001	0.0003	0.0006	3.8	56.6	39.6
0.47	1.05	0.30	0.002	1.133	0	6.0	1.16005	5.589	2.4635	4.9332	18.1	25.6	56.3
					1	17.8	0.59892	6.316	1.2719	5.5747	19.3	33.2	47.4
			0.006	0.061	0	68.2	0.00313	0.0007	0.0067	0.0111	0.0	51.0	49.0
					1	201.7	0.00103	0.0002	0.0022	0.0037	0.0	51.2	48.8
			0.010	0.015	0	97.4	0.00033	0.000018	0.0007	0.0012	0.0	49.8	50.2
					1	288.7	0.00011	0.000006	0.0002	0.0004	0.0	51.5	48.5
0.74	1.05	0.70	0.002	0.529	0	12.9	0.71376	1.613	0.9603	3.0476	6.2	19.0	74.8
					1	38.1	0.23422	0.296	0.3151	0.5597	0.0	4.5	95.5
			0.006	0.028	0	146.0	0.00109	0.00007	0.0015	0.0024	0.0	0.0	100.0
					1	431.6	0.00037	0.00002	0.0005	0.0008	0.0	0.0	100.0
			0.010	0.007	0	208.5	0.00012	0.000002	0.0002	0.0003	0.0	0.0	100.0
					1	617.8	0.00004	0.000001	0.0001	0.0001	0.0	0.0	100.0

Table 1. Point estimates from simulations with BALROG.

Notes. The superscript 'inj' stands for injected, i.e. assumed as the true value; the abbreviation 'S/N' stands for the signal-to-noise ratio. The three leftmost columns represent classification probabilities for each source, according to the three classes defined in Sect. 2.2: 'No explosion' $(m_1 < 0.5 \text{ M}_{\odot})$, 'Underluminous' $(0.5 \text{ M}_{\odot} < m_1 < 0.8 \text{ M}_{\odot})$ and 'Normal SN Ia' $(m_1 > 0.8 \text{ M}_{\odot})$.

of SN Ia progenitor binaries and the error on the chirp mass. As discussed in Sect. 2.1, at frequencies higher than 2 mHz, LISA can detect every relevant binary, allowing the estimate of the merger rate of $1.05\,M_{\odot}$ + $0.7\,M_{\odot}$ without concerns about selection effects.

To estimate the error on \mathcal{R}_{SNIa} , we first sampled $N_{SNIa}(> f_{GW})$ from a Poisson distribution with the mean set by assuming SN Ia merger rates of $(2, 4, 7) \times 10^{-3} \text{ yr}^{-1}$ (e.g. Cappellaro & Turatto 2001; Li et al. 2011; Maoz et al. 2018), derived based on EM observations. Our assumption on the underlying 'true' merger rate sets the number of detected binaries, which we then distributed in frequency according to Eq. (5). As a reference, setting the SN Ia merger rate to 2×10^{-3} yr⁻¹ (7 × 10⁻³ yr⁻¹) yields 1069, 57, 15 (3743, 200, 51) binaries with a chirp mass of $0.74 M_{\odot}$ at frequencies above 2, 6, and 10 mHz, respectively. To mimic the effects of measurement uncertainties, each chirp mass measurement is subsequently drawn from a Gaussian distribution, the width of which is interpolated from our results for the posterior widths for the $1.05 \,M_{\odot} + 0.7 \,M_{\odot}$ binary in Fig. 2. We performed Monte Carlo simulations over an arbitrarily large number of realisations. The result is illustrated in Fig. 3 (solid lines); for comparison, we also plot the number count error only (dashed lines). This experiment demonstrates that LISA's error on the merger rate including binaries at $f_{\rm GW}$ < 4 mHz will be dominated by the large number of binaries with relatively poor constraints on the chirp mass (~10%; cf. Fig. 2). These binaries are about an order of magnitude more numerous than those at $f_{GW} > 4$ mHz, where the chirp mass constraint improves to ${\sim}1\%$ level and better. On the other hand, in the sample including binaries with $f_{\rm GW} > 4 \,\rm mHz$, the error is primarily driven by the Poissonian error given the lower number of sources (<50–10 at $f_{\rm GW}$ > 10 mHz for the considered SN Ia rates). The measurement is optimal for the subsample of binaries with frequencies of less than 4 mHz, where, based on the LISA observations alone, we achieve SN Ia merger rate error below 10%. It might also be possible to obtain an improved measurement of the rate \mathcal{R}_{SNIa} (i.e. with a smaller uncertainty) by also using the larger, but incomplete, sample of binaries with lower fre-

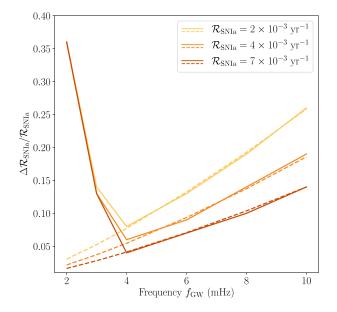


Fig. 3. LISA's capability to measure SN Ia merger rates (\mathcal{R}_{SNIa}) from double-degenerate SN Ia progenitors at frequencies between 2 and 10 mHz for different SN Ia rates. Solid lines represent the results of the Monte Carlo simulation where we combined uncertainties in the number count of SN Ia progenitors (assumed to be Poisson-distributed) with LISA's ability to measure the chirp mass. Dashed lines show the number count error only.

quencies, although this would require a more detailed populationlevel, hierarchical analysis that accounts for selection effects.

If the merger rate of WD+WD LISA sources inferred in this way turns out to be consistent with the known rate of SNe Ia, this would be persuasive evidence in favour of the double-degenerate scenario. If, on the other hand, the rates do not match, then this suggests that at least some fraction of SNe Ia come from another channel.

3. The chance of a direct observation of a final inspiral and SN Ia

As discussed in Sect. 2, the double-degenerate SN Ia progenitor scenario can already be confirmed or rejected based on the number/merger rate of close, massive WD+WD binaries that LISA will detect across our Galaxy. Given the observed SN Ia rate in the Milky Way-like galaxies, $\mathcal{R}_{SNIa} = (3-7) \times 10^{-3} \text{ yr}^{-1}$ (e.g. Cappellaro & Turatto 2001; Li et al. 2011; Maoz et al. 2018), we expect a 3-7% chance of a SN Ia event during LISA's maximum lifetime of 10 yr. Additionally, the most massive SN Ia WD+WD progenitors LISA can also be observed in the Magellanic Clouds (Korol et al. 2020; Roebber et al. 2020; Keim et al. 2023) and possibly as far as the Andromeda galaxy (Korol et al. 2018). Here we outline the implications if such an opportunity arises. In Sect. 3.1 we illustrate the expected GW signal, assuming a double-degenerate scenario in which the primary white dwarf undergoes double detonation (Livne 1990; Fink et al. 2010). In Sect. 3.2 we briefly discuss the potential insights that could be gained from multi-messenger observations.

3.1. Gravitational wave signal

To illustrate the GW signal from a WD+WD binary resulting in a SN Ia, we adopted a 3D hydrodynamical simulation of Pakmor et al. (2022). The simulation represents the last few orbits of a $1.05 M_{\odot}$ and $0.7 M_{\odot}$ carbon-oxygen WD+WD binary system, in which the primary undergoes the double-detonation mechanism via a dynamical ignition on the surface of the primary (Guillochon et al. 2010; Pakmor et al. 2013, 2022; Rajavel et al. 2024).

We computed the GW signal following the same methods as in Morán-Fraile et al. (2023, see also Seitenzahl et al. 2015). The amplitude of the GW signal is derived from the approximate quadrupole radiation from Newtonian gravity, following the numerical approach described in Blanchet et al. (1990). We summarise the main points of this computation in Appendix A. In Fig. 4 we show the obtained evolution of GW frequency and strain amplitude as a function of time, assuming a distance of 8.2 kpc as in Sect. 2.2. In the figure, we consider the most optimistic scenario for detectability, corresponding to a face-on binary orientation. This means the plane of the binary's orbit is perpendicular to the line of sight, maximising the '+' GW polarisation component (see Appendix A), which is shown in the middle panel of the figure. We estimate the time evolution of the GW frequency using $f_{\text{GW}} = 2/P_{\text{orb}}$, with P_{orb} taken directly from the output of the hydrodynamical simulation.

The first part of the signal (between -100 s and 0 s) represents the end of the inspiral phase starting with the onset of mass-transfer from the secondary (0.7 M_{\odot}) onto the primary (1.05 M_{\odot}) white dwarf via Roche-lobe overflow. During these 100 s, the primary gains about $10^{-2} \text{ M}_{\odot}$ of ⁴He. The evolution of the binary in this phase can still be described as in Sect. 2; indeed, the GW signal shows no significant deviation from a regular sinusoidal waveform. During this time, the orbital separation changes only slightly before the binary is disrupted, resulting in a small increase in GW frequency from 92 Hz to 96 Hz (bottom panel).

At t = 0, the helium detonation ignites close to the point where the accretion stream hits the surface of the primary. The helium detonation then wraps around the primary burning its helium shell and sending a shockwave into its core. This shockwave converges in a single point in the core of the primary white dwarf and ignites a carbon detonation there at t = 1.3 s. The carbon detonation completely burns and destroys the primary white dwarf (t = 4.9 s), generating a SN Ia. After the detonation of the primary, the strain amplitude in Fig. 4 shows a small excess signal (see the inset), which then levels off at a constant value until the end of the simulation t = 100 s. This part of GW signal is generated by the homogeneous expansion of the supernova ejecta.

At the same time, the shockwave of the explosion of the primary hits the secondary white dwarf. It ignites the helium shell of the secondary at around t = 2 s and additionally sends a shockwave into its core directly. This shockwave, supported by the helium detonation burning the remaining helium around the secondary white dwarf converges in its core at t = 4.9 s. The converging shockwave in the secondary white dwarf fails to ignite a carbon detonation in its core and the secondary white dwarf survives until the end of the simulation 100s later (the 'one-explosion' model in Fig. 4). It is interesting to note that a detonation initiation in the secondary is physically plausible, given its density and temperature at t = 4.9 s. We show the GW signal for this possible scenario generated by artificially igniting a carbon detonation in the secondary at the convergence point of the shockwave (the 'two-explosion' model in Fig. 4). In this case, the second carbon detonation burns the secondary completely within about 1 s and destroys it as well. In the 'twoexplosion' model, we observe an additional small excess signal between 5 s and 6 s in Fig. 4, with the strain amplitude levelling off at a slightly higher constant value than in the 'oneexplosion' model due to the expansion of the secondary's ejecta. At the time of writing, the likelihood of the secondary's detonation remains uncertain, and it is unclear whether the two models (one- and two-explosion) can be differentiated through EM observations (e.g. Pakmor et al. 2022; Pollin et al. 2024). Given the small additional strain amplitude produced as a result of the secondary's explosion, it is unlikely that this extra signal can be confidently extracted from the actual GW data. A more detailed technical investigation would be required to fully explore this possibility.

In summary, Fig. 4 illustrates that the binary emits nearly monochromatic GWs until just before the primary is disrupted by carbon detonation in the core, at which point the system virtually ceases to emit GWs. If the double-detonation mechanism is responsible for a significant portion of normal SNe Ia (resulting from a detonation of $0.8-1.1 M_{\odot}$ primary), the ignition and explosion must occur prior to the merger, leading to a 'clean' disappearance of the binary's GW signal as in our example. If, on the other hand, the explosion occurs after the merger, such as in the case of the lower luminosity thermonuclear transient than a normal SN Ia (e.g. resulting from the merger of a $0.6 \, M_{\odot}$ carbon-oxygen white dwarf with a $0.4\,M_{\odot}$ helium white dwarf; see Morán-Fraile et al. 2024) the GW signal will comprise both the merger and post-merger phases until the double detonation occurs (see also Dan et al. 2011; Seto 2023). In this case, the delay between the merger and the explosion is of the order of several minutes. A more detailed description of this scenario will be provided in a dedicated study.

3.2. Chance of a multi-messenger observation

If a SN Ia occurs in the Milky Way while LISA is operational, we might observe a GW signal followed by the detection of EM signal (e.g. see synthetic light curves and spectra in Pakmor et al. 2022), followed by a shut off of the GW signal. Such an event would directly confirm the double-degenerate scenario, particularly demonstrating that SNe Ia are rapid dynamical

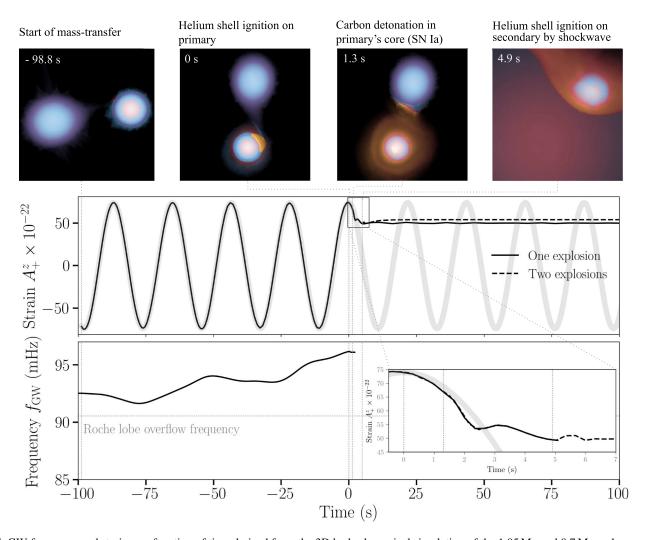


Fig. 4. GW frequency and strain as a function of time derived from the 3D hydrodynamical simulation of the 1.05 M_{\odot} and 0.7 M_{\odot} carbon-oxygen white dwarf binary in Pakmor et al. (2022), in which the primary undergoes double detonation. Top panels: Key steps of the double-detonation mechanism. t = -98.8 s is the onset of the mass transfer from the secondary (the visibly larger, fluffier white dwarf) onto the primary (the more compact of the two). t = 0 s is the helium-shell ignition on the primary. At t = 1.3 s the helium detonation wraps around the primary, triggering the detonation of the primary's carbon-oxygen core. At t = 4.9 s, the carbon detonation completely burns the primary (resulting in a SN Ia) and triggers helium-shell ignition on the secondary. Middle panel: Evolution of GW strain. The A_{\pm}^2 GW polarisation amplitude is computed based on the output of the hydrodynamical simulation following the Morán-Fraile et al. (2023) method and assuming a distance of 8.2 kpc. The solid black line shows the 'one-explosion' model, in which only the primary undergoes double detonation; the dashed line represents the 'two-explosion' model, in which the explosion of the simulation, which represents the homogeneous expansion of the supernova ejecta. For comparison, the thick grey-shaded line represents a monochromatic signal of 92 Hz frequency and of equivalent amplitude. The inset shows a zoomed-in view between -0.5 s and 7 s. Bottom panel: Evolution of the GW frequency (solid line) that we computed directly from the binary separation obtained from the hydrodynamical simulation.

explosions, unfolding over just a few seconds, as suggested by recent double-detonation models (cf. Sect. 3.1) or violent mergers (e.g. Pakmor et al. 2010, 2012). Any measurable delay between the GW and EM signals could indicate alternative detonation mechanisms and would represent an equally significant discovery.

A constraint on the progenitor binary component masses from the inspiral phase of the GW signal from LISA (see Sect. 2.2) and the observation of SNe Ia would lead to significant progress in modelling explosion physics of SNe Ia, even from a single observed event. Combining it with the EM signal would link the initial pre-explosion state of the system, and the outcome of the explosion in the form of SN Ia ejecta and an EM display. This would likely allow us to constrain and improve on the inherent uncertainties in the modelling of explosion physics for SNe Ia.

Observing a GW signal without a corresponding EM signal would also provide valuable insights, leading to several possible interpretations. First, with LISA's capability to localise WD+WD binaries within an area $\ll 1 \text{ deg}^2$ (e.g. Finch et al. 2023), it could allow us to confirm or exclude that no EM emission is detectable due to strong extinction. If extinction is ruled out, the absence of EM emission might suggest a traditional double-degenerate super-Chandrasekhar scenario (i.e. a WD+WD merger with a total mass exceeding Chandrasekhar mass limit) with a long delay that may extend up to 10^4 yr (e.g. Nomoto 1985; Shen et al. 2012).

Finally, if an EM event is observed without a corresponding GW signal in the LISA band, this could indicate a merger with a delay-time between merger and explosion longer than the observing time of LISA (as discussed above) or a singledegenerate scenario, in which case the GW signal in the LISA band is not expected. Studies by Falta et al. (2011) and Seitenzahl et al. (2015) computed GW signals for SNe Ia produced via different single-degenerate models. While the progenitor systems (carbon-oxygen white dwarf + main sequence or a red giant) would emit at frequencies below 10^{-4} Hz, these studies find that the asymmetric explosion of the white dwarf would generate a short-duration GW signal between ~0.4 Hz and ~2.5 Hz, the exact frequency depends on the specifics of the model.

In the fortunate event that we observe a SN Ia, this multimessenger approach, leveraging both GW and EM information, promises significant progress in our understanding of SNe Ia, potentially directly resolving longstanding questions about their progenitors and providing crucial insights into the explosion mechanism.

3.3. Expectations for neutrino emission

Neutrinos represent yet another messenger that could offer valuable insights into supernovae (e.g. Janka 2017). For example, neutrinos from a core-collapse supernova were observed in 1987 (e.g. Hirata 1987). Despite the very limited signal, they provided valuable insights into multiple neutrino properties and helped test the fundamental principles of the core-collapse explosion mechanism. Should we detect a neutrino signal from a SN Ia, it would offer direct insights into the explosion mechanism (Nomoto et al. 1993; Odrzywolek & Plewa 2011; Wright et al. 2016, 2017).

In SNe Ia, neutrinos are mainly produced in the first second immediately after thermonuclear burning. They are produced primarily via two processes: electron captures on protons, neutrons, and nuclei (mainly 12C and 16O for white dwarfs that can undergo SNe Ia), and thermal production (e.g. electronpositron annihilation, bremsstrahlung, and recombination processes). Compared to core-collapse (type II) supernovae, however, both neutrino production channels are weaker by many orders of magnitude. In the pre-explosion phase, the typical densities of white dwarfs are not high enough to overcome the threshold energy for electron capture reactions. These conditions can only be met for a short duration (of the order of couple of seconds) during thermonuclear burning. Thermal neutrino production is also lower because the temperatures in SN Ia explosions are lower compared to those in the corecollapse supernovae (10^9 K vs. 10^{11} K). In fact, considering a near-Chandrasekhar mass SN Ia model Seitenzahl et al. (2015) obtained a total neutrino luminosity (generated by both types of neutrino production processes) of the order of 10^{49} erg s⁻¹, while core-collapse supernovae produce an energy flux of the order of $10^{53} \text{ erg s}^{-1} \text{ over } 10 \text{ s.}$

Given the weaker neutrino production in SNe Ia, the detection prospects are significantly lower compared to corecollapse supernovae. Wright et al. (2016) calculated interaction rates for various detectors, including the Super-Kamiokande (Super-K; Fukuda 2003), future Hyper-Kamiokande (Hyper-K; Hyper-Kamiokande Proto-Collaboration 2018), Jiangmen Underground Neutrino Observatory (JUNO; An 2016), Deep Underground Neutrino Experiment (DUNE; Abi et al. 2020), and IceCube Neutrino Observatory (IceCube; Aartsen 2017). They found that at a distance of 10 kpc, which is a likely distance due to the peak of stellar density near the Galactic centre at ~8 kpc, the expected number of neutrino interactions is very low. Specifically, Super-K, JUNO, and DUNE are expected to detect only a few events, while Hyper-K may observe several tens of events. At 1 kpc, a distance at which a SN Ia is much less likely, JUNO, Super-K, and DUNE are expected to register a few events, while IceCube and Hyper-K would register several tens of events.

The neutrino calculations discussed above have been performed for single-degenerate near-Chandrasekhar mass SN Ia models. In this scenario, it has even been suggested that based on neutrino emission one would be able to differentiate between different detonation mechanisms (Wright et al. 2017). However, given lower densities and temperatures in the sub-Chandrasekhar double-detonation scenario considered in this study, we expect neutrino emission and prospects for detection to be even lower, of the order of 10^{45} erg s⁻¹. In fact, detecting neutrinos from a SN Ia would be a strong indication of explosive nuclear burning at densities above $10^9 \,\mathrm{g \, cm^{-3}}$, which would suggest a near-Chandrasekhar mass white dwarf undergoing deflagration (Seitenzahl et al. 2015). A non-detection of a neutrino signal, on the other hand, would favour models involving detonations in less massive white dwarfs, such as the violent merger or doubledetonation models.

4. Summary and conclusions

The nature of SNe Ia has long been one of the most debated open questions in astrophysics. In this study, we reviewed the expected insights that GW observations with LISA will provide about these transient phenomena. In particular, we argue that GW observations provide the most promising way for testing the so-called double-degenerate progenitor scenario, which involves a binary comprising two white dwarfs that either interact with each other or merge via GW radiation, resulting in a SN Ia. LISA's ability to survey WD+WD binaries across the entirety of the Milky Way makes it an ideal tool for testing this progenitor scenario.

In addition to LISA's science objectives outlined in Colpi et al. (2024), we provide some quantitative estimates on the science that LISA will likely deliver in the context of SNe Ia:

- A complete sample of Galactic WD+WD binaries with GW frequencies above 2–3 mHz, corresponding to orbital periods shorter than 16–11 minutes. This implies that by simply counting WD+WD binaries in the LISA sample without any concerns regarding selection effects we will be able to estimate whether there are enough double-degenerate binaries in the Milky Way to account for the observed SN Ia merger rate.
- Constraints on the binary chirp mass to better than 1% at frequencies of 4–6 mHz. This, in turn, will allow us to set a lower bound on the primary mass and to differentiate which WD+WD binaries in the LISA's sample will eventually result in a SN Ia ($m_1 > 0.8 M_{\odot}$).
- Constraints on the merger rate of WD+WD binaries in the Milky Way to better than 4–9% (depending on the true WD+WD merger rate). If this turns out to be consistent with the SN Ia rate measured based on EM observations in Milky Way-like galaxies, it would be persuasive evidence in favour of the double-degenerate scenario.

We also discussed the possibility of a direct observation of a final inspiral and SN Ia event; based on observational estimates, the likelihood of this is 3-7% for an extended LISA mission duration of 10 yr. We have illustrated the expected GW signal for a double-degenerate scenario in which the primary white dwarf

undergoes double detonation. In this case, the ignition and explosion of the primary occur prior to the merger, leading to a 'clean' disappearance of the binary's quasi-monochromatic GW signal. We speculate that even a single multi-messenger detection would significantly advance the modelling of SN Ia explosions, reducing the parameter space on the initial conditions (based on constraints from the GW inspiral) and final EM ejecta. If we observe a quasi-monochromatic GW signal around 90 mHz – the exact frequency depends on the binary - followed by the detection of an EM signal and a subsequent shut off of the GW signal, we would confirm the double-degenerate scenario in which a SN Ia results from a double detonation of the primary white dwarf.

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Appendix A: Computation of the gravitational wave signal

Here we briefly summarise the approach for computing the GW signal based on the output of the hydrodynamic simulation as detailed in Seitenzahl et al. (2015) and Morán-Fraile et al. (2023). The amplitude of the GWs can be derived from the second time derivative of the quadrupole moment, following a numerical approach based on the approximate quadrupole formula derived in Blanchet et al. (1990).

The gravitational quadrupole radiation field in the transverse-traceless gauge h_{ij}^{TT} can be written as

$$h_{ij}^{TT}(\mathbf{x},t) = \frac{2G}{c^4 d} P_{ijkl}(\mathbf{n}) \int \rho(2v_k v_l - x_k \partial_l \Phi - x_l \partial_k \Phi) \,\mathrm{d}^3 x, \quad (A.1)$$

where $P_{ijkl}(\mathbf{n}) = (\delta_{ij} - n_i n_k)(\delta_{jl} - n_j n_k) - \frac{1}{2}(\delta_{ij} - n_i n_j)(\delta_{kl} - n_k n_l)$ is the transverse-traceless projection operator, with $\mathbf{n} = \mathbf{x}/d$ being the normalised position vector, ρ is the density, \mathbf{v} is the velocity, ∂_i denotes a partial derivative with respect to the spatial coordinate *i*, and Φ is the Newtonian gravitational potential; as before, *G* is the gravitational constant, *c* is the speed of light, and $d = |\mathbf{x}|$ is the distance to the source.

The amplitude of the GW radiation field can be written in terms of the two unit linear polarisation tensors e_+ and e_{\times} , and for a chosen line of sight, the GW strain takes the form

$$h_{ij}^{TT}(\mathbf{x},t) = \frac{1}{d} (A_+ e_{ij}^+ + A_\times e_{ij}^\times), \tag{A.2}$$

where A_+ and A_{\times} are the amplitudes of the two GW polarisation at the source.

As an example, we considered the most optimistic scenario for detectability, corresponding to a face-on binary orientation. This means that the orbital plane of the binary is perpendicular to the line of sight, which we assumed to be in the *z*-direction. In this case, the polarisation amplitudes are given by

$$A_z^+ = A_{xx} - A_{yy} \tag{A.3}$$

and

$$\mathbf{A}_{z}^{\times} = 2A_{xy},\tag{A.4}$$

with A_{ij} defined as

$$A_{ij} = \frac{G}{c^4} \int \rho(2v_i v_j - x_i \partial_j \Phi - x_j \partial_i \Phi) \,\mathrm{d}^3 x. \tag{A.5}$$

We represent A_z^+ in Fig. 4 to provide a visual example that maximises the detectability of the GW signal. For different binary inclination angles, the relative amplitudes of the polarisation would vary, affecting the observed signal by a factor of a few; examples of the impact of the inclination on the signal-to-noise ratio for edge-on ($\cos \iota^{inj} = 0$) and face-on ($\cos \iota^{inj} = 1$) cases are presented in Table 1 (see also Shah et al. 2012; Finch et al. 2023). Finally, we note that the GW amplitudes discussed here represent an ideal case, as they need to be combined with the detector's response functions, as detailed in Cutler (1998).