



Effect of redox on Fe–Mg–Mn exchange between olivine and melt and an oxybarometer for basalts

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Abstract

The Fe–Mg exchange coefficient between olivine (ol) and melt (m), defined as $Kd_{Fe^T-Mg} = (Fe_{ol}/Fe_m) \cdot (Mg_m/Mg_{ol})$, with all Fe^T expressed as Fe^{2+} , is one of the most widely used parameters in petrology. We explore the effect of redox conditions on Kd_{Fe^T-Mg} using experimental, olivine-saturated basaltic glasses with variable H_2O (≤ 7 wt%) over a wide range of fO_2 (iron-wüstite buffer to air), pressure (≤ 1.7 GPa), temperature (1025–1425 °C) and melt composition. The ratio of Fe^{3+} to total Fe ($Fe^{3+}/\sum Fe$), as determined by Fe K-edge μ XANES and/or Synchrotron Mössbauer Source (SMS) spectroscopy, lies in the range 0–0.84. Measured $Fe^{3+}/\sum Fe$ is consistent (± 0.05) with published algorithms and appears insensitive to dissolved H_2O . Combining our new data with published experimental data having measured glass $Fe^{3+}/\sum Fe$, we show that for Fo_{65-98} olivine in equilibrium with basaltic and basaltic andesite melts, Kd_{Fe^T-Mg} decreases linearly with $Fe^{3+}/\sum Fe$ with a slope and intercept of 0.3135 ± 0.0011 . After accounting for non-ideal mixing of forsterite and fayalite in olivine, using a symmetrical regular solution model, the slope and intercept become 0.3642 ± 0.0011 . This is the value at Fo_{50} olivine; at higher and lower Fo the value will be reduced by an amount related to olivine non-ideality. Our approach provides a straightforward means to determine $Fe^{3+}/\sum Fe$ in olivine-bearing experimental melts, from which fO_2 can be calculated. In contrast to Kd_{Fe^T-Mg} , the Mn–Mg exchange coefficient, Kd_{Mn-Mg} , is relatively constant over a wide range of P–T– fO_2 conditions. We present an expression for Kd_{Mn-Mg} that incorporates the effects of temperature and olivine composition using the lattice strain model. By applying our experimentally-calibrated expressions for Kd_{Fe^T-Mg} and Kd_{Mn-Mg} to olivine-hosted melt inclusions analysed by electron microprobe it is possible to correct simultaneously for post-entrapment crystallisation (or dissolution) and calculate melt $Fe^{3+}/\sum Fe$ to a precision of ≤ 0.04 .

Keywords Olivine · Experiments · Melt inclusions · μ XANES · Mössbauer · Oxygen fugacity

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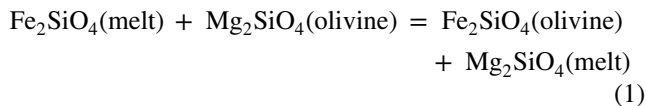
Introduction

The exchange of iron and magnesium between olivine and coexisting melt bears directly on the generation and chemical evolution of basaltic magmas. Consequently, the

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Fe–Mg exchange coefficient, $Kd_{\text{Fe-Mg}}$, is one of the mostly widely used parameters in petrology.

$Kd_{\text{Fe-Mg}}$ is related to the equilibrium constant for the exchange reaction:



and is defined as

$$Kd_{\text{Fe}^{2+}\text{-Mg}} = \frac{(\text{Fe}^{2+}/\text{Mg})_{\text{ol}}}{(\text{Fe}^{2+}/\text{Mg})_{\text{melt}}}, \quad (2)$$

where Fe^{2+} and Mg are expressed as atomic concentrations. At equilibrium $Kd_{\text{Fe}^{2+}\text{-Mg}}$ is expected to vary with the free energy of exchange reaction (1) for the pure end-members, as well as any non-ideal interactions of Fe^{2+} and Mg dissolved in melts and in olivine. As the enthalpies, entropies and volumes of fusion of the olivine end-members forsterite and fayalite are somewhat different from each other (e.g., Lange and Carmichael 1990) one would expect, a priori, some temperature and pressure dependence of $Kd_{\text{Fe}^{2+}\text{-Mg}}$. In addition, the non-ideality of silicate melts and, to a lesser extent, of olivine solid solutions would be expected to confer significant compositional dependence on $Kd_{\text{Fe}^{2+}\text{-Mg}}$. However, despite these expectations, the seminal work of Roeder and Emslie (1970) showed that $Kd_{\text{Fe}^{2+}\text{-Mg}}$ is remarkably constant over a wide range of pressure, temperature and composition (P–T–X), such that a value of 0.30 ± 0.03 can be used with some confidence to describe melting and crystallisation in a wide variety of olivine-bearing systems. We refer to this as the ‘canonical’ value of $Kd_{\text{Fe}^{2+}\text{-Mg}}$.

There have been many subsequent studies of olivine–melt equilibrium (e.g., Ulmer 1989; Beattie et al. 1991; Beattie 1993; Herzberg and O’Hara 2002; Toplis 2005; Mysen 2006; Matzen et al. 2011; Putirka 2016) and associated attempts to refine the canonical value or establish its sensitivity to P–T–X, but it has remained one of the most durable underpinning tenets of basalt petrology, used in a wide variety of ways, from tests of the primitive (i.e., mantle-derived) character of basaltic magmas, to corrections for post-entrapment crystallisation of melt inclusions, to fractionation of basaltic magmas in the crust and mantle.

A particular challenge with using Eq. (1) is the need to know the Fe^{3+} content of the silicate melt, which is not readily measurable by conventional electron microprobe techniques (see review by Hughes et al. 2018). Olivine contains negligible Fe^{3+} (less than a few thousand ppm and not more than a few percent of the total Fe, Fe^{T} ; Ejima et al. 2018) so that where Fe^{3+} in the melt is low, i.e., in relatively reduced systems, $Kd_{\text{Fe}^{2+}\text{-Mg}}$ can be used with confidence assuming that $\text{Fe}^{2+} = \text{Fe}^{\text{T}}$. In such cases

a variant of Eq. (2), with all Fe expressed as Fe^{T} , i.e., $\text{Fe}^{\text{T}} = \Sigma\text{Fe} = \text{Fe}^{2+} + \text{Fe}^{3+}$, may be used instead:

$$Kd_{\text{Fe}^{\text{T}}\text{-Mg}} = \frac{(\text{Fe}^{\text{T}}/\text{Mg})_{\text{ol}}}{(\text{Fe}^{\text{T}}/\text{Mg})_{\text{melt}}}. \quad (3)$$

Most natural magmatic systems contain some Fe^{3+} , thus $Kd_{\text{Fe}^{\text{T}}\text{-Mg}}$, as expressed in (3), will be sensitive to redox state. $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratios vary widely in basaltic magmas, from almost zero in the case of lunar basalts to >0.5 in the case of some oxidised, hydrous subduction-related igneous rocks (Stolper and Bucholz 2019). Moreover, even at constant P, T and $f\text{O}_2$, $\text{Fe}^{3+}/\Sigma\text{Fe}$ is known to vary with melt composition (Kress and Carmichael 1991; Putirka 2016; Borisov et al. 2018). For example, elevated $\text{Fe}^{3+}/\Sigma\text{Fe}$ occurs in alkaline basaltic magmas due to the stabilising effect of Na^+ and K^+ on Fe^{3+} (Mysen and Virgo 1989; Kress and Carmichael 1991). Thus, in some tectonic environments, $Kd_{\text{Fe}^{\text{T}}\text{-Mg}}$ can be lower than $Kd_{\text{Fe}^{2+}\text{-Mg}}$ by as much as a factor of two or more, with far-reaching implications for olivine–melt equilibrium in basaltic systems.

If the availability of Fe^{2+} in the melt is the dominant control on Fe–Mg exchange, then $Kd_{\text{Fe}^{\text{T}}\text{-Mg}}$ should vary systematically with the redox state of the system; the relationship between $Kd_{\text{Fe}^{\text{T}}\text{-Mg}}$ and $Kd_{\text{Fe}^{2+}\text{-Mg}}$ will reflect the proportion of total iron in the melt that is trivalent (Fe^{3+}) at the pressure, temperature and melt composition of interest:

$$Kd_{\text{Fe}^{\text{T}}\text{-Mg}} = Kd_{\text{Fe}^{2+}\text{-Mg}} \times \left(1 - \frac{\text{Fe}^{3+}}{\Sigma\text{Fe}}\right). \quad (4)$$

Recognising the problem of Fe^{3+} in the melt Roeder and Emslie (1970) attempted to account for its effect by determining, via wet chemistry, the $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratio of their bulk experimental charges and making a correction for any contained olivine crystals using a simple mass balance. The behaviour predicted in Eq. (4) is apparent in the original Roeder and Emslie (1970) dataset (Fig. 1), although the uncertainty in the $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratio of the glass (as opposed to the bulk) precludes any meaningful conclusions. For example, it is unclear if the scatter in Fig. 1 arises due to temperature or compositional effects, the use of different capsule materials (and attendant Fe loss from the glass), or the presence of crystals in the aliquot of the experimental charge used for measuring $\text{Fe}^{3+}/\Sigma\text{Fe}$. The scatter is not removed even when more sophisticated mass balance techniques are used, taking into account other iron-bearing mineral phases in the glass, e.g., clinopyroxene, magnetite (Matzen, 2012). However, in principle, if we know the redox state of a magmatic system, usually defined in terms of an oxygen fugacity ($f\text{O}_2$), and the relationship between $f\text{O}_2$ and $\text{Fe}^{3+}/\Sigma\text{Fe}$, then we should be able to use Eq. (4) as an oxybarometer. The potential of this approach was recognised by Putirka (2016)

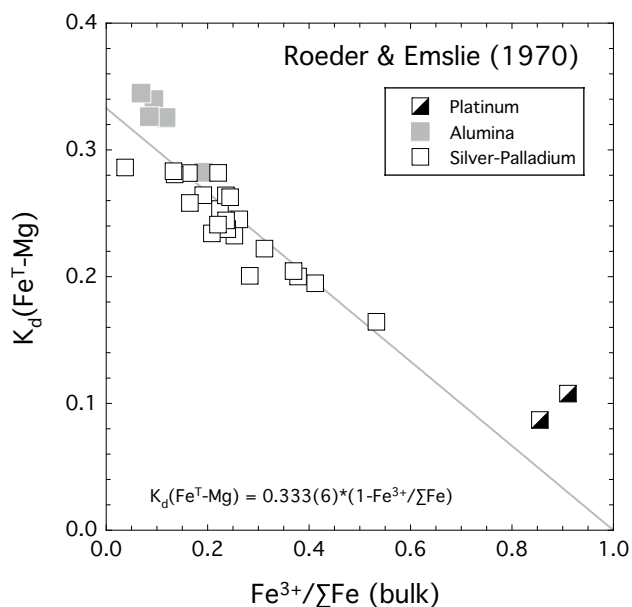


Fig. 1 Variation of olivine-melt $K_{d_{\text{Fe}^T-\text{Mg}}}$ with $\text{Fe}^{3+}/\Sigma\text{Fe}$ in the bulk experimental run product from the seminal experimental study of Roeder and Emslie (1970). Results for three different capsule materials are shown. The data hint at the operation of a relationship akin to Eq. (4), but the measurement of $\text{Fe}^{3+}/\Sigma\text{Fe}$ is insufficiently precise for a more thorough treatment because of the need to correct the bulk $\text{Fe}^{3+}/\Sigma\text{Fe}$ analysis for included, Fe-bearing crystalline phases. The line and equation correspond to fits to Eq. (4), for comparison to Fig. 6a

who developed an expression for $K_{d_{\text{Fe}^T-\text{Mg}}}$ that explicitly includes an $f\text{O}_2$ term. However, the form of his Eq. (9b) is not optimised for oxybarometry, partly because of the way the fitting was performed, and partly because of the dearth of experimental olivine-melt data with measured $\text{Fe}^{3+}/\Sigma\text{Fe}$.

Application of Eq. (4) as an oxybarometer requires, of course, that the olivine-melt pair of interest is in equilibrium. When $\text{Fe}^{3+}/\Sigma\text{Fe}$ in the melt is unknown, the problem of testing for equilibrium and calculating $f\text{O}_2$ becomes circular. To resolve this circularity requires understanding the behaviour of a component that is not redox-sensitive, such as exchange of Mn and Mg between olivine and melt, $K_{d_{\text{Mn}-\text{Mg}}}$. If the difference between the behaviour of Fe and Mn can be quantified, it has the potential to be used to test for olivine-melt equilibrium and so enable oxybarometry. The aim of this study is to (a) compare methods for the reliable, high-spatial resolution measurement of the Fe^{3+} content of hydrous and anhydrous glasses of broadly basaltic composition synthesised over a range of $f\text{O}_2$; and (b) determine the partitioning of Fe, Mg and Mn between olivine and basaltic melt across a wide range of redox conditions. The ultimate objective is to establish whether Eq. (4) provides a useful means to correct $K_{d_{\text{Fe}^T-\text{Mg}}}$ for Fe^{3+} -rich systems, and whether it is possible to recover $f\text{O}_2$ from determinations of $K_{d_{\text{Fe}^T-\text{Mg}}}$ in natural or

experimental basaltic systems by exploiting the redox insensitive exchange of Mn and Mg between olivine and melt.

Experimental methods

This study utilises 72 experimental samples, mainly from our previously published studies with existing, modified or new determinations of the $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratio in the glass to explore the effect of redox on $K_{d_{\text{Fe}^T-\text{Mg}}}$. Our experimental starting materials comprised eight basalts, two basaltic andesites and one andesite, all based on natural rock compositions from subduction-related magmatic systems: Lesser Antilles arc (St. Vincent, Grenada, Martinique, St. Kitts, Montserrat), Central American arc (Masaya), Aeolian arc (Stromboli), and the post-collisional, calc-alkaline Adamello Batholith, Italy. For St. Vincent and Martinique we used three and two different starting materials, respectively; these are referred to as St. Vincent series 1, 2 and 3, and Martinique series 1 and 2. MgO contents of the starting materials range from 2.3 to 17.1 wt%; total alkali contents range from 1.6 to 4.7 wt%. Mg#, expressed in terms of Fe^T (i.e., molar $\text{Mg}/[\text{Mg} + \text{Fe}^T]$) ranges from 0.34 to 0.76. Compositions, on an anhydrous basis, of all eleven starting materials are given in Table 1. None of the studied glasses contain sulphur, to prevent possible modifications of $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratios due to the homogeneous reaction $\text{S}^{2-} + 8\text{Fe}^{3+} = \text{S}^{6+} + 8\text{Fe}^{2+}$ during quenching of the glass (Nash et al. 2019).

With the exception of the three ‘XANES’ experiments (see Supplementary Method in supplementary material 3) all of the experimental runs are taken from the published studies listed in Tables 1 and 2, where the experimental techniques are described in detail, and summarised as follows. One-atmosphere experiments (Adamello series) were run in vertical quench furnaces at the Geophysical Laboratory, Carnegie Institution of Washington, with CO–CO₂ gases to regulate $f\text{O}_2$ using methods described in Ulmer (1989) and Kägi et al. (2005). One-atmosphere experiments (Grenada series) were run in vertical quench furnaces at University of Bristol and Australian National University with CO–CO₂ gases to regulate $f\text{O}_2$ using methods in Stamper et al. (2014). Internally-heated pressure vessel (IHPV) runs (St. Vincent 2 and 3, St. Kitts, Martinique 1 and 2, and Montserrat series) were performed at Université d’Orléans using techniques reported by Pichavant et al. (2002) and Melekhova et al. (2017) with $f\text{O}_2$ controlled by H₂ added to the argon pressurising gas, and $f\text{O}_2$ monitored using an NiPd sensor. IHPV experiments at Leibnitz University of Hannover (Stromboli and Masaya series) were run using the methods described in Lesne et al. (2011), without H₂ control. Piston cylinder (St. Vincent 1 and Grenada series) runs were performed in half-inch pressure cells at University of Bristol using

Table 1 Starting compositions used in experiments

Series	Adamello	Grenada	St Vincent 1	St Vincent 2	St Vincent 3	Stromboli	Montserrat	Martinique 1	St Kitts	Martinique 2	Masaya
Sample	RC158c	GRN15	RSV49	STV301	STV315	St8.1.B	MVO788	031-22b	KSI_BR	MT33S	MAS.1.B
SiO ₂	47.67	46.26	47.63	46.97	51.96	52.29	49.27	53.65	55.00	62.25	51.49
TiO ₂	0.73	0.93	0.75	1.09	0.78	0.85	1.00	0.81	0.96	0.46	1.20
Al ₂ O ₃	12.87	12.84	14.54	15.66	17.12	18.78	20.28	19.07	18.47	17.84	19.00
FeO ^T	9.41	9.20	9.00	9.14	8.54	7.37	9.06	8.13	8.69	6.09	11.34
MnO	0.19	0.19	0.16	0.19	0.16	0.00	0.10	0.25	0.25	0.18	0.00
MgO	17.13	15.17	14.62	12.73	7.74	6.07	5.46	4.47	3.97	2.25	3.21
CaO	10.38	12.80	10.78	11.42	10.74	11.20	11.66	9.86	8.61	6.28	9.53
Na ₂ O	1.22	2.05	2.29	2.32	2.62	2.00	2.62	3.02	3.56	3.60	2.94
K ₂ O	0.40	0.57	0.24	0.47	0.34	1.45	0.55	0.74	0.49	1.05	1.31
Mg#	0.764	0.746	0.743	0.713	0.617	0.595	0.518	0.495	0.448	0.397	0.335
Reference	1	2	3	4	4	5	6	7	8	7	5

1. Ulmer (1989); Kägi et al. (2005)
2. Stamper et al. (2014)
3. Melekhova et al. (2015)
4. Pichavant and Macdonald (2007)
5. Lesne et al. (2011)
6. Pichavant (unpublished)
7. Pichavant et al. (2002)
8. Melekhova et al. (2017)

Table 2 Experimental run conditions and products

Starting material	Run	Source ^a	Method ^b	Capsule or wire	P (MPa)	T (°C)	logO ₂	ΔNNO ^d	Phase assemblage ^c (wt proportions)	H ₂ O ^f (wt%)	CO ₂ ^f (ppm)
St8.1.B	ST8_IB4	L11	IHPV-H	Au ₈₀ Pd ₂₀	300	1150			gl (100)	3.66 (15)	920 (92)
St8.1.B	ST8_IB5	L11	IHPV-H	Au ₈₀ Pd ₂₀	150	1150			gl (100)	3.12 (15)	230 (23)
St8.1.B	ST8_IB7	L11	IHPV-H	Au ₈₀ Pd ₂₀	50	1150			gl (100)	2.20 (16)	60 (5)
MAS.1.B	MAS1_B4	L11	IHPV-H	Au ₈₀ Pd ₂₀	300	1150			gl (100)	3.00 (15)	705 (71)
KS_BR1	Run1#1	M17	IHPV-O	Au	240	1025	-9.6	0.3	gl (100)	5.90 (20)	16 (1)
KS_BR1	Run1#2	M17	IHPV-O	Au	240	1025	-10.3	-0.4	gl(57) ol(3) opx(tr) cpx(7) pl(31) mag(1)	3.80 (10)	813 (10)
RSV49	RSV49-4a ^e										
RSV49	RSV49-4b ^e	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1270			gl(94) ol(5) sp(1)	0.60 (1)	
RSV49	RSV49-4c ^e										
RSV49	BM40	M15	PC	Au ₈₀ Pd ₂₀ /Pt	700	1150			gl(80) ol(13) cpx(6) sp(1)	3.05 (9)	
RSV49	BM6	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1100	-9	-0.4	gl(76) ol(1) cpx(10) sp(4)	4.42 (35)	6483 (193)
RSV49	BM33	M15	PC	Au ₈₀ Pd ₂₀ /Pt	700	1200			gl(99) sp(1)	4.46 (15)	
RSV49	BM37	M15	PC	Au ₈₀ Pd ₂₀ /Pt	700	1150			gl(82) ol(13) cpx(3) mg(2)	5.20 (14)	
RSV49	BM34	M15	PC	Au ₈₀ Pd ₂₀ /Pt	700	1100			gl(40) ol(6) cpx(15) amph(35) mag(4)	7.20 (21)	
RSV49	BM46a ^e										
RSV49	BM46b ^e	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1300	1250			gl(98) sp(2)	4.52 (13)	
RSV49	BM46c [§]										
RSV49	RSV49-2	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1350			gl(100)	0.60 (1)	
RSV49	BM38	M15	PC	Au ₈₀ Pd ₂₀ /Pt	700	1200			gl(92) ol(7) sp(1) qu	2.50 (8)	
RSV49	BM3	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1200			gl(81) ol(12) cpx(4) sp(3) qu	2.94 (20)	
RSV49	BM9	M15	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1100	-8	0.6	gl(79) ol(12) cpx(7) sp(2) qu	5.34 (10)	8087 (65)
RSV49	BM17	M15	PC	Au ₉₀ Pd ₁₀ /Pt	1000	1080	-8.1	0.8	gl(74) ol(9) cpx(14) sp(3) qu	6.70 (12)	6864 (200)
RSV49	XANES9	this study	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1250			gl (100)	3.38 (14)	320 (44)
RSV49	XANES2	this study	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1250			gl (95) ol(5) sp(tr)	5.63 (13)	3159 (77)
RSV49	XANES11	this study	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1200			gl(91) ol(8) sp(1)	5.60 (15)	
STV315	6-4	PM07	IHPV-O	Au ₇₀ Pd ₃₀	415	1155	-8.1	0	gl (100)	4.37 (5)	666 (49)
STV301	7-2	PM07	IHPV-O	Au ₇₀ Pd ₃₀	420	1198	-5.3	2.39	gl(96) ol(3) sp(1) qu	4.70 (60)	
STV301	7-3	PM07	IHPV-O	Au ₇₀ Pd ₃₀	420	1198	-6.1	1.59	gl(91) ol(8) sp(1) qu	2.27 (19)	1335 (65)
STV301	3-1	PM07	IHPV-O	Au ₇₀ Pd ₃₀	400	1092	-8.5	0.47	gl(88) ol(11) sp(1)	5.82 (2)	698 (70)
031-22b	HAB-18	P02	IHPV-O	Au	395	1016	-9.4	0.62	gl(96) pl(2) cpx(1)	5.40 (50)	
031-22b	HAB-20	P02	IHPV-O	Au	406	1000	-6.7	3.55	gl(92) cpx(3) mg(5)	8.30 (50)	
031-22b	HAB-23	P02	IHPV-O	Au	406	1025	-5.9	3.99	gl(95) mg(5)	8.30 (50)	
MT33S	HAB-26/P1D	P02	IHPV-O	Au	399	952	-7	4	gl(96) mg(4)	7.90 (50)	
MVO788	MVO2	This study	IHPV-O	Au	403	1000	-9.8	0.46	gl (89) amph(9) pl(2)	6.52 (37)	1559 (120)
MVO788	MVO1	This study	IHPV-O	Au	403	1000	-9.7	0.56	gl(87) amph(13)	7.58 (13)	135 (10)
GRN-15	W1	S14	PC	Au ₉₀ Pd ₁₀ /Pt	700	1150			gl(82) ol(13) cpx(5) sp(tr)	5.15 (38)	2504 (430)
GRN-15	W3	S14	PC	Au ₈₀ Pd ₂₀ /Pt	700	1200			gl(97) ol(3) sp(tr)	3.62 (18)	236 (12)

Table 2 (continued)

Starting material	Run	Source ^a	Method ^b	Capsule or wire	P (MPa)	T (°C)	logO ₂	ΔNNO ^d	Phase assemblage ^c (wt proportions)	H ₂ O ^f (wt%)	CO ₂ ^f (ppm)
GRN-15	AN-2	S14	PC	Pd	700	1425			gl (100)	0.32 (1)	516 (27)
GRN-15	R-5	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1280			gl(93) ol(6) sp(1)	2.60 (24)	2473 (122)
GRN-15	33	S14	PC	Au ₇₅ Pd ₂₅ /Pt	1000	1325			gl (100)	2.48 (8)	11694 (252)
GRN-15	AN-3	S14	PC	Au ₇₅ Pd ₂₅ /Pt	1000	1400			gl(98) ol(2) sp(tr)	0.35 (4)	723 (26)
GRN-15	30	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1300	1280			gl(92) ol(4) cpx(3) sp(tr)	3.73 (7)	1586 (96)
GRN-15	D-11	S14	GMF-A	Pd wire	0.1	1241	- 6.48	0.81	gl(84) ol(11) sp(5)		
GRN-15	D-10	S14	GMF-A	Au ₈₀ Pd ₂₀	0.1	1280	- 4.81	2.08	gl(89) ol(7) sp(4)		
GRN-15	D-13	S14	GMF-A	Re wire	0.1	1283	- 9.32	- 2.46	gl(92) ol (6) sp(2)		
GRN-15	D-8	S14	GMF-A	Pd wire	0.1	1292	- 7.29	- 0.52	gl(90) ol(8) sp(2)		
GRN-15	D-12	S14	GMF-A	Au ₈₀ Pd ₂₀ /Pt	0.1	1296	- 6.62	0.11	gl(93) ol(4) sp(3)		
GRN-15	RD-1	S14	GMF-B	Au ₈₀ Pd ₂₀ /Pt	0.1	1300	- 6.07	0.62	gl(93) ol(6) sp(1)		
GRN-15	D-7	S14	GMF-B	Au ₈₀ Pd ₂₀ /Pt	0.1	1300	- 2.9	3.79	gl(96) ol(3) sp(1)		
GRN-15	35	S14	TZM	Au ₈₀ Pd ₂₀	150	1200			gl(96) ol(3) sp(1)	1.97 (148)	360 (30)
GRN-15	41	S14	PC	Au ₈₀ Pd ₂₀ /Pt	700	1200			gl(98) ol(10) cpx(1) sp(1)	3.68 (14)	1565 (174)
GRN-15	23	S14	PC	Au ₈₀ Pd ₂₀ /Pt	700	1275			gl(94) ol(5) sp(1)	3.30 (12)	1456 (61)
GRN-15	25	S14	PC	Au ₈₀ Pd ₂₀ /Pt	700	1280			gl(95) ol(4) sp(1)	3.43 (25)	1960 (1181)
GRN-15	36	S14	PC	Au ₇₅ Pd ₂₅ /Pt	700	1325			gl(100)	4.48 (20)	3226 (791)
GRN-15	AN-1	S14	PC	Au ₇₅ Pd ₂₅ /Pt	700	1400			gl(96) ol(4) sp(tr)	0.34 (10)	393 (22)
GRN-15	R-2	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1265			gl(83) ol(10) cpx(7) sp(tr)	3.44 (37)	3126 (234)
GRN-15	22	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1265			gl(81) ol(8) cpx(10) sp(1)	2.85 (30)	1822 (116)
GRN-15	R-1	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1300			gl(93) ol(6) sp(1)	2.95 (34)	2080 (15)
GRN-15	28	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1000	1300			gl(96) ol(4) sp(tr)	3.17 (24)	1193 (176)
GRN-15	R-6	S14	PC	Au ₇₅ Pd ₂₅ /Pt	1000	1325			gl(98) ol(1) sp(1)	2.98 (18)	2309 (128)
GRN-15	12	S14	PC	Au ₉₀ Pd ₁₀ /Pt	1300	1200			gl(62) ol(8) cpx(27) sp(2)	3.97 (20)	3106 (277)
GRN-15	10	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1300	1250			gl(81) ol(8) cpx(9) sp(1)	3.95 (20)	6540 (1086)
GRN-15	15	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1300	1265			gl(85) ol(8) cpx(6) sp(tr)	3.72 (10)	1608 (177)
GRN-15	32	S14	PC	Au ₈₀ Pd ₂₀ /Pt	1700	1280			gl(82) ol(3) cpx(14) sp(1)	3.62 (1)	1692 (168)
GRN-15	38	S14	PC	Au ₇₅ Pd ₂₅ /Pt	1700	1360			gl(100)	2.99 (12)	1610 (40)
RC158c	PU1	U89	GMF-G	Pt wire	0.1	1350	- 9	- 2.78	gl(91) ol(9)		
RC158c	PU4	U89	GMF-G	Pt wire	0.1	1250	- 10	- 2.8	gl(81) ol(19)		
RC158c	PU2	U89	GMF-G	Pt wire	0.1	1300	- 9.5	- 2.81	gl(86) ol(14)		
RC158c	PU5	U89	GMF-G	Pt wire	0.1	1400	- 8.5	- 2.73	gl(99) ol(1)		
RC158c	PU364	K05	GMF-G	Pt wire	0.1	1300	- 6.7	0	gl(87) ol(13) sp(tr)		
RC158c	PU363	K05	GMF-G	Pt wire	0.1	1250	- 7.2	0	gl(83) ol(17) sp(tr)		
RC158c	PU351	K05	GMF-G	Pt wire	0.1	1250	- 0.68	6.52	gl(86) ol(13) sp(tr)		
RC158c	PU56	K05	GMF-G	Pt wire	0.1	1300	- 0.68	6.01	gl(91) ol(8) sp(1)		

Table 2 (continued)

Starting material	Run	Source ^a	Method ^b	Capsule or wire	P (MPa)	T (°C)	log f_{O_2}	Δ NNO ^d	Phase assemblage ^c (wt proportions)	H ₂ O ^f (wt%)	CO ₂ ^f (ppm)
RC158c	PU359	K05	GMF-G	Pt wire	0.1	1300	-6.7	0	gl(90) ol(10) sp(tr)		
RC158c	PU58	K05	GMF-G	Pt wire	0.1	1325	-0.68	5.77	gl(95) ol(5) sp(tr)		
RC158c	PU361	K05	GMF-G	Pt wire	0.1	1350	-0.68	5.54	gl(99) ol(1)		

[§]Analysis by SMS of previously irradiated spot to simulate beam damage

^aSources of experiments: L11—Lesne et al. (2011); M17—Melekhova et al. (2017); M15—Melekhova et al. (2015); PM07—Pichavant and Macdonald (2007); P02—Pichavant et al. (2002); S14—Stamper et al. (2014); U89—Ulmer (1989); K05—Kägi et al. (2005)

^bExperimental apparatus used: IHPV-H (internally-heated pressure vessel—Hannover); IHPV-O (Orleans); PC (piston cylinder—Bristol); TZM (externally-heated pressure vessel—Bristol); GMF-A (gas mixing furnace—ANU); GMF-B (Bristol); GMF-G (Geophysical Laboratory)

^cPhase abbreviations: *gl* glass, *ol* olivine, *cpx* clinopyroxene, *pl* plagioclase, *amph* amphibole, *sp* chrome spinel, *mag* magnetite

^d f_{O_2} in log units relative to NNO calculated at P and T using O'Neill and Pownceby (1993). Values estimated using aH_2O from Burnham (1979). Values shown in italics

^eRepeat analyses on different spots of same glass chip

^fVolatiles measured by SIMS or Karl-Fischer titration (Martinique series) except where estimated from glass fraction and starting material (or volatiles by difference) shown in italics

techniques described by Melekhova et al. (2015) and Stamper et al. (2014). Those experiments used a double capsule technique, with sample materials placed in both inner and outer capsules to minimise H loss or gain by diffusion. In some St. Vincent series 1 runs a sensor capsule of pure Pd, loaded with a mixture of Ni, NiO and H₂O, was placed inside the outer capsule to monitor f_{O_2} by means of analyses of NiPd alloys.

All 72 experiments have the $Fe^{3+}/\Sigma Fe$ ratio of their glass determined by one or multiple techniques (see Table 3); two samples have replicate measurements. f_{O_2} was known most precisely in the 18 one-atmosphere runs. In high-pressure runs, performed at water-undersaturated conditions in IHPV or piston cylinder with NiPd sensors, f_{O_2} can be calculated only by taking account of the reduced H₂O activity (aH_2O) in the melt at run conditions. This was done using the method of Burnham (1979). The f_{O_2} of the run is then that of the NiPd sensor plus $2\log(aH_2O)$. This approach, which involves a greater uncertainty than the one-atmosphere experiments, provides f_{O_2} estimates for a further 15 runs. The overall range in measured f_{O_2} these 33 experiments is 9.3 log units relative to the NNO buffer (O'Neill and Pownceby 1993) at experimental P and T (i.e., from NNO - 2.8 to NNO + 6.5). In the remaining 40 experimental runs the experimental f_{O_2} was not precisely constrained.

In addition, we considered another ~ 100 experiments with measured $Fe^{3+}/\Sigma Fe$ ratios for the glass (see below) and a database of over 1000 published olivine-bearing experiments conducted at known f_{O_2} above NNO - 3, to test various aspects of our parameterizations.

Analytical methods

Electron probe microanalysis (EPMA)

Major and minor elements in glasses and minerals in the Adamello (RC158c), St. Vincent 1 (RSV49, XANES) and Montserrat series of experiments were analysed using a Cameca SX100 electron microprobe at University of Bristol. Analytical conditions were: olivine—20 kV primary beam, 10 nA beam current and 1 μ m beam diameter; glass—20 kV, 4 nA and 10 μ m beam. Calibration was performed on a range of mineral, oxide and glass standards. Secondary standards used were: St. John's Island olivine, Kakanui hornblende, diopside, Columbia River Basalt glass (USGS) and an in-house synthetic amphibolite glass (#3570). All other glasses and minerals are those reported by the original authors (Table 1). At least 5 analyses were made of each olivine and glass. The subset of the 72 experiments containing analysed olivine crystals is 52.

Table 3 Measured $Fe^{3+}/\sum Fe$ ratios in experimental glasses using different techniques, and exchange coefficients

Run	$Fe^{3+}/\sum Fe$ SMS	Al foil ^a μm	$Fe^{3+}/\sum Fe$ $\mu XANES$	$Fe^{3+}/\sum Fe$ Mössbauer	$Fe^{3+}/\sum Fe$ Colorimetry	$Fe^{3+}/\sum Fe$ Preferred ^c	$Fe^{3+}/\sum Fe$ KC91 ^e	$Fe^{3+}/\sum Fe$ BBH18 ^e	$Fe^{3+}/\sum Fe$ OBM18 ^e	Kd ^f Fe ⁷ -Mg	Kd ^f Mn-Mg
ST8_IB4	0.287 (20)				0.32 (3)	0.287 (20)					
ST8_IB5	0.368 (24)				0.37 (3)	0.368 (24)					
ST8_IB7	0.325 (25)				0.32 (3)	0.325 (25)					
MAS1_B4	0.289 (16)				0.18 (3)	0.289 (16)					
Run1#1	0.144 (24)					0.144 (24)	0.211	0.162	0.148	0.317 (16)	0.237 (39)
Run1#2	0.137 (48)					0.137 (48)	0.165	0.127	0.105	0.289 (11)	0.199 (59)
RSV49-4a ^d	0.075 (23)	0.115	0.263 (9)			0.075 (23)				0.289 (11)	0.199 (59)
RSV49-4b ^d	0.120 (34)					0.120 (34)				0.289 (11)	0.199 (59)
RSV49-4c ^d	0.101 (34)					0.101 (34)				0.289 (11)	0.199 (59)
BM40	0.272 (21)	0.115	0.388 (8)			0.272 (21)				0.196 (6)	0.204 (45)
BM6	0.043 (32)	0.065	0.360 (14)			0.043 (32)				0.322 (10)	0.158 (42)
BM33	0.083 (22)	0.115	0.433 (19)			0.083 (22)				0.122 (6)	0.169 (40)
BM37	0.530 (23)	0.115	0.550 (29)			0.530 (23)	0.136	0.144		0.121 (9)	0.109 (28)
BM34	0.366 (23)	0.115	0.620 (32)			0.366 (23)					
BM46a ^d	0.130 (23)	0.115	0.450 (15)			0.130 (23)					
BM46b ^d	0.104 (20)					0.104 (20)					
BM46c [§]	0.196 (17)										
RSV49-2		0.115	0.448 (15)							0.192 (6)	0.197 (53)
BM38		0.115	0.534 (18)							0.266 (8)	0.219 (48)
BM3		0.065	0.300 (12)							0.250 (7)	0.218 (40)
BM9		0.065	0.415 (19)				0.200	0.227	0.205	0.170 (10)	0.170 (63)
BM17		0.115	0.553 (29)				0.215	0.244			
XANES9	0.229 (22)	0.065	0.386 (1)	0.20 (3)		0.229 (22)					
XANES2		0.065	0.581 (14)							0.381 (54)	0.231 (12)
XANES11		0.015	0.482 (19)							0.363 (23)	0.242 (10)
6-4	0.083 (42)	0.065	0.366 (13)	0.13 (3)		0.083 (42)	0.176	0.161	0.136		
7-2	0.250 (34)	0.065	0.425 (15)			0.250 (34)	0.377	0.394	0.376	0.226 (11)	0.26 (25)
7-3	0.236 (44)	0.065	0.293 (11)			0.236 (44)	0.304	0.308	0.292	0.257 (13)	0.15 (13)
3-1		0.065	0.459 (16)				0.221	0.197	0.179	0.252 (11)	0.13 (8)
HAB-18	0.111 (26)	0.065	0.358 (13)			0.111 (26)	0.234	0.193	0.186		
HAB-20	0.759 (47)	0.065	0.781 (27)			0.759 (47)	0.563	0.465	0.558		
HAB-23	0.770 (68)	0.065	0.810 (28)			0.770 (68)	0.606	0.529	0.623		
HAB-26/PID	0.470 (30)	0.065	0.702 (24)			0.470 (30)	0.616	0.508	0.603		
MVO2		0.065	0.382 (15)				0.218	0.177	0.178		
MVO1		0.065	0.428 (14)				0.226	0.186	0.180		
W1	0.316 (20)	0.115	0.517 (18)			0.316 (20)				0.211 (7)	0.231 (18)

Table 3 (continued)

Run	Fe ³⁺ /ΣFe SMS	Al foil ^a μm	Fe ³⁺ /ΣFe μXANES	Fe ³⁺ /ΣFe Mössbauer	Fe ³⁺ /ΣFe Colorimetry	Fe ³⁺ /ΣFe Preferred ^c	Fe ³⁺ /ΣFe KC91 ^e	Fe ³⁺ /ΣFe BBH18 ^e	Fe ³⁺ /ΣFe OBMI18 ^e	Kd ^f Fe ⁷ -Mg	Kd ^f Mn-Mg
W3	0.693 (17)	0.115	0.679 (23)			0.693 (17)				0.113 (4)	0.207 (24)
AN-2	0.580 (18)	0.115	0.597 (20)			0.580 (18)					
R-5	0.533 (19)	0.115	0.617 (21)			0.533 (19)				0.147 (8)	0.224 (12)
33	0.314 (25)	0.115	0.490 (17)			0.314 (25)					
AN-3	0.691 (23)	0.115	0.678 (23)			0.691 (23)				0.101 (3)	0.215 (28)
30	0.646 (19)	0.115	0.720 (24)			0.646 (19)				0.116 (6)	0.226 (31)
D-11		0.115	0.258 (9)			0.258 (9)	0.270	0.241	0.209	0.234 (10)	0.233 (40)
D-10		0.115	0.263 (13)			0.263 (13)	0.387	0.372	0.345	0.231 (7)	0.210 (32)
D-13		0.115	0.070 (2)			0.070 (2)	0.066	0.057	0.031	0.302 (8)	0.195 (34)
D-8		0.115	0.085 (3)			0.085 (3)	0.160	0.135	0.100	0.287 (8)	0.251 (44)
D-12		0.115	0.267 (9)			0.267 (9)	0.204	0.189	0.143	0.221 (5)	0.225 (43)
RD-1		0.115	0.229 (8)			0.229 (8)	0.249	0.241	0.191	0.210 (10)	0.240 (30)
D-7		0.115	0.568 (19)			0.568 (19)	0.577	0.595	0.590	0.067 (4)	0.221 (28)
35		0.115	0.830 (28)			0.830 (28)				0.056 (5)	0.203 (25)
41		0.115	0.708 (24)			0.708 (24)				0.128 (8)	0.192 (23)
23		0.115	0.552 (19)			0.552 (19)				0.144 (8)	0.225 (30)
25		0.115	0.614 (21)			0.614 (21)				0.121 (7)	0.212 (28)
36		0.115	0.840 (28)			0.840 (28)					
AN-1		0.115	0.675 (23)			0.675 (23)				0.089 (3)	0.219 (27)
R-2		0.115	0.479 (16)			0.479 (16)				0.183 (7)	0.211 (55)
22		0.115	0.664 (22)			0.664 (22)				0.107 (5)	0.179 (14)
R-1		0.115	0.421 (14)			0.421 (14)				0.222 (3)	0.224 (26)
28		0.115	0.695 (23)			0.695 (23)				0.119 (4)	0.216 (28)
R-6		0.115	0.493 (17)			0.493 (17)				0.185 (4)	0.231 (18)
12		0.115	0.542 (18)			0.542 (18)				0.167 (8)	0.203 (23)
10		0.115	0.475 (16)			0.475 (16)				0.222 (14)	0.225 (15)
15		0.065	0.497 (17)			0.497 (17)				0.195 (11)	0.218 (20)
32		0.115	0.681 (23)			0.681 (23)				0.126 (3)	0.210 (26)
38		0.115	0.770 (26)			0.770 (26)					
PU1		0.065	0.078 (3)			0.078 (3)	0.056	0.052	0.026	0.315 (4)	0.250 (5)
PU4	0.055 (47)	0.065	0.057 (2)			0.055 (47)	0.056	0.050	0.024	0.316 (4)	0.257 (6)
PU2	0.058 (37)	0.065	0.065 (1)			0.058 (37)	0.057	0.048	0.026	0.312 (5)	0.249 (16)
PU5		0.065	0.067 (2)			0.067 (2)	0.060	0.053	0.029	0.303 (6)	0.242 (11)
PU364		0.065	0.200 (7)			0.200 (7)	0.181	0.176	0.125	0.242 (5)	0.228 (15)
PU363	0.230 (37)	0.065	0.218 (8)			0.230 (37)	0.186	0.169	0.130	0.239 (5)	0.221 (5)

Table 3 (continued)

Run	Fe ³⁺ /ΣFe SMS	Al foil ^a μm	Fe ³⁺ /ΣFe μXANES	Fe ³⁺ /ΣFe Mössbauer	Fe ³⁺ /ΣFe Colorimetry	Fe ³⁺ /ΣFe Preferred ^c	Fe ³⁺ /ΣFe KC91 ^e	Fe ³⁺ /ΣFe BBH18 ^e	Fe ³⁺ /ΣFe OBMI18 ^e	Kd ^f Fe ⁷ -Mg	Kd ^f Mn-Mg
PU351	0.800 (32)	0.065	0.814 (2)			0.800 (32)	0.810	0.817	0.858	0.055 (3)	0.190 (13)
PU56	0.800 (37)	0.065	0.778 (27)			0.800 (37)	0.762	0.788	0.812	0.061 (2)	0.206 (15)
PU359		0.115	0.225 (7)			0.225 (7)	0.172	0.175	0.121	0.237 (11)	0.240 (10)
PU58		0.115 ^b	0.769 (24)			0.769 (24)	0.738	0.771	0.785	0.065 (1)	0.207 (4)
PU361		0.065	0.746 (26)			0.746 (26)	0.713	0.751	0.754	0.088 (6)	0.224 (5)

Figures in parentheses denote 2 sd. in terms of least significant digits

[§] Analysis by SMS of previously irradiated spot to simulate beam damage

^a Thickness of aluminium foil used to reduce photon flux for μXANES measurements. See text for details

^b Also analysed with 0.265 μm Al filter

^c Value used for plotting data, unless otherwise specified. See text for selection criteria

^d Repeat analyses on different spots of same glass chip

^e Calculated at experimental P, T, fO₂ and glass composition: Kress and Carmichael (1991) (KC91), Borisov et al. (2018) (BBH18), O'Neill et al. (2018) (OBMI18)

^f Olivine-melt exchange coefficient

Micro X-ray absorption near-edge spectroscopy (μXANES)

Fe³⁺/ΣFe ratios were measured in 66 experimental glasses by μXANES at the Diamond Light Source synchrotron facility, UK, using techniques described in Stamper et al. (2014), with some modifications, as summarized here. μXANES spectra were collected at the Fe K-edge in fluorescence mode on Beamline I18 using the Si(111) monochromator. The beam size at the sample was an ellipse with principal axes approximately 2.5 × 4.5 microns. The incident beam flux was reduced by placing one or more 50 μm-thick aluminium foil sheets in front of the sample in addition to the fixed 15 μm-thick filter used for all analyses (Table 3). The total flux density (defined as total photons delivered per second per square micrometer; Cottrell et al. 2018) is 6.8 × 10¹⁰ (with 15 μm Al filter) or 2.5 × 10¹⁰ photons s⁻¹ μm⁻² (with 15 + 50 μm Al filters). One sample (PU58) was analysed twice with both 65 μm and 115 μm thickness of Al filters (flux density of < 1.1 × 10¹⁰ photons s⁻¹ μm⁻²); the two measured Fe³⁺/ΣFe ratios are 0.761 and 0.777; the mean is reported in Table 3.

Fluorescence counts were normalized to the incident beam flux at every energy step and collected using a 9-element solid-state Ge detector. The energy was calibrated by defining the first peak of the first derivative of Fe foil to be 7112 eV. Each spectrum was collected using four sets of energy acquisition conditions, giving good resolution over the pre-edge region and sufficient post-edge detail to allow high-quality normalization and background fitting. Each point was analyzed for 1000 or 2000 ms, giving total acquisition times of approximately 10–15 min. Calibration was performed on ten basalt glass standards loaned by the Smithsonian Institution (Cottrell et al. 2009), using the revised and updated Fe³⁺/ΣFe values of Zhang et al. (2018). Data processing is described in more detail in Stamper et al. (2014), but their original values have been updated in Table 3. Multiple (2 or 3) analyses were made of each glass; mean Fe³⁺/ΣFe and 2 standard deviations (s.d.) are reported in Table 3.

Secondary ion mass spectrometry (SIMS)

Dissolved volatiles (H₂O, CO₂) in seven high-pressure experimental glasses from Montserrat and St. Vincent 1, 2 and 3 series were measured by SIMS using a Cameca ims4f instrument at the NERC Edinburgh ion-microprobe facility (EIMF), UK. Samples were gold-coated for analysis. The primary beam was 10 keV O⁻ ions with net impact energy of 14.5 keV (4.5 kV secondary voltage). Beam current was 5 nA, focussed to a ~ 15 μm spot at the sample surface. Prior to analysis the sample surface was sputtered with a 25 × 25 μm raster for 3 min to eliminate surface contamination. Positive

secondary ions of ^1H and ^{12}C were collected with the 25 μm imaged field and 150 μm field aperture in two separate analytical routines with offset voltages of 75 (^1H) and 50 V (^{12}C). To avoid $^{24}\text{Mg}^{2+}$ interference $^{12}\text{C}^+$ secondary ions were collected at high mass resolution ($M/\Delta M = 1200$). $^1\text{H}^+$ secondary ions were collected at lower mass resolution ($M/\Delta M = 500$). A total of 15 analytical cycles was used, with count times of 5 s per cycle for ^1H and 12 s for ^{12}C . Only the final 5 cycles (^1H) or 7 cycles (^{12}C) were processed to remove any lingering effects of surface contamination. ^{30}Si was used as an internal standard, based on prior EPMA analyses. Calibration was performed on a suite of H_2O - and CO_2 -bearing synthetic and natural glass standards. Backgrounds, monitored on natural quartz grains co-mounted with the experimental glasses, were 2.8 ± 0.8 counts per second (cps) ^{12}C and 1600 ± 700 cps ^1H . Minimum detection limits, calculated as 3 s.d. on the blanks, were 140 ppm H_2O and 26 ppm CO_2 . At least three analyses were made of each glass except for St. Vincent series 2 run 7–3, where only one sufficiently large glass pool could be found.

H_2O and CO_2 contents of a further 32 Grenada, St. Kitts, Stromboli, Masaya and St. Vincent 1 series glasses analysed by SIMS using similar techniques can be found in the original sources. Pichavant et al. (2002) report H_2O , but not CO_2 , in five St. Vincent 2 and Martinique series glasses. Melikhova et al. (2015) report H_2O contents for 14 St. Vincent series 1 glasses. Uncertainties on H_2O and CO_2 (Table 2) are based on 1 s.d. of multiple analyses for new SIMS data, or are taken from original data sources.

In-house Mössbauer spectroscopy

Mössbauer spectroscopy measurements of two experimental glasses were made at Bayerisches Geoinstitut, Bayreuth, using a constant acceleration Mössbauer spectrometer in transmission mode with a nominal 370 MBq ^{57}Co point source in a 12 μm Rh matrix. Active dimensions of the point source were $500 \times 500 \mu\text{m}^2$. The velocity scale was calibrated relative to $\alpha\text{-Fe}$ and line widths of 0.36 mm s^{-1} were obtained for outer lines of $\alpha\text{-Fe}$ at room temperature. Experimental glasses were at room temperature during data collection. The glass samples were 200 μm thick and Mössbauer spectra were collected over a 500 μm diameter region in the middle of each sample. Data collection took 7–12 days.

Mössbauer spectra were fitted using MossA (Prescher et al. 2012) with a linear baseline to account for shadowing. We adopted the xVBFmodel (see Alberto et al. 1996; Lagarec and Rancourt 1997) for the fit, with the full transmission integral to account for thickness effects of the source and absorber (Rancourt 1989), and conventional constraints (doublet components with equal widths and areas). The Fe^{2+} doublet fit used the xVBFmodel with correlation. One extra

Fe^{2+} doublet was added to improve the fit of the Fe^{2+} absorption envelope; we used pseudo-Voigt line shape to minimize the number of extra parameters. The Fe^{3+} doublet fit used a pseudo-Voigt line shape to approximate the xVBFmodel with no correlation (see Partzsch et al. 2004; McCammon 2004). The $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratio was determined from relative areas. Spectra were fit with different models to assess dependence of $\text{Fe}^{3+}/\Sigma\text{Fe}$ on fitting model and error bars were estimated accordingly (± 0.03 in the ratio).

Synchrotron Mössbauer Source (SMS) spectroscopy

Energy-domain SMS measurements on 37 experimental glasses were conducted at the Nuclear Resonance Beamline ID18 (Rüffer and Chumakov 1996) at the European Synchrotron Radiation Facility (ESRF), Grenoble, France, operating in multibunch (7/8 + 1) mode. SMS is based on a nuclear resonant monochromator employing pure nuclear reflections of an iron borate ($^{57}\text{FeBO}_3$) single crystal (Potapkin et al. 2012). This source provides ^{57}Fe resonant radiation at 14.4 keV within a bandwidth of 6 neV which is tuneable in energy over a range of $\pm 0.6 \mu\text{eV}$ (Potapkin et al. 2012). Sample glasses were prepared as 150–350 μm -thick, doubly-polished wafers. After polishing, the transparent wafers were checked under a microscope to locate areas free of bubbles or crystals.

The X-ray beam was focused at the sample surface to an ellipse with principal axes $17 \times 18 \mu\text{m}$ at the full-width half-maximum (FWHM). Before and after each sample measurement, SMS linewidth was determined using a $\text{K}_2\text{Mg}^{57}\text{Fe}(\text{CN})_6$ reference single-line absorber. The velocity scale ($\pm 5 \text{ mm s}^{-1}$) was calibrated relative to a 25 μm -thick natural $\alpha\text{-Fe}$ foil. The small cross section, high brilliance and fully resonant and polarized nature of the beam allowed for rapid spectrum collection (approximately 2 h). Slightly longer run times (up to 6 h) were required for Fe-poor samples. Note that the glasses measured in this study contain only natural abundances of ^{57}Fe -atoms, i.e., $\sim 2\%$ of total Fe, thus the total radiation dosage, defined as photon delivered per μm^2 of the sample is 150, compared to 10^{12} for μXANES at Diamond.

Typical samples for SMS analysis are shown in Fig. 2; SMS spectra (and fits) for these samples are shown in Fig. 3. All SMS spectra consist of two broad symmetric doublets, typical of basaltic glasses. The spectra were fitted with a full transmission integral and Lorentzian line shape using the software package MossA (Prescher et al. 2012). The single line spectra were fitted with a normalized Lorentzian-squared source line shape. A linear function was applied to model the background. To obtain the maximum amount of photons we used the confocal Be-lenses installed at the ESRF beamline ID18. Be-lenses always bear traces of iron that result in the presence of two components

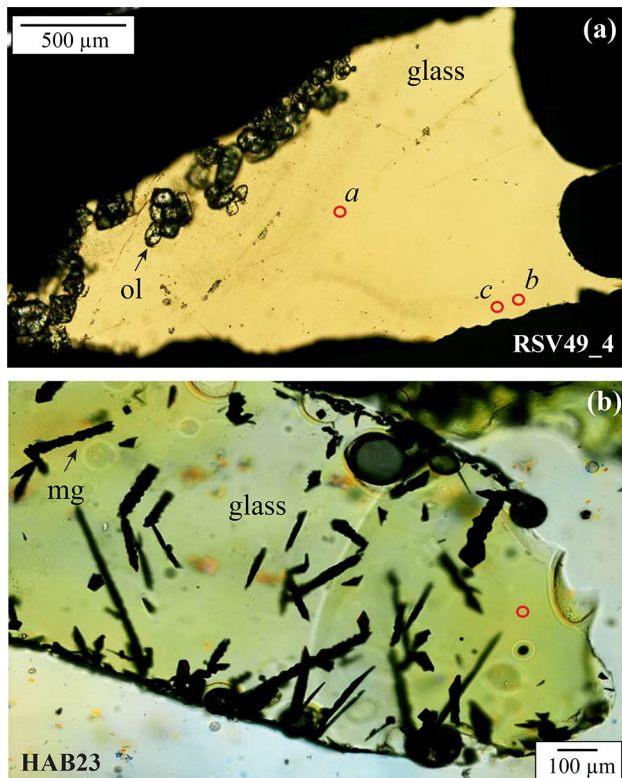


Fig. 2 Transmitted light photomicrographs of typical run products prepared for SMS analysis: **a** run RSV49_4; and **b** run HAB23. Doubly polished glass chips show clear glass pools suitable for SMS analysis. Crystalline phases are olivine in **a** and magnetite in **b**. The locations of the SMS analyses reported in Table 3 are shown as red circles

(Supplementary Fig. 1). The signal for iron in Be-lenses is easily corrected for and defined in all of the glass SMS spectra (Fig. 3).

The approach we adopt for the fitting uses only two distinct components represented by two doublets, one for Fe^{3+} and one for Fe^{2+} . Attempts using a model involving an additional Fe^{2+} component did not improve the quality of the fitting nor change the final $\text{Fe}^{3+}/\Sigma\text{Fe}$ results. Hyperfine parameters (centre shift, CS, and quadrupole splitting, QS) were first determined from the spectra where the two components were easily identified. For the other samples, the hyperfine parameters were allowed to vary within those ranges. $\text{Fe}^{3+}/\Sigma\text{Fe}$ values were obtained from the relative areas of the two components. The errors (2 s.d.) on the $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratios were obtained by normal error propagation.

Hyperfine parameters, $\text{Fe}^{3+}/\Sigma\text{Fe}$ values and related errors for all SMS analyses are reported in Supplementary Table 1. Centre shift varies in the range 1.00–1.12 mm s^{-1} for Fe^{2+} and 0.27–0.41 for Fe^{3+} . Quadrupole splitting varies in the range 1.89–2.60 for Fe^{2+} and 0.74–1.29 mm s^{-1} for Fe^{3+} . With one exception (run HAB23; Supplementary Table 1), absolute errors on $\text{Fe}^{3+}/\Sigma\text{Fe}$ range from 0.02 to 0.05. Highest errors are typically associated with samples having either

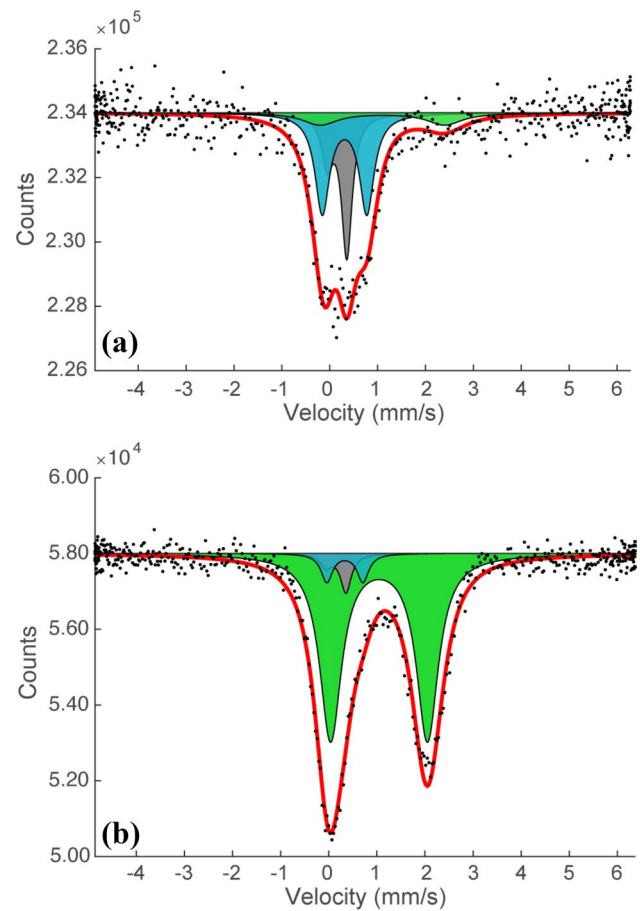


Fig. 3 Mössbauer spectra of experimental samples **a** HAB23 and **b** RSV49_4 (spot a) obtained using synchrotron Mössbauer source (SMS) spectroscopy at the beamline ID18, ESRF. Green and blue areas represent the fitted Fe^{2+} and Fe^{3+} components, respectively, while the grey area represents the contribution of Fe in Be-lenses (see text and Supplementary Material 1). Red curve represents the sum of all components (i.e., the modelled fit)

low or high $\text{Fe}^{3+}/\Sigma\text{Fe}$, for which the Fe^{3+} or Fe^{2+} component is less easily resolved.

Colorimetry

Four glasses of the Stromboli and Masaya series of Lesne et al. (2011) were analysed previously for $\text{Fe}^{3+}/\Sigma\text{Fe}$ using colorimetric wet-chemistry, following the method of Schuessler et al. (2008).

Results

Experimental run conditions and products are presented in Table 2, $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratios and exchange coefficient in Table 3, and analyses of glasses and olivines in Tables 4 and 5, respectively. On an anhydrous basis glasses are basalts

Table 4 Chemical compositions of experimental glasses

Run	SiO ₂	TiO ₂	Al ₂ O ₃	FeO [†]	MnO	MgO	CaO	Na ₂ O	K ₂ O	P ₂ O ₅	Cr ₂ O ₃	Total [‡]
S18.1.B4	49.33 (26)	0.82 (6)	17.69 (18)	6.96 (15)		5.55 (7)	10.45 (11)	1.91 (11)	1.39 (5)			97.84
S18.1.B5	49.23 (23)	0.81 (5)	17.89 (18)	7.00 (18)		5.67 (12)	10.57 (26)	1.89 (10)	1.36 (6)			97.56
S18.1.B7	50.02 (25)	0.82 (6)	17.99 (19)	7.05 (19)		5.86 (21)	10.70 (10)	1.90 (9)	1.37 (6)			97.92
MAS1B4	48.70 (20)	1.14 (5)	18.27 (13)	10.71 (17)		3.14 (9)	9.10 (8)	2.81 (12)	1.25 (6)			98.18
Run1#1	50.76 (17)	0.87 (2)	17.53 (17)	7.98 (20)	0.21 (1)	3.73 (5)	7.95 (17)	3.23 (13)	0.45 (3)	0.11 (4)		98.72
Run1#2	53.73 (21)	1.20 (3)	16.59 (25)	8.73 (21)	0.23 (1)	2.89 (11)	6.39 (15)	4.21 (20)	0.66 (4)	0.24 (4)		98.75
RSV49_4	47.55 (31)	0.80 (3)	15.21 (22)	7.84 (21)	0.21 (5)	12.40 (2)	11.51 (16)	1.85 (10)	0.15 (16)			98.12
BM40	46.88 (4)	0.89 (2)	17.01 (13)	8.72 (17)	0.15 (3)	8.30 (12)	11.33 (9)	2.37 (16)	0.17 (2)	0.11 (3)	0.02 (1)	99.00
BM6	46.88 (29)	0.86 (4)	16.13 (22)	6.63 (16)	0.16 (2)	9.41 (15)	10.96 (9)	2.15 (11)	0.15 (1)	0.12 (3)	0.06 (4)	98.58
BM33	45.37 (27)	0.70 (4)	13.88 (19)	7.30 (26)	0.34 (9)	13.63 (21)	10.30 (13)	2.23 (13)	0.14 (1)	0.08 (3)	0.13 (1)	98.56
BM37	45.93 (13)	0.82 (2)	15.85 (32)	7.58 (2)	0.15 (3)	8.35 (13)	11.73 (23)	2.67 (13)	0.16 (2)	0.09 (2)	0.01	98.54
BM34	51.23 (5)	0.42 (3)	17.64 (35)	4.65 (27)	0.17 (4)	4.83 (12)	7.81 (11)	2.92 (13)	0.26 (2)	0.17 (4)		97.30
BM46	45.26 (28)	0.68 (2)	13.69 (18)	7.36 (14)	0.15 (2)	13.69 (17)	10.27 (11)	2.23 (12)	0.14 (1)	0.08 (2)	0.13 (1)	98.20
RSV49_2	46.78 (42)	0.71 (2)	14.28 (20)	8.88 (27)	0.18 (6)	14.15 (16)	10.78 (9)	1.79 (9)	0.12 (2)	0.09 (3)	0.11 (2)	98.47
BM38	46.44 (3)	0.79 (2)	14.99 (27)	8.49 (18)	0.17 (4)	11.34 (5)	11.29 (15)	2.15 (13)	0.15 (3)	0.08 (2)	0.05 (6)	98.44
BM3	47.53 (39)	0.81 (3)	16.02 (34)	7.72 (15)	0.16 (3)	9.16 (7)	11.64 (35)	2.11 (2)	0.16 (2)	0.10 (2)	0.07 (1)	98.42
BM9	45.27 (24)	0.79 (4)	15.98 (2)	7.90 (17)	0.14 (2)	8.57 (3)	11.03 (12)	2.49 (17)	0.16 (2)	0.09 (3)	0.04 (1)	98.61
BM17	45.58 (51)	0.75 (4)	14.61 (18)	8.58 (26)	0.2 (7)	10.91 (8)	10.99 (69)	2.28 (18)	0.17 (1)	0.13 (2)	0.03 (1)	101.62
XANES9	45.96 (16)	0.73 (1)	14.07 (11)	8.44 (3)	0.160 (0)	13.33 (9)	10.54 (3)	1.73 (10)	0.13 (0)	0.08 (4)	0.07 (2)	98.65
XANES2	50.32 (91)	0.82 (1)	15.82 (13)	1.06 (3)	0.092 (5)	13.09 (17)	11.50 (8)	2.09 (11)	0.15 (1)	0.08 (4)	0.09 (2)	101.06
XANES11	48.55 (74)	0.78 (1)	14.71 (11)	3.48 (4)	0.140 (5)	13.35 (17)	11.11 (10)	1.93 (5)	0.15 (1)	0.10 (2)	0.08 (2)	99.97
6-4	49.63 (50)	0.79 (8)	16.23 (20)	7.74 (4)	0.18 (18)	7.28 (8)	10.25 (12)	2.37 (30)	0.37 (8)		0.04	99.32
7-2	45.21 (20)	1.03 (7)	14.76 (20)	8.25 (18)	0.11 (6)	10.02 (30)	10.86 (20)	2.13 (10)	0.48 (4)		0.02	97.56
7-3	47.09 (30)	1.19 (6)	16.14 (20)	8.18 (29)	0.17 (8)	8.49 (19)	11.82 (10)	2.37 (12)	0.58 (4)		0.02	98.46
3-1	45.73 (70)	1.10 (7)	16.14 (20)	7.62 (17)	0.20 (8)	6.91 (18)	11.80 (20)	2.19 (11)	0.53 (2)		0.05	98.15
HAB-18	49.78 (60)	0.82 (13)	17.33 (40)	7.69 (31)	0.12 (11)	4.19 (10)	8.77 (11)	3.24 (31)	0.77 (4)			98.12
HAB-20	50.73 (60)	0.40 (6)	18.07 (20)	2.75 (14)	0.21 (7)	3.88 (6)	8.78 (9)	3.34 (6)	0.81 (5)			97.26
HAB-23	50.69 (70)	0.52 (7)	18.04 (10)	3.51 (24)	0.20 (9)	3.87 (6)	9.11 (20)	3.50 (8)	0.78 (5)			98.53
HAB-26/P1D	58.50 (80)	0.23 (7)	16.14 (10)	2.63 (12)	0.15 (10)	2.08 (3)	6.07 (14)	3.85 (6)	1.01 (7)			98.56
MV02	46.89 (36)	0.81 (1)	20.83 (9)	8.15 (49)	0.17 (3)	4.49 (68)	11.10 (81)	2.41 (8)	0.57 (2)	0.09 (3)	bd	102.20
MV01	45.41 (20)	0.80 (3)	18.94 (17)	8.30 (27)	0.17 (3)	4.72 (13)	10.64 (9)	2.27 (9)	0.48 (19)	0.08 (2)		99.40
W1	43.74 (18)	1.02 (3)	14.20 (11)	8.82 (13)	0.17 (1)	9.06 (9)	13.13 (14)	2.35 (12)	0.65 (3)	0.28 (6)		98.82
W3	43.43 (15)	0.9 (3)	12.28 (8)	9.10 (13)	0.2 (2)	13.00 (18)	12.70 (8)	2.08 (13)	0.55 (2)	0.22 (5)		98.10
AN-2	45.38 (33)	0.92 (3)	12.55 (5)	8.93 (7)	0.2 (1)	15.07 (10)	12.72 (15)	2.13 (10)	0.57 (3)	0.24 (3)	0.14 (1)	99.22
R-5	44.72 (23)	0.95 (3)	12.35 (14)	9.34 (12)	0.19 (1)	12.15 (10)	13.19 (15)	2.14 (15)	0.51 (2)	0.24 (3)		98.63
33	43.28 (21)	0.89 (3)	12.22 (16)	8.69 (9)	0.17 (2)	13.81 (18)	12.15 (7)	1.93 (11)	0.53 (3)	0.21 (6)	0.12 (1)	97.65
AN3	45.26 (44)	0.96 (3)	12.41 (9)	9.51 (16)	0.18 (2)	13.82 (28)	12.85 (10)	2.18 (10)	0.58 (3)	0.24 (5)		98.41
30	43.53 (90)	0.92 (4)	12.89 (8)	9.01 (13)	0.17 (2)	12.55 (17)	12.33 (12)	2.07 (15)	0.55 (3)	0.25 (4)		98.16

Table 4 (continued)

Run	SiO ₂	TiO ₂	Al ₂ O ₃	FeO ^a	MnO	MgO	CaO	Na ₂ O	K ₂ O	P ₂ O ₅	Cr ₂ O ₃	Total ^b
D-11	48.31 (68)	1.00 (3)	13.47 (40)	8.83 (21)	0.12 (2)	10.29 (24)	13.87 (14)	2.08 (6)	0.33 (2)	0.25 (4)	0.07 (2)	98.62
D-10	47.35 (37)	0.96 (2)	13.31 (17)	8.80 (17)	0.15 (2)	11.66 (10)	13.51 (11)	1.91 (11)	0.31 (2)	0.21 (2)	0.08 (1)	98.25
D-13	47.47 (21)	0.94 (3)	12.95 (8)	9.56 (17)	0.14 (2)	13.18 (12)	13.40 (6)	0.06 (3)	0.01 (2)	0.18 (5)	0.14 (1)	98.03
D-8	48.82 (36)	0.97 (3)	13.44 (8)	6.78 (9)	0.13 (2)	12.73 (10)	13.89 (7)	0.94 (7)	0.30 (2)	0.16 (4)	0.13 (1)	98.29
D-12	47.85 (36)	0.95 (2)	13.00 (12)	8.79 (10)	0.12 (2)	12.42 (13)	13.20 (9)	1.98 (13)	0.32 (2)	0.24 (6)	0.10 (1)	98.97
DR-1	46.25 (20)	0.92 (0)	13.25 (10)	8.93 (14)	0.24 (2)	12.45 (20)	13.25 (16)	2.31 (14)	0.61 (2)	0.27 (2)	0.09 (1)	98.57
D-7	45.78 (16)	0.94 (4)	12.64 (8)	9.47 (15)	0.18 (2)	13.55 (20)	13.11 (8)	2.20 (9)	0.57 (2)	0.22 (5)	0.05 (1)	98.71
35	44.53 (42)	0.90 (3)	12.54 (15)	8.73 (11)	0.18 (2)	13.19 (57)	12.23 (13)	1.94 (19)	0.54 (25)	0.21 (5)	0.04 (1)	97.04
41	44.11 (8)	0.97 (3)	13.74 (12)	8.82 (7)	0.20 (2)	10.30 (13)	13.40 (12)	2.11 (14)	0.58 (2)	0.27 (5)	0.02 (1)	98.36
23	43.78 (35)	0.91 (3)	12.62 (22)	8.86 (10)	0.17 (2)	12.32 (22)	12.30 (15)	1.87 (11)	0.53 (3)	0.23 (4)	0.08 (2)	97.12
25	44.33 (42)	0.93 (3)	12.66 (28)	9.00 (13)	0.18 (2)	12.66 (35)	12.36 (12)	1.84 (12)	0.52 (2)	0.20 (2)	0.07 (2)	98.38
36	42.35 (31)	0.87 (2)	11.85 (22)	8.80 (16)	0.17 (2)	13.98 (18)	11.70 (31)	1.43 (15)	0.60 (9)	0.24 (5)	0.15 (3)	96.94
AN-1	45.31 (53)	0.94 (5)	12.94 (21)	9.57 (13)	0.19 (2)	13.08 (33)	13.22 (9)	2.24 (14)	0.57 (3)	0.24 (4)	0.06 (2)	98.74
R-2	44.3 (29)	1.08 (5)	13.72 (22)	9.58 (12)	0.20 (2)	10.00 (35)	12.51 (5)	2.30 (14)	0.60 (3)	0.27 (3)	0.04 (1)	98.35
22	44.05 (31)	1.00 (4)	13.78 (21)	9.02 (9)	0.21 (1)	10.39 (29)	12.07 (14)	2.25 (12)	0.61 (3)	0.25 (3)	0.03 (2)	96.69
R-1	45.11 (24)	0.95 (3)	12.62 (17)	8.91 (10)	0.2 (2)	12.35 (10)	13.11 (7)	1.89 (18)	0.51 (3)	0.22 (5)	0.12 (1)	99.15
28	44.05 (29)	0.91 (4)	12.66 (18)	8.91 (6)	0.18 (2)	12.81 (12)	12.42 (12)	2.00 (11)	0.52 (2)	0.21 (5)	0.06 (1)	98.02
R-6	44.43 (22)	0.92 (5)	11.65 (17)	9.17 (10)	0.20 (1)	13.83 (11)	12.55 (10)	1.95 (12)	0.49 (3)	0.24 (4)	0.14 (2)	98.78
12	44.01 (40)	1.15 (3)	15.19 (18)	8.85 (25)	0.20 (2)	9.60 (19)	10.53 (22)	2.71 (7)	0.79 (4)	0.28 (5)		97.60
10	43.3 (70)	1.02 (9)	14.00 (78)	8.71 (40)	0.18 (1)	10.53 (40)	11.99 (9)	2.05 (28)	0.56 (8)	0.27 (6)	0.07 (3)	97.28
15	43.61 (43)	0.97 (4)	13.61 (18)	9.14 (16)	0.19 (1)	10.90 (54)	12.36 (22)	2.18 (20)	0.57 (4)	0.22 (5)	0.08 (2)	97.71
32	43.12 (28)	0.99 (5)	13.38 (17)	9.44 (10)	0.19 (2)	12.44 (21)	11.21 (12)	2.22 (17)	0.60 (3)	0.22 (7)	0.04 (1)	97.64
38	43.6 (17)	0.87 (4)	12.14 (13)	8.97 (15)	0.18 (3)	14.41 (14)	11.98 (10)	2.00 (10)	0.52 (4)	0.22 (5)	0.14 (2)	98.18
PU1	47.64 (32)	0.819 (3)	13.97 (12)	9.51 (2)	0.186 (4)	14.01 (7)	11.29 (3)	1.08 (9)	0.41 (1)	0.06 (3)	0.16 (1)	99.14
PU2	47.26 (20)	0.763 (5)	12.57 (23)	9.49 (4)	0.188 (4)	17.04 (10)	10.344 (3)	0.85 (5)	0.32 (1)	0.05 (4)	0.16 (1)	99.03
PU4	48.46 (32)	0.858 (6)	14.80 (18)	8.81 (11)	0.182 (6)	11.97 (5)	11.88 (4)	0.97 (10)	0.36 (2)	0.07 (6)	0.13 (1)	98.50
PU5	49.19 (49)	0.922 (12)	15.77 (34)	8.71 (4)	0.178 (7)	9.96 (18)	12.71 (2)	1.33 (10)	0.47 (2)	0.10 (4)	0.09 (2)	99.41
PU364	46.45 (34)	0.859 (6)	14.16 (11)	9.98 (7)	0.186 (5)	11.81 (18)	11.87 (7)	1.34 (7)	0.46 (3)	0.07 (4)	0.08 (1)	97.28
PU363	47.43 (38)	0.905 (7)	15.06 (4)	9.47 (4)	0.184 (1)	10.19 (4)	12.45 (3)	1.37 (7)	0.47 (1)	0.10 (3)	0.04 (2)	97.67
PU351	48.28 (14)	0.845 (8)	14.02 (13)	9.50 (4)	0.184 (2)	11.49 (8)	11.85 (5)	1.33 (10)	0.46 (2)	0.11 (5)	bd	98.06
PU56	47.15 (29)	0.799 (9)	13.51 (7)	10.34 (5)	0.183 (4)	13.64 (13)	11.11 (4)	1.34 (6)	0.45 (1)	0.08 (3)		98.62
PU359	47.01 (11)	0.808 (16)	13.80 (9)	9.91 (11)	0.185 (2)	13.73 (20)	11.18 (5)	1.35 (3)	0.45 (0)	0.08 (1)	0.08 (1)	98.58
PU58	46.66 (22)	0.778 (2)	13.04 (8)	10.26 (7)	0.184 (4)	14.74 (5)	10.77 (2)	1.25 (13)	0.42 (1)	0.07 (2)	bd	98.17
PU361	46.71 (16)	0.751 (7)	12.48 (7)	10.01 (6)	0.182 (3)	16.21 (12)	10.31 (4)	1.19 (18)	0.38 (2)	0.12 (3)	bd	98.34

All concentrations given at wt%. Standard deviation (in parentheses) based on multiple analyses and expressed in terms of least significant digits

Blank denotes not analysed; bd is below detection

All Fe expressed as FeO

^aTotal includes H₂O and CO₂ content of glasses as reported in Table 2

($n = 61$) and basaltic andesites ($n = 10$) and a single dacite (HAB-26). H_2O and CO_2 range from zero (nominally) up to 8.3 and 1.2 wt%, respectively. Glass MgO contents range from 2 to 17 wt%; olivines are Fo_{86} to Fo_{98} with 0.09–0.59 wt% MnO (one at Fo_{65} and 0.56 wt% MnO) and 0.02–0.94 wt% CaO . Total alkalis ($\text{Na}_2\text{O} + \text{K}_2\text{O}$) in the glasses range from 0.1 to 4.9 wt%.

Ferric–ferrous ratios

$\text{Fe}^{3+}/\Sigma\text{Fe}$ ratios range from 0.06 to 0.84 (μXANES) and 0.04 to 0.80 (SMS). Typical uncertainties (2 s.d.) in $\text{Fe}^{3+}/\Sigma\text{Fe}$, propagated through the various sources of analytical error, are in the range 0.001–0.32 (mean = 0.016) for μXANES ; 0.02–0.07 (mean = 0.029) for SMS; and ~ 0.03 for in-house Mössbauer and colorimetry. To test the homogeneity of individual glasses we used SMS to analyze three separate chips of water-poor glass RSV49_4 from the centre (RSV49_4a, b) and from the edge (RSV49_4c) of the experimental charge. All three measurements lie within 2 s.d. of each other (Table 3). Similarly, two SMS analyses of hydrous glass BM46 from the centre (BM46a) and periphery (BM46b) of the same glass chip give values of $\text{Fe}^{3+}/\Sigma\text{Fe}$ that agree within 2 s.d. (BM46c analysis is described below).

Two experimental glasses (XANES9, 6-4) analysed by SMS and in-house Mössbauer displayed consistency to within 2 s.d. (Table 3). SMS and colorimetry agree within 2 s.d. for three of the four glasses analysed by both techniques; the fourth (MAS1_B4) has a significantly higher $\text{Fe}^{3+}/\Sigma\text{Fe}$ by SMS (0.289) than by colorimetry (0.18). The cause of this discrepancy is unclear. However, it is noteworthy that the $\text{Fe}^{3+}/\Sigma\text{Fe}$ from colorimetry is significantly lower than other three values from glasses synthesised under similar conditions in the study of Lesne et al. (2011), i.e., 0.32–0.37, suggesting a potential problem with colorimetric analysis of MAS1_B4. For the 27 glasses analysed by both μXANES and SMS, the former method gives significantly higher $\text{Fe}^{3+}/\Sigma\text{Fe}$ for all but ten (Table 3). This discrepancy is well outside the analytical uncertainty and is suggestive of oxidation by the X-ray beam during μXANES analysis (Cottrell et al. 2018). The problem of oxidation is found to be most acute in hydrous glasses (> 0.5 wt% H_2O) containing a significant proportion of the oxidizable species, Fe^{2+} . This is evident from a plot of the difference between $\text{Fe}^{3+}/\Sigma\text{Fe}$ by SMS and $\text{Fe}^{3+}/\Sigma\text{Fe}$ by μXANES against the $\text{Fe}^{3+}/\Sigma\text{Fe}$ (by SMS) in glass (Fig. 4). For anhydrous glasses (< 0.5 wt% H_2O) the two methods agree across a broad range of $\text{Fe}^{3+}/\Sigma\text{Fe}$; for hydrous glasses the scale of the mismatch increases roughly linearly with decreasing $\text{Fe}^{3+}/\Sigma\text{Fe}$ (i.e., increasing $\text{Fe}^{2+}/\Sigma\text{Fe}$). This is consistent with the findings of Cottrell et al. (2018), albeit here based on a much wider range of glass compositions and $\text{Fe}^{3+}/\Sigma\text{Fe}$. Cottrell et al. (2018)

conclude that oxidation is most acute when photon flux densities are as high as those used in our analyses; they recommend using flux densities some two orders of magnitude lower to minimise the oxidative effects of the beam.

To explore further the influence of photon dosage on in situ oxidation during μXANES analysis, we ran a series of continuous time-scans at Diamond at energies corresponding to the peaks of the Fe^{2+} and Fe^{3+} regions of the pre-edge, without attenuating Al foils in front of the beam. This enables a semi-quantitative, real-time assessment of maximum beam damage. We analysed synthetic hydrous glasses MAS1_B4 and MAS1_B5 from Lesne et al. (2011) with 3.0 and 2.6 wt% H_2O , respectively, alongside anhydrous glass standard LW_10 from Cottrell et al. (2009). Both hydrous glasses have ~ 10.7 wt% FeO^{T} ; LW has 10.2 wt% FeO^{T} (Cottrell et al. 2009). All samples are moderately oxidised with $\text{Fe}^{3+}/\Sigma\text{Fe}$ of 0.18 (MAS1_B4) and 0.32 (MAS1_B5), as determined by colorimetry (Lesne et al. 2011), 0.289 (MAS1_B4) by SMS (Table 3), and 0.235 (LW_10) by in-house Mössbauer (Cottrell et al. 2009). The sample shutter was kept closed until the beginning of counting, and counts were collected every 5 s for 500 s, which is approximately the same length of time taken to reach the pre-edge region in our quantitative μXANES analyses. For LW_10, Fe^{3+} count rates (normalised to I_0) showed only a minimal increase during the analysis, whereas MAS1_B4 and MAS1_B5 showed relatively small increases in apparent $\text{Fe}^{3+}/\Sigma\text{Fe}$ (calculated from peak height alone, not from a full area-weighted centroid fit) of ~ 0.02 and 0.05, respectively (Supplementary Fig. 2).

This experiment confirms that beam damage during μXANES is occurring in our samples, and that the extent of damage increases with higher H_2O concentrations and lower initial redox state, as described in Cottrell et al. (2018). However, regardless of H_2O concentration, the measured deviations are very weak in oxidised glasses with $\text{Fe}^{3+}/\Sigma\text{Fe} \geq 0.5$ and strongest in reduced glasses with $\text{Fe}^{3+}/\Sigma\text{Fe} \leq 0.5$ (Fig. 4). In unpublished μXANES data from more evolved (rhyolitic) compositions we have also observed greater beam damage in reduced, H_2O -poor glasses than in oxidised, H_2O -rich equivalents. We suggest, therefore, that the dominant factor controlling beam-damage susceptibility is the initial redox state of the glass. However, as anhydrous glasses experience little or no damage, the presence of H_2O is clearly important (Cottrell et al. 2018). During electron beam damage of hydrous glasses, H_2O appears to facilitate damage by enhancing the diffusion of alkalis and OH towards or away from the centre of electron deposition (Humphreys et al. 2006). We speculate, following Cooper et al. (1996), that a similar effect may occur during X-ray irradiation, with Fe oxidation generated as a result of alkali migration towards the site of maximum X-ray flux. Such mechanisms could be tested in future by detailed mapping

Table 5 Chemical compositions of experimental olivines

Run	SiO ₂	TiO ₂	Al ₂ O ₃	FeO	MnO	MgO	CaO	Cr ₂ O ₃	NiO	Total	%Fo ^a	%Fa ^a	%Te ^a
Run1-2	36.55 (31)	0.00	0.06 (2)	29.96 (57)	0.59 (9)	31.28 (28)	0.22 (4)			98.66	64.6	34.7	0.7
RSV49_4	41.14 (48)		0.12 (2)	9.22 (26)	0.17 (3)	50.53 (41)	0.28 (2)	0.08 (1)	0.22 (8)	101.80	90.6	9.3	0.2
BM40	39.80 (37)		0.17 (1)	10.04 (15)	0.18 (2)	48.82 (28)	0.33 (1)		0.3 (2)	99.68	89.5	10.3	0.2
BM6	40.67 (44)		0.06 (2)	11.00 (7)	0.13 (3)	48.45 (47)	0.23 (2)		0.21 (2)	100.82	88.6	11.3	0.1
BM37	40.82 (4)		0.12 (17)	5.82 (24)	0.16 (2)	52.76 (56)	0.27 (1)	0.01	0.36 (3)	100.34	94.0	5.8	0.2
BM34	41.05 (44)		0.07 (3)	6.09 (23)	0.2 (2)	52.33 (47)	0.23 (6)		0.41 (4)	100.38	93.7	6.1	0.2
BM38	40.69 (4)		0.17 (1)	7.31 (16)	0.15 (2)	50.86 (4)	0.33 (11)		0.38 (2)	99.97	92.4	7.5	0.2
BM3	41.07 (50)		0.46 (45)	10.54 (13)	0.18 (2)	46.97 (70)	0.49 (23)	0.07 (3)	0.82 (19)	100.63	88.6	11.2	0.2
BM9	40.57 (4)		0.06 (5)	10.97 (18)	0.17 (2)	47.63 (2)	0.24 (4)	0.03 (1)	0.19 (3)	99.88	88.4	11.4	0.2
BM17	41.48 (24)		0.27 (19)	6.84 (35)	0.16 (2)	51.22 (5)	0.20 (7)		0.43 (1)	100.60	92.9	7.0	0.2
XANES2	41.63 (34)	0.02 (1)	0.28 (37)	1.72 (24)	0.09	55.49 (61)	0.26 (10)	0.07 (2)		99.56	98.2	1.7	0.1
XANES11	40.67 (24)	0.02	0.05 (4)	4.83 (29)	0.13	51.13 (26)	0.28 (1)	0.06 (2)	0.04 (2)	97.21	94.8	5.0	0.1
7-2	42.00 (10)	0.00	0.17 (20)	8.97 (30)	0.14 (11)	48.30 (10)	0.28 (3)			99.87	90.4	9.4	0.1
7-3	41.70 (10)	0.03	0.08 (20)	11.60 (30)	0.14 (11)	46.90 (10)	0.25 (3)	0.17 (1)		100.87	87.7	12.2	0.1
3-1	39.80 (50)		0.12 (13)	12.80 (30)	0.17 (8)	46.00 (50)	0.30 (3)			99.32	86.3	13.5	0.2
W1	40.85 (17)		0.14 (27)	9.92 (19)	0.21 (1)	48.39 (96)	0.45 (43)		0.24 (2)	100.20	89.5	10.3	0.2
W3	41.49 (40)		0.11 (5)	4.21 (10)	0.17 (1)	53.35 (28)	0.31 (3)		0.60 (3)	100.24	95.6	4.2	0.2
R-5	41.80 (48)	0.02 (1)	0.34 (23)	5.81 (31)	0.18	51.39 (33)	0.42 (12)		0.50 (1)	100.46	93.9	6.0	0.2
AN3	41.71 (14)		0.15 (3)	3.73 (5)	0.15 (1)	53.55 (35)	0.02 (1)		0.30 (1)	99.61	96.1	3.8	0.2
30	41.89 (34)		0.35 (84)	4.34 (15)	0.16 (1)	52.20 (1.9)			0.36 (3)	99.82	95.4	4.4	0.2
D-11	39.80 (11)		0.51 (66)	9.61 (16)	0.13	47.89 (1.1)	0.80 (45)	0.14 (1)	0.17 (2)	99.10	89.8	10.1	0.1
D-10	41.62 (14)	0.25 (1)	0.13 (2)	8.40 (15)	0.13 (1)	48.17 (31)	0.65 (1)	0.01		99.37	91.0	8.9	0.1
D-13	40.12 (14)		0.07 (2)	10.58 (15)	0.10 (1)	48.35 (31)	0.33 (1)	0.11	0.13 (1)	99.80	89.0	10.9	0.1
D-8	40.89 (68)	0.01	0.07 (2)	7.75 (10)	0.13 (1)	50.63 (88)	0.41 (1)	0.11 (2)	0.07 (2)	100.07	92.0	7.9	0.1
D-12	40.73 (24)	0.06 (4)	0.27 (25)	7.92 (10)	0.11 (1)	50.53 (47)	0.61 (12)		0.10 (1)	100.46	91.8	8.1	0.1
DR-1	41.28 (37)		0.32 (34)	7.51 (31)	0.23	49.76 (66)	0.65 (18)	0.07 (1)	0.17 (3)	100.01	92.0	7.8	0.2
D-7	42.27 (11)	0.02 (1)	0.16 (6)	2.55 (13)	0.16 (1)	54.60 (15)	0.47 (4)	0.06 (3)	0.30 (2)	100.59	97.3	2.5	0.2
35	42.73 (31)		0.19 (32)	2.00 (17)	0.15	54.10 (99)		0.03 (1)	0.58 (3)	100.30	97.8	2.0	0.2
41	41.66 (35)		0.48 (91)	5.58 (25)	0.19 (1)	50.89 (1.8)		0.02 (1)	0.28 (2)	99.72	94.0	5.8	0.2
23	40.80 (17)		0.09 (4)	5.36 (28)	0.16 (1)	51.58 (43)	0.30 (3)	0.05 (1)	0.37 (2)	98.72	94.3	5.5	0.2
25	41.17 (19)		0.07 (2)	4.56 (20)	0.16 (1)	53.16 (35)	0.30 (2)	0.04 (1)	0.38 (2)	99.85	95.3	4.6	0.2
AN-1	42.24 (60)		0.13 (2)	3.46 (6)	0.17 (1)	53.38 (55)	0.41 (3)	0.04 (1)	0.33 (3)	100.17	96.3	3.5	0.2
R-2	40.73 (15)		0.08 (5)	8.70 (6)	0.21 (5)	49.74 (17)	0.37 (5)	0.03 (1)	0.36 (1)	100.23	90.9	8.9	0.2
22	40.72 (30)		0.09 (5)	4.87 (20)	0.19 (1)	52.47 (42)	0.27 (2)		0.40 (2)	99.04	94.9	4.9	0.2
R-1	41.51 (14)		0.06 (2)	7.93 (4)	0.18 (1)	49.56 (9)	0.38 (2)	0.07	0.28 (2)	99.98	91.6	8.2	0.2
28	42.31 (32)		0.06 (1)	4.37 (14)	0.16 (1)	52.61 (21)	0.27 (3)	0.03 (1)	0.38 (2)	100.19	95.4	4.4	0.2
R-6	41.93 (22)		0.22 (26)	6.25 (8)	0.17 (1)	50.95 (73)	0.40 (15)	0.06 (1)	0.4 (2)	100.40	93.4	6.4	0.2

Table 5 (continued)

Run	SiO ₂	TiO ₂	Al ₂ O ₃	FeO	MnO	MgO	CaO	Cr ₂ O ₃	NiO	Total	%Fo ^a	%Fa ^a	%Te ^a
12	41.33 (67)		0.18 (13)	7.67 (24)	0.21 (1)	49.69 (50)	0.31 (14)	0.00	0.36 (2)	99.76	91.8	8.0	0.2
10	40.79 (41)		0.10 (4)	9.09 (10)	0.19	49.47 (38)	0.24 (2)	0.03 (1)	0.26 (2)	100.18	90.5	9.3	0.2
15	41.00 (41)		0.13 (9)	8.17 (15)	0.19 (1)	49.99 (77)	0.51 (73)	0.04 (1)	0.29 (2)	100.33	91.4	8.4	0.2
32	41.39 (25)		0.10 (4)	5.08 (6)	0.17 (1)	53.04 (37)	0.33 (18)	0.02 (1)	0.36 (2)	100.50	94.7	5.1	0.2
PU1	40.08 (34)		0.16 (15)	10.30 (11)	0.16 (1)	48.20 (20)	0.37 (1)		0.17 (2)	99.64	89.1	10.7	0.2
PU4	40.23 (38)		0.09 (1)	8.70 (3)	0.14	49.49 (44)	0.33 (1)	0.13 (3)	0.065 (2)	99.19	90.9	9.0	0.1
PU2	40.20 (57)		0.22 (27)	10.92 (5)	0.18 (1)	47.60 (26)	0.45 (13)	0.11 (1)	0.11 (1)	99.82	88.4	11.4	0.2
PU5	39.59 (23)		0.21 (11)	12.30 (7)	0.20	46.34 (42)	0.46 (1)	0.16 (10)	0.14 (1)	99.43	86.9	12.9	0.2
PU364	39.41 (44)		0.27 (15)	9.68 (13)	0.17 (1)	47.36 (29)	0.42 (1)		0.22	97.74	89.5	10.3	0.2
PU363	39.51 (13)		0.11 (6)	10.56 (7)	0.19	47.54 (90)	0.41 (1)		0.19	98.58	88.7	11.1	0.2
PU351	42.64 (38)		1.05 (83)	2.39 (11)	0.16 (1)	52.48 (1.2)	0.72 (45)	0.00	0.20 (1)	99.68	97.3	2.5	0.2
PU56	41.72 (28)	0.37 (11)	0.15 (6)	2.52 (6)	0.15 (1)	54.42 (48)	0.02 (1)		0.26 (1)	99.61	97.3	2.5	0.2
PU359	40.38 (1.3)	0.02	0.21 (1.1)	8.46 (6)	0.16	49.43 (1.9)	0.40 (63)	0.11 (5)	0.23 (1)	99.40	91.1	8.7	0.2
PU58	41.62 (19)	0.01	0.13 (3)	2.47 (5)	0.14	54.17 (18)	0.28 (1)	0.00	0.28	99.10	97.4	2.5	0.1
PU361	42.03 (9)	0.06 (3)	0.78 (25)	2.81 (20)	0.13	51.70 (70)	0.94 (32)		0.29 (1)	98.75	96.9	3.0	0.1

All concentrations given as wt%. Standard deviation (in parentheses) based on multiple analyses and expressed in terms of least significant digits

^aMolar percentage of forsterite (Fo), fayalite (Fa) and tephroite (Te)

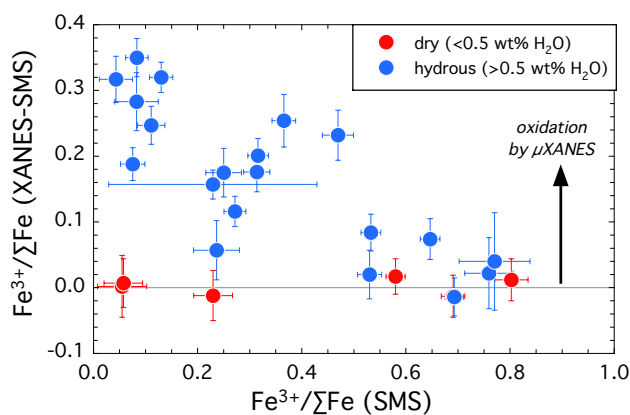


Fig. 4 Comparison of μ XANES and SMS methods used to measure $\text{Fe}^{3+}/\Sigma\text{Fe}$ in our experimental glasses. The difference between XANES and SMS measurements of $\text{Fe}^{3+}/\Sigma\text{Fe}$ is plotted versus that measured by SMS. μ XANES tends to overestimate $\text{Fe}^{3+}/\Sigma\text{Fe}$ due to beam damage at the high photon fluxes used. As the amount of oxidisable Fe^{2+} in the glass increases, so the tendency to oxidise during μ XANES increases for all but the most dry (<0.5 wt% H_2O) glasses. Only for very oxidised ($\text{Fe}^{3+}/\Sigma\text{Fe} > 0.5$) or dry glasses do μ XANES and SMS agree within experimental uncertainty. Data are taken from Table 3; error bars are 2 sd

of cation distribution in the regions surrounding irradiated sites (Cottrell et al. 2018).

To directly simulate possible beam damage caused by μ XANES analysis at the high photon flux densities used at Diamond we analysed by SMS a glass chip from experiment BM46 previously exposed to comparable beam dosage to μ XANES. A spot on the sample (BM46c in Table 3) was first irradiated for 10 min with a beam flux of 10^{14} photon s^{-1} , corresponding to a total photon dosage of 8×10^{11} . A dark spot appeared at the glass surface after irradiation. This spot was then analysed by SMS, using the same low photon flux as previously. The analysis revealed significantly higher $\text{Fe}^{3+}/\Sigma\text{Fe}$ (0.196 ± 0.017) compared to un-irradiated spots (BM46a,b) on the same chip (0.130 ± 0.023 and 0.104 ± 0.020), confirming that high photon-flux irradiation of hydrous glass, such as that during μ XANES at Diamond, causes appreciable oxidation. The extent of the oxidation is, however, somewhat less than we observed for the typical mismatch between SMS and μ XANES (Fig. 4), probably due to the smaller spot size of μ XANES (i.e., greater flux density) compared to the SMS simulation. The mechanism of oxidation is not clear, but may involve the formation of tiny magnetite nanolites (Di Genova et al. 2017; Hughes et al. 2018), as suggested by Raman spectra of some μ XANES spots and the darkening of the glass after irradiation. This mechanism may operate in tandem with the alkali migration proposed above.

In light of the likely oxidation of some hydrous glasses during μ XANES analysis, we favour SMS data over μ XANES data for all hydrous glasses. For glasses

with <0.5 wt% H_2O , but lacking SMS analyses, we have adopted the μ XANES $\text{Fe}^{3+}/\Sigma\text{Fe}$ values. Our ‘preferred’ $\text{Fe}^{3+}/\Sigma\text{Fe}$ values for each experiment are given in Table 3; these are the $\text{Fe}^{3+}/\Sigma\text{Fe}$ values used in all subsequent calculations and plots. Note that some hydrous glasses without SMS analysis have no preferred $\text{Fe}^{3+}/\Sigma\text{Fe}$ value and are not considered further. The total number of different glasses with preferred $\text{Fe}^{3+}/\Sigma\text{Fe}$ values is 47, of which 28 were synthesised at known $f\text{O}_2$ and 20 coexist with olivine.

We have supplemented our new experimental data with a further 108 experimental glasses of broadly basaltic (or haplobasaltic) and basaltic andesite (≤ 60 wt% SiO_2) composition with measured $\text{Fe}^{3+}/\Sigma\text{Fe}$ performed at controlled (or measured) $f\text{O}_2$. This dataset was selected to include experiments that contain olivine and/or experiments where the glass contains known amounts of dissolved H_2O . This provides, respectively, an additional set of data with which to explore olivine-melt partitioning and an additional set of $\text{Fe}^{3+}/\Sigma\text{Fe}$ data for hydrous systems. The studies used are: Mysen (2006), Matzen et al. (2011), Partzsch et al. (2004), Botcharnikov et al. (2005), Vetere et al. (2014), Wilke et al. (2002), Moore et al. (1995), and Schuessler et al. (2008). The number and type of measurements from these studies are provided in Supplementary Table 2.

Calculated $\text{Fe}^{3+}/\Sigma\text{Fe}$ in hydrous basaltic melts

In Fig. 5, we compare the measured $\text{Fe}^{3+}/\Sigma\text{Fe}$ in our 28 glasses from experiments with known $f\text{O}_2$, together with the additional 108 glasses described above, to the calculated $\text{Fe}^{3+}/\Sigma\text{Fe}$ at the experimental P–T– $f\text{O}_2$ using three different algorithms: the widely used algorithm of Kress and Carmichael (1991), which includes a pressure term; and the recent algorithms of Borisov et al. (2018) and O’Neill et al. (2018) that do not.¹ None of these algorithms includes an explicit H_2O term, even though O’Neill et al. (2018) did use the hydrous data of Moore et al. (1995) in their calibration. The agreement for all three algorithms is encouraging (average absolute deviation, $aad = 0.06$ – 0.08 in $\text{Fe}^{3+}/\Sigma\text{Fe}$), with Borisov et al. (2018) performing marginally better than the other two. The observed aad is in excellent agreement with that claimed by Borisov et al. (2018) for their much larger, anhydrous calibrant dataset (± 0.05 at $\text{Fe}^{3+}/\Sigma\text{Fe} = 0.25$). The good performance of both algorithms is despite the fact that the combined dataset in Fig. 5 ($n = 136$) includes a large number ($n = 79$) of hydrous glasses, whereas only that of O’Neill et al. (2018) included any hydrous glass in their calibrations. For our dataset, plots (not shown) of the deviation of $\text{Fe}^{3+}/\Sigma\text{Fe}$ from the values calculated using any of the three algorithms against wt% H_2O (or $a\text{H}_2\text{O}$, calculated at

¹ For a useful comparison of a variety of pre-2016 algorithms for the relationship between $\text{Fe}^{3+}/\Sigma\text{Fe}$ and $f\text{O}_2$ see Putirka (2016).

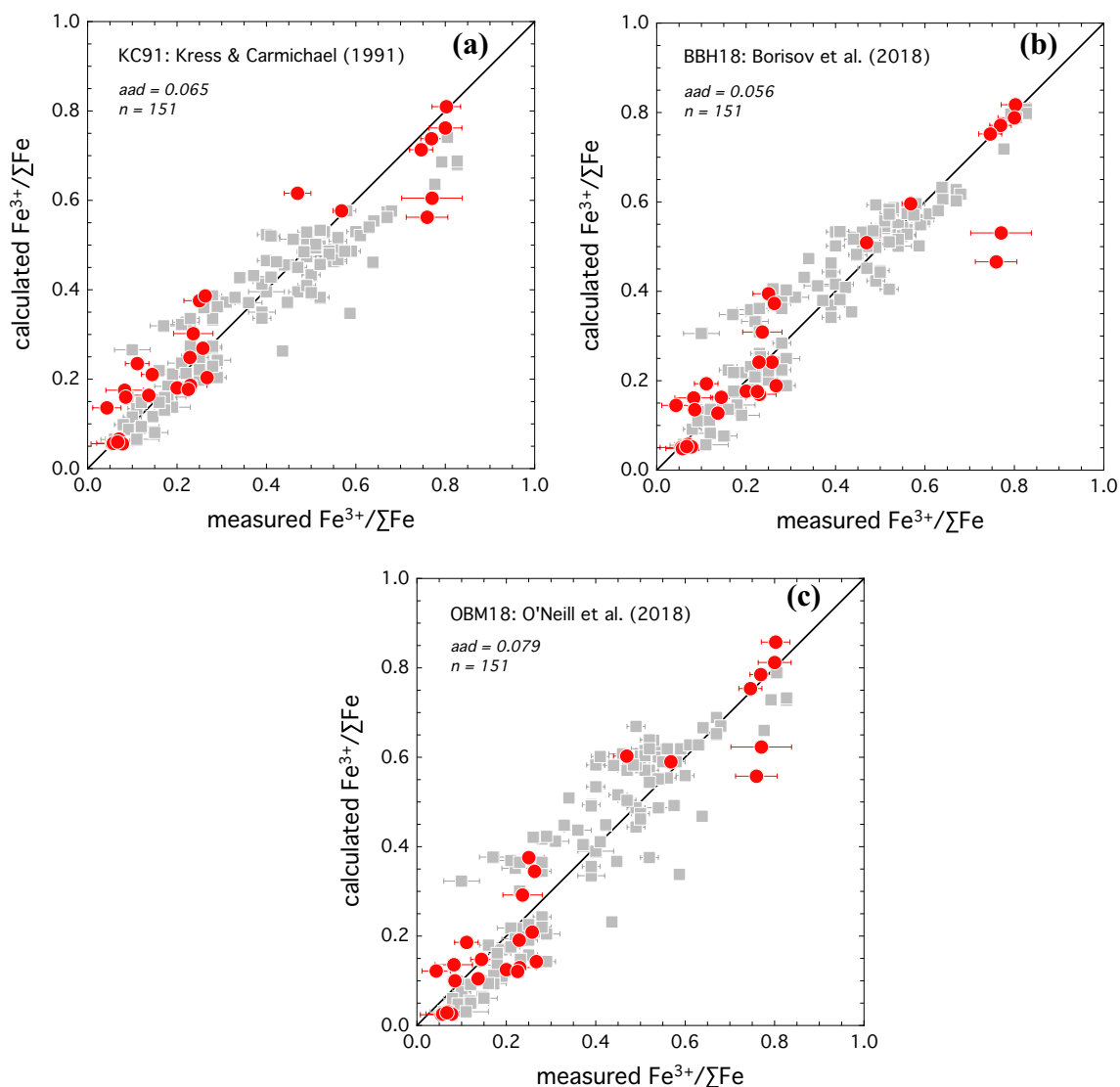


Fig. 5 Tests of the ability of three widely used algorithms to recover $\text{Fe}^{3+}/\Sigma\text{Fe}$ from experiments at known temperature and $f\text{O}_2$. **A** Kress and Carmichael (1991); **b** Borisov et al. (2018); **c** O'Neill et al. (2018). Only Kress and Carmichael (1991) include a pressure term.

Plotted are new data from Table 3 (red symbols), alongside published data for hydrous basalts (grey symbols). A total of 151 glasses are plotted; the average absolute deviation (*aad*) from the analysed values is given in each panel

experimental conditions using the method of Burnham 1979) does not reveal any systematic behaviour. This finding is in agreement with previous studies that conclude that dissolved H_2O has negligible influence on $\text{Fe}^{3+}/\Sigma\text{Fe}$ in silicate melts (e.g., Sisson and Grove 1993; Moore et al. 1995; Botcharnikov et al. 2005). If there is an influence on $\text{Fe}^{3+}/\Sigma\text{Fe}$ of H_2O it is subtle and non-systematic, and requires further, targeted experimental exploration.

It is noteworthy that the two persistent outliers in all panels of Fig. 5 are both highly oxidised glasses from our dataset with > 8wt % H_2O (HAB-20, HAB-23). These are the wettest glasses yet analysed for $\text{Fe}^{3+}/\Sigma\text{Fe}$, so it is unclear whether their failure to lie on the 1:1 line reflects an effect

of very high H_2O on $\text{Fe}^{3+}-\text{Fe}^{2+}$ equilibria or a consequence of analytical challenges in such unstable glasses even using SMS. We conclude that, except possibly for very H_2O -rich basaltic glasses, there is no appreciable interaction between Fe species and H_2O , such that the algorithms of Borisov et al. (2018), O'Neill et al. (2018) and Kress and Carmichael (1991) can be used with some confidence. For reference, in a typical basalt the average absolute deviation of ± 0.05 in calculated $\text{Fe}^{3+}/\Sigma\text{Fe}$ equates to approximately ± 0.6 log units of $f\text{O}_2$ at NNO + 1 and 1250 °C. This gives an indication of the accuracy available to recover $f\text{O}_2$ from a hydrous mafic melt with known $\text{Fe}^{3+}/\Sigma\text{Fe}$ and equilibration temperature. In all subsequent calculations we will adopt, for convenience,

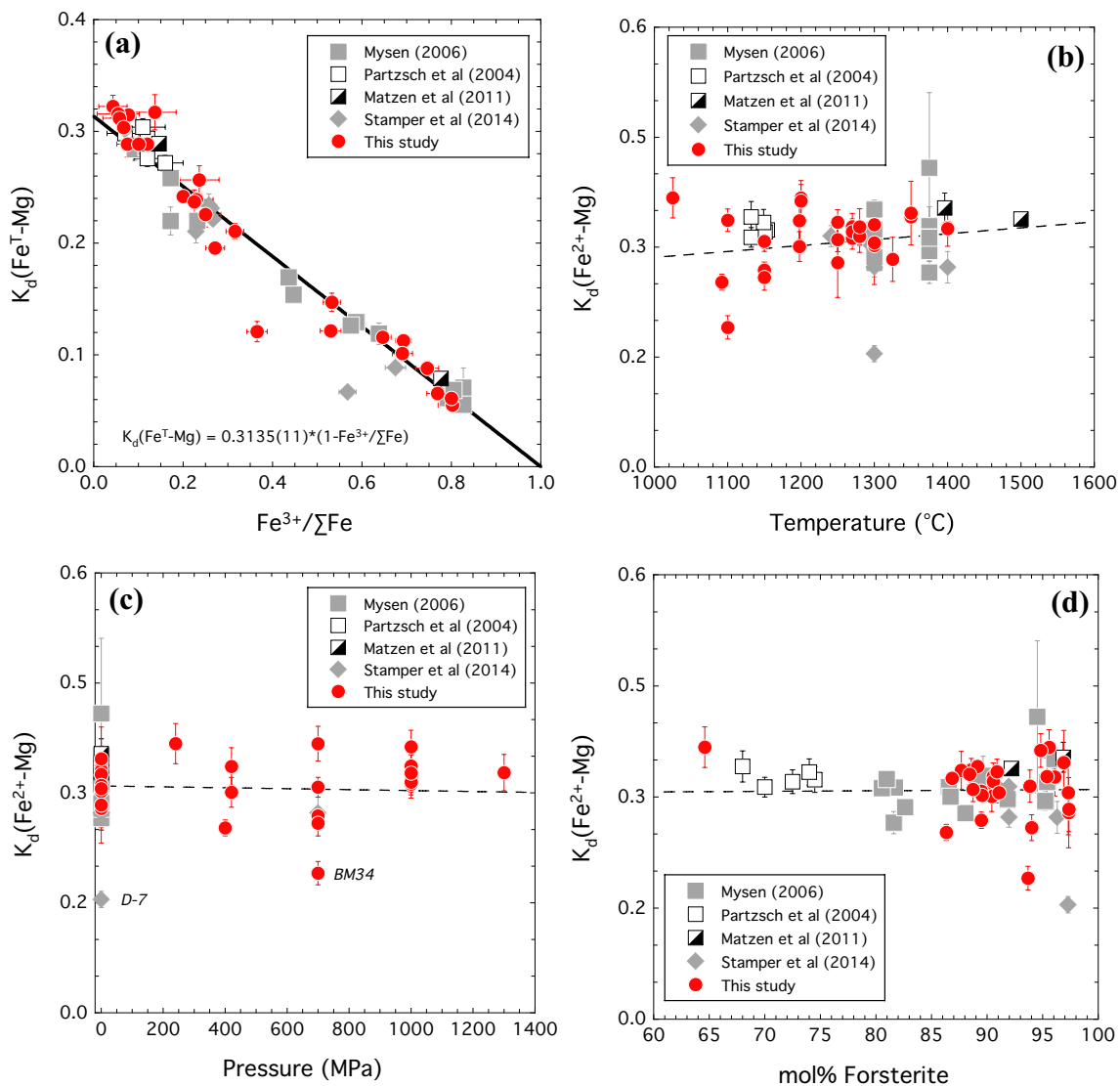


Fig. 6 Fe–Mg exchange between olivine and melt in new experiments and published studies given in Supplementary Table 2. **a** $K_{d_{\text{Fe}^{\text{T}}-\text{Mg}}}$ versus measured $\text{Fe}^{3+}/\Sigma\text{Fe}$ showing the diluting effect of Fe^{3+} . For clarity we distinguish the experiments of Stamper et al. (2014) that are included in Table 2. The line has a slope and inter-

cept of 0.3135 ± 0.0011 . $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ versus **b** temperature; **c** pressure; and **d** olivine forsterite content (mol%). The dashed lines are shown for guidance only. Note the two persistent outlier experiments (runs BM34 and D-7) in all panels; labelled in **c**

the Borisov et al. (2018) algorithm, although, according to Fig. 5, the results would be broadly similar for the other two algorithms, as well as that of Putirka (2016).

Olivine-melt partitioning of Fe^{2+} , Mn and Mg

Olivine-melt $K_{d_{\text{Fe}^{\text{T}}-\text{Mg}}}$ shows a considerable range in our experimental dataset, as would be predicted from the presence of Fe^{3+} in the glass. As expected, $K_{d_{\text{Fe}^{\text{T}}-\text{Mg}}}$ decreases with increasing $\text{Fe}^{3+}/\Sigma\text{Fe}$ as the availability of Fe^{2+} diminishes and, as a consequence, olivine becomes more Fo-rich (Fig. 6a). A weighted fit to Eq. (4) yields

$$K_{d_{\text{Fe}^{\text{T}}-\text{Mg}}} = 0.3135 \pm 0.0011 \times \left(1 - \frac{\text{Fe}^{3+}}{\Sigma\text{Fe}} \right). \quad (5)$$

This is consistent with a simple dilution of Fe^{2+} by Fe^{3+} in the melt, in the manner hinted at from the data of Roeder and Emslie (1970; Fig. 1). The linearity of the relationship across a very wide range of $\text{Fe}^{3+}/\Sigma\text{Fe}$ argues strongly against significant non-ideal interactions between Fe^{2+} and Fe^{3+} in the melt, of the type proposed by Jayasuriya et al. (2004). The intercept at $\text{Fe}^{3+}/\Sigma\text{Fe}$ equates to $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ and is in excellent agreement with the canonical value of 0.30 ± 0.03 of Roeder and Emslie (1970). This observation

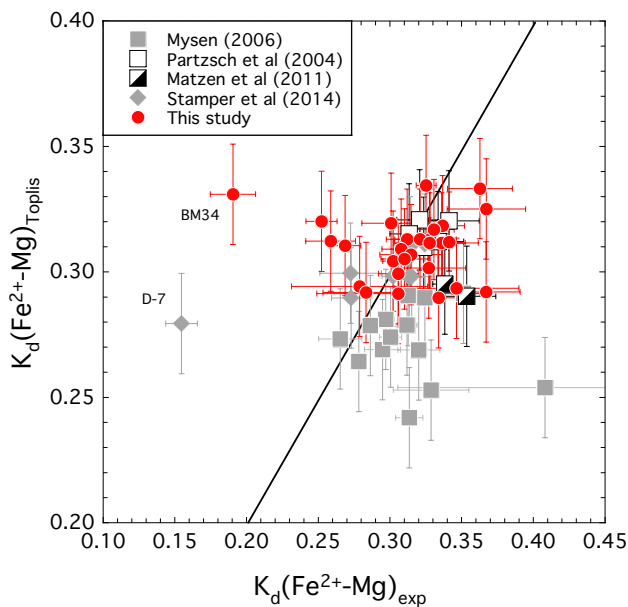


Fig. 7 Comparison of $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ calculated using the algorithm of Toplis (2005) with the experimental data in Table 3. The 1:1 line is shown. The two persistent outliers in our dataset (runs BM34 and D-7) are highlighted. Error bars are 1 sd for the experimental measurements and ± 0.02 for the Toplis (2005) method

confirms Roeder and Emslie's (1970) finding that $f\text{O}_2$ has little effect on $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$. Consequently, the measured value of $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ can be used to recover $\text{Fe}^{3+}/\Sigma\text{Fe}$, provided that the potential role of olivine non-ideality can be disregarded or suitably accounted for. We return to this issue in a later section.

We explore the influence of other parameters on $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ in Fig. 6b–d. There is no discernible influence of temperature (Fig. 6b) suggesting that over the studied temperature range the change in free energy of reaction (1), ΔG_1 , is relatively small. According to the standard state free energy of fusion data compiled by Toplis (2005) an increase in temperature from 1100 to 1500 °C would equate to an increase in ΔG_1 of 2.9 kJ mol⁻¹, corresponding to a 14% increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$, broadly consistent with that observed. There is also no effect of dissolved H₂O (as previously discussed) or pressure (Fig. 6c). Using the volume change for reaction (1), ΔV_1 , as presented by Toplis (2005), we would expect very little change in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ over the pressure range studied. For example, at 1200 °C, $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ should increase by just 4% from one atmosphere to 1400 MPa, again broadly consistent with that observed.

Our observations raise the possibility that much of the pressure dependence claimed by Ulmer (1989) results simply from the effect of pressure on ferric–ferrous ratio in basaltic melts. For a given $f\text{O}_2$, at higher pressures Fe^{2+} in the melt is stabilised relative to Fe^{3+} up to at least 3 GPa (Kress and Carmichael, 1991). Thus, as pressure increases

the availability of Fe^{2+} will increase, leading to an increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$. This is precisely the effect seen by Ulmer (1989); from 1 atmosphere to 3 GPa his experiments show an increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ from 0.30 to 0.37. Assuming that $f\text{O}_2$ in these experiments remains constant, relative to a solid state buffer such as NNO, the $\text{Fe}^{3+}/\Sigma\text{Fe}$ ratio, calculated using Kress and Carmichael (1991) for Ulmer's (1989) starting material and a reference temperature of 1200 °C, ranges from 0.191 at atmospheric pressure to 0.105 at 3 GPa. From the one atmosphere value of 0.30, this equates to an increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ to 0.33, approximately 50% of the observed increase. However, Ulmer's (1989) higher pressure experiments used graphite-lined Pt capsules, and consequently are significantly more reduced than NNO, approximating the iron–wüstite buffer. Thus, the higher pressure melts will contain negligible Fe^{3+} , leading to a further increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ to 0.37, relative to the 1 atmosphere value of 0.30, as observed. We suggest that the apparent pressure increase in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ observed by Ulmer (1989) is a combination of two effects: the decrease in $\text{Fe}^{3+}/\Sigma\text{Fe}$ that occurs with increasing pressure at fixed temperature along an $f\text{O}_2$ buffer; and the more reduced nature of his higher pressure experiments compared to those at one atmosphere.

Finally, there is a small negative dependence of $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ on olivine composition (Fig. 6d), consistent with modest non-ideality on the forsterite–fayalite join, as previously noted by Toplis (2005). For a symmetrical regular solution, characterised by a binary interaction parameter $W_{\text{Fe}-\text{Mg}}$, $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ will decrease from Fo_{50} towards both the fayalite (Fo_0) and forsterite (Fo_{100}) end-members. With a value of $W_{\text{Fe}-\text{Mg}} = 2.6$ kJ mol⁻¹, as determined experimentally O'Neill et al. (2003), $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ (at 1200 °C) would be expected to decrease by ~16% from Fo_{60} to Fo_{100} . This is a small effect, but not inconsistent with the variation seen in Fig. 6d. In a subsequent section we incorporate olivine non-ideality into our expression for $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$.

The fact that Eq. (5) holds across a wide range in pressure, temperature and melt composition (especially H₂O) contrasts with the strong melt compositional dependence of $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ that was proposed by Toplis (2005) and Putirka (2016) based on large published experimental datasets. In Fig. 7, we compare our measured values of $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$ to those calculated using the method of Toplis (2005) at our experimental conditions. There is broad agreement (within about ± 0.05 in $K_{d_{\text{Fe}^{2+}-\text{Mg}}}$) despite the fact that Toplis (2005) does not include an explicit compositional term for Fe^{3+} in his parameterisation. Instead he used the parameterisation of Kilinc et al. (1983) to calculate $\text{Fe}^{2+}/\text{Fe}^{3+}$ at the run T– $f\text{O}_2$ conditions for his experimental dataset. Kilinc et al.'s (1983) parameterization was updated by Kress and Carmichael (1991) using additional experimental data, with significantly different temperature and composition parameters as a result. It is unclear to what extent

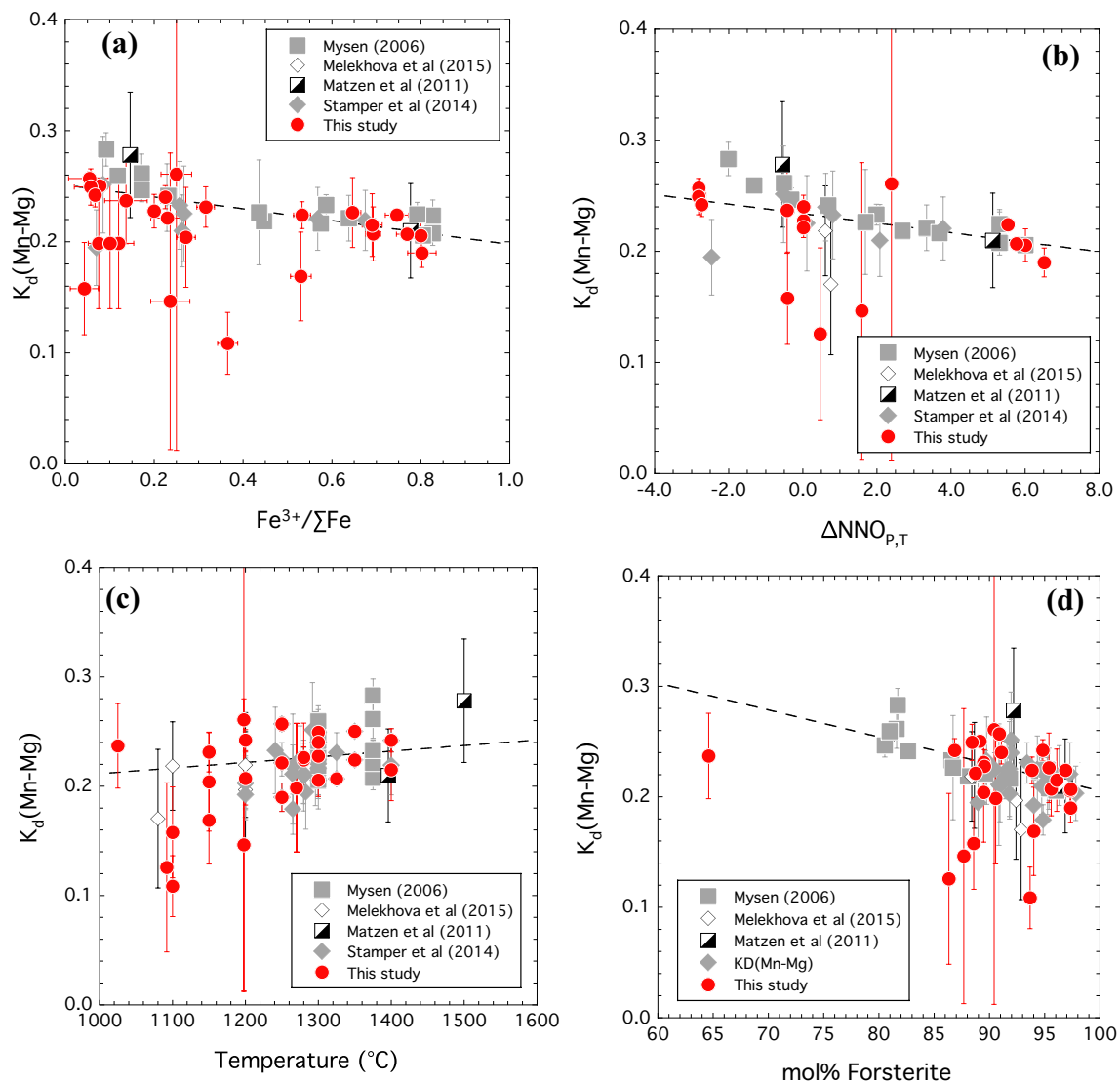


Fig. 8 Mn–Mg exchange between olivine and melt in new experiments and published studies given in the text—for clarity we distinguish the experiments of Stamper et al. (2014) and Melekhova et al.

(2015). $K_{\text{d}_{\text{Mn-Mg}}}$ versus: **a** measured $\text{Fe}^{3+}/\Sigma\text{Fe}$; **b** $f\text{O}_2$ (expressed as log units relative to NNO buffer); **c** temperature; and **d** olivine forsterite content (mol%). The dashed lines are shown for guidance only

some of the compositional dependence $K_{\text{d}_{\text{Fe}^{2+}\text{-Mg}}}$ identified by Toplis (2005) is aliased to compositional dependence of $\text{Fe}^{2+}/\text{Fe}^{3+}$ above and beyond that captured by the parameterisation of Kilinc et al. (1983). In this respect, it is notable that Toplis' (2005) compositional terms include a strong influence of molar Na_2O and K_2O in the melt, the two components known to exert the greatest influence on $\text{Fe}^{2+}/\text{Fe}^{3+}$ in melts at fixed P, T and $f\text{O}_2$ (Kress and Carmichael 1991; Borisov et al. 2018). It is very difficult to disentangle these two effects in the absence of measured $\text{Fe}^{3+}/\Sigma\text{Fe}$ in experimental glasses.

In contrast to Fe–Mg exchange between olivine and melt, we would not expect Mn–Mg exchange to be redox-sensitive under most terrestrial $f\text{O}_2$ conditions. In Fig. 8, we plot $K_{\text{d}_{\text{Mn-Mg}}}$ for our experimental dataset against a variety of

intensive and compositional parameters. As expected, a strong variation with $\text{Fe}^{3+}/\Sigma\text{Fe}$ (Fig. 8a) is not observed, because Mn is divalent across almost all of the $f\text{O}_2$ range considered (Stokes et al. 2019). Nonetheless, at the highest $\text{Fe}^{3+}/\Sigma\text{Fe}$, i.e., the most oxidised conditions, any Mn that is trivalent should lead to a small reduction in $K_{\text{d}_{\text{Mn-Mg}}}$. In Fig. 8b, we show $K_{\text{d}_{\text{Mn-Mg}}}$ plotted against ΔNNO (the deviation in log units relative to the NNO buffer at P and T). Any reduction in $K_{\text{d}_{\text{Mn-Mg}}}$ at the highest ΔNNO is evidently very small, consistent with the observation that $\text{Mn}^{3+}/\Sigma\text{Mn}$ in lime–alumina–silica melts is low, even in air (Tamura et al. 1987). Moreover, $\text{Mn}^{3+}/\Sigma\text{Mn}$ decreases significantly with decreasing molar Na/Si ratios (Schreiber et al. 1994), such that for basalts (Na/Si ≈ 0.1) equilibrated in air at ~ 1150 $^{\circ}\text{C}$ $\text{Mn}^{3+}/\Sigma\text{Mn}$ will be less than

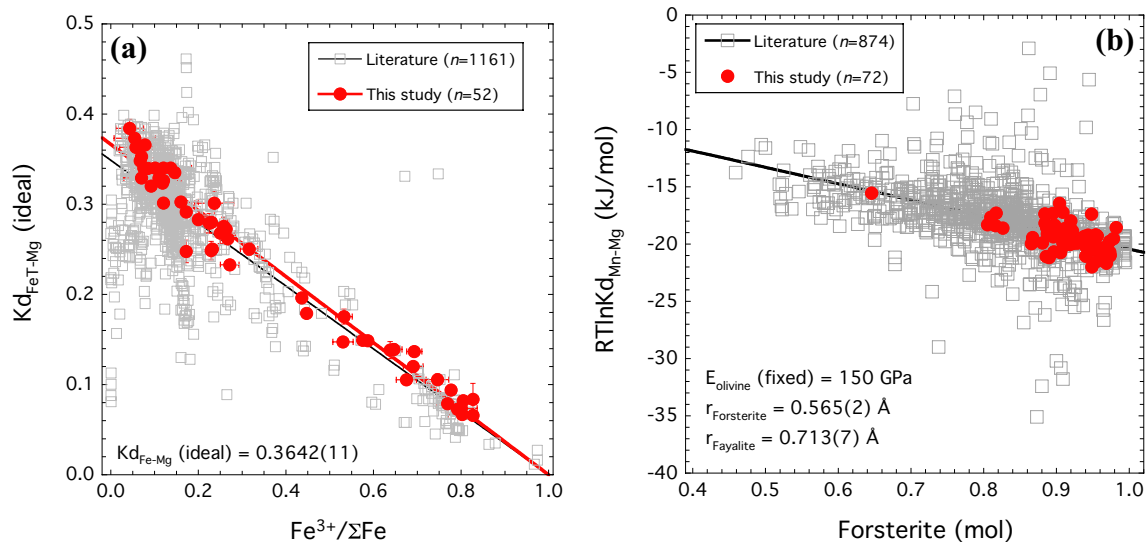


Fig. 9 Models for Fe–Mg and Mn–Mg exchange coefficients. **a** $Kd_{Fe^{2+}-Mg}$ (after correction for olivine non-ideality, as described in text) versus $Fe^{3+}/\Sigma Fe$. Data labelled ‘this study’ include experiments presented in Table 2 plus those additionally plotted in Fig. 6a for which $Fe^{3+}/\Sigma Fe$ is independently measured (see Supplementary Table 2). ‘Literature data’ are taken from the compilation of Matzen et al. (2011), whence original sources can be found, plus additional data from Laubier et al. (2014), Gaetani and Grove (1997), Mallman and O’Neill (2009, 2013), Canil (1997), and Canil and Fedortchouk

(2001). Glass $Fe^{3+}/\Sigma Fe$ was not measured in these experiments; the plotted value is calculated using Borisov et al. (2018) at the experimental T - fO_2 and, therefore, subject to greater uncertainty than the measured values. The line (red) fitted to the data from this study data has a slope and intercept of $Kd_{Fe^{2+}-Mg} = 0.3642 \pm 0.0011$. The line (black) through the entire literature dataset has a very similar slope of 0.349 ± 0.002 . **b** $RT \ln Kd_{Mn-Mg}$ (in $kJ\ mol^{-1}$) plotted against molar fraction Fo in olivine. Data sources as in **a**. The black line is a fit to the lattice strain Eq. (10) with the fit parameters given

0.02. Thus the effect of redox on Kd_{Mn-Mg} is expected to be minimal under all conditions investigated experimentally and likely to be found in nature (e.g., Stokes et al. 2019).

Kd_{Mn-Mg} shows minor dependence on temperature (Fig. 8c) and olivine composition (Fig. 8d), as expected for trace element substitution. To a large extent these effects are interlinked in the experimental dataset and should be considered in combination. Mn^{2+} exchange for Fe^{2+} or Mg^{2+} in olivine is likely to be highly non-ideal, due to the large sixfold ionic radius differences (Shannon, 1976) between Mn^{2+} (0.83 Å), Fe^{2+} (0.78 Å) and Mg^{2+} (0.72 Å). The ease of inserting an Mn^{2+} ion into the olivine lattice increases with temperature at fixed olivine composition, and with decreasing forsterite content at fixed temperature. This behaviour is consistent with the lattice strain model of trace element partitioning (Blundy and Wood, 1994), as developed further below.

Discussion

The experimental data presented above show the strong dependence of Fe–Mg exchange on fO_2 , but the relative insensitivity of Mn–Mg exchange to the same parameter. This raises the possibility of using Fe–Mg partitioning systematics to determine fO_2 from equilibrium pairs of olivine and silicate melt, for example in high-pressure experiments

where fO_2 is hard to control/monitor, and using the redox-insensitive Mn–Mg exchange as a means to test for olivine–melt equilibrium. Ultimately our goal is to introduce a simple method to correct olivine-hosted melt inclusion compositions for post-entrapment crystallization (using Mn–Mg) and then recover the magmatic fO_2 (using Fe–Mg). We are helped in this enterprise by the fact that existing models for ferric–ferrous equilibria in silicate melts as a function of redox (e.g., Kress and Carmichael 1991; Borisov et al. 2018; O’Neill et al. 2018), have proven surprisingly accurate, even for hydrous basaltic compositions (Fig. 5). The first step is to develop models for Fe–Mg and Mn–Mg exchange between olivine and melt, and then to test these expressions against large datasets of experimental olivine–melt pairs.

A model for Fe–Mg partitioning in basaltic melts

Ignoring, for the moment, non-ideality in the melt, Fe^{2+} –Mg exchange can be described by the following relationship (cf. Toplis 2005):

$$Kd_{Fe^{2+}-Mg} = \exp \left\{ \frac{-\Delta H_1 + T\Delta S_1 - P\Delta V_1 + W_{FeMg}^{olivine} (1 - 2X_{Fo})}{RT} \right\}, \quad (6)$$

where the terms ΔH_1 , ΔS_1 and ΔV_1 denote, respectively, the enthalpy, entropy and volume changes of reaction (1), and $W_{\text{FeMg}}^{\text{olivine}}$ is a symmetrical regular solution interaction parameter for the forsterite–fayalite binary solid solution. $W_{\text{FeMg}}^{\text{olivine}}$ has been constrained experimentally to be in the region of a few kJ mol^{-1} ; we will adopt the value of 2.6 kJ mol^{-1} of O'Neill et al. (2003). As noted above, our experimental data provide some constraints on ΔH_1 , ΔS_1 and ΔV_1 over the P–T–X studied. Given the limited temperature dependence (Fig. 6b) ΔH_1 is expected to lie close to zero. We did explore the use of $\Delta H_1 = +6.766 \text{ kJ mol}^{-1}$ derived from the free energy of fusion of forsterite and fayalite (Toplis 2005),² but it led to no improvement in our modelled fits, suggesting that the effective ΔH_1 is smaller than this value, probably due to fortuitous cancellation by non-ideal interactions of Fe^{2+} and Mg in the melt. Beattie (1993), for example, obtains a value for ΔH_1 of $+3.2 \pm 0.8 \text{ kJ mol}^{-1}$ using experimental olivine–melt pairs. The limited pressure dependence (Fig. 6c) suggests that ΔV_1 is also small; Toplis (2005) proposes a value of $-0.35 \text{ kJ GPa}^{-1} \text{ mol}^{-1}$, while Beattie (1993) obtains a value of $-0.09 \pm 0.11 \text{ kJ GPa}^{-1} \text{ mol}^{-1}$ from experimental olivine–melt data. The remaining term, ΔS_1 , embraces the entropy of mixing of Fe^{2+} and Mg in both olivine and melt. The quantity $\exp(\Delta S_1/R)$ in Eq. (6) equates to the ‘ideal’ value of $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ (termed $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0$) prior to any correction for olivine non-ideality. The value of $\exp(\Delta S_1/R)$ using the derived thermodynamic data of Beattie (1993) is 0.121; the equivalent value from Toplis (2005) is 0.414. We can use our experimental data to derive a value for $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0$ by modifying Eq. (6) to

$$\text{Kd}_{\text{Fe}^{2+}\text{-Mg}} = \text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0 \times \exp\left(\frac{\Delta W_{\text{Fe}^{2+}\text{-Mg}}^{\text{olivine}} (1 - 2X_{\text{Fo}})}{RT}\right), \quad (7)$$

where $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0$ can then be obtained from a weighted regression of $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}} / \exp\left(\frac{\Delta W_{\text{Fe}^{2+}\text{-Mg}}^{\text{olivine}} (1 - 2X_{\text{Fo}})}{RT}\right)$ against $\text{Fe}^{3+}/\Sigma\text{Fe}$. For the 52 experiments with known $\text{Fe}^{3+}/\Sigma\text{Fe}$ the regressed value of $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0$ is 0.3642 ± 0.0011 at $\text{Fe}^{3+}/\Sigma\text{Fe} = 0$ (Fig. 9a). To obtain this value we eliminated two persistent outliers in the dataset: experiments D-7 of Stamper et al (2014) and BM34 of Melekhova et al (2015). Note that for a symmetrical, regular solution $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0 = 0.3642$ gives the Fe^{2+} –Mg exchange coefficient at Fo_{50} ; it will be lower for olivines with higher or lower Fo than 0.5. This accounts for the difference from the value of $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}} = 0.3135$ (Fig. 6a) presented above, which takes no account of olivine non-ideality. For example, for a Fo_{70}

olivine at $1200 \text{ }^\circ\text{C}$, the bracketed term in Eq. (7) equals 0.92; for Fo_{90} at $1450 \text{ }^\circ\text{C}$ it equals 0.86. It is worth noting that the strong dependence of the olivine–melt Mg partition coefficient (D_{Mg}) on olivine Fo content will lead to an apparent negative correlation between $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ and D_{Mg} , such as that observed by Herzberg and O’Hara (2002). Evidently, any such correlation should be carefully evaluated in the light of olivine non-ideality, as discussed above in the context of Fig. 6c.

An assumption in using Eq. (7) to describe Fe^{2+} –Mg exchange between olivine and melt is that melt composition does not play a role, i.e., a single value of $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}^0$ captures the full variation in the data provided that $\text{Fe}^{3+}/\Sigma\text{Fe}$ is known (measured) and can be treated as an independent variable. Toplis (2005) and Putirka (2016) have argued, on the basis of an experimental dataset for which $\text{Fe}^{3+}/\Sigma\text{Fe}$ was not measured, that additional compositional terms are important. Unfortunately, the experimental, olivine-bearing dataset with measured glass $\text{Fe}^{3+}/\Sigma\text{Fe}$ is too small ($n=55$) to explore fully such additional melt compositional effects. Thus, as noted by Matzen et al. (2011) in their Appendix, some of the compositional dependence in the $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ expressions of Toplis (2005) may arise through any compositional dependence of melt $\text{Fe}^{3+}/\Sigma\text{Fe}$ not fully captured by the algorithm of Kilinc et al. (1983). To illustrate this point, we show also in Fig. 9a a database of over 1000 experimental olivine–melt $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$, for which $f\text{O}_2$ is known but $\text{Fe}^{3+}/\Sigma\text{Fe}$ is not. The data are fitted to an adapted version of Eq. (5) that allows for olivine non-ideality, using the expression in Eq. (7), to give

$$\text{Kd}_{\text{Fe}^{2+}\text{-Mg}} = 0.3642 \times \left(1 - \frac{\text{Fe}^{3+}}{\Sigma\text{Fe}}\right) \times \exp\left(\frac{312.7(1 - 2X_{\text{Fo}})}{T}\right), \quad (8)$$

where T is in Kelvin and X_{Fo} is the molar fraction forsterite in olivine. In fitting this equation, we calculated $\text{Fe}^{3+}/\Sigma\text{Fe}$ at the experimental T– $f\text{O}_2$ conditions using the expression of Borisov et al (2018). The bulk of the data lie close to the regression line; 57% of all of the calculated $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ values lie within 0.02 of the experimental values, and the average absolute deviation (*aad*) of all 1135 experiments is 0.030. If we consider only the natural compositions, i.e., those with non-zero alkalis, *aad* reduces to 0.022. The *aad* is also dependent on the total alkali contents ($\text{Na}_2\text{O} + \text{K}_2\text{O}$). For example, melts with $\text{Na}_2\text{O} + \text{K}_2\text{O} \geq 6 \text{ wt}\%$ have *aad* = 0.040, while those with $\text{Na}_2\text{O} + \text{K}_2\text{O} \geq 9 \text{ wt}\%$ have *aad* = 0.063. This behaviour cannot be attributed to olivine non-ideality; it must instead be the result of either non-ideality in the melt [the interpretation preferred by Toplis (2005), and Putirka (2016)] or a failure of the Borisov et al (2018) algorithm to capture fully the effect of alkalis on $\text{Fe}^{3+}/\Sigma\text{Fe}$. In all likelihood the deviation is a combination of these two factors, but without determinations of $\text{Fe}^{3+}/\Sigma\text{Fe}$ in these

² Note the change in sign because Toplis (2005) provides data for the reverse of reaction (1).

alkali-rich experiments it is not possible to disentangle the two effects. We conclude that Eq. (8) is best suited to basalts with between 0 and 8 wt% Na₂O + K₂O ($aad=0.019$); at higher alkali contents its precision is reduced slightly. As noted by Toplis (2005), the analytical precision of $Kd_{Fe^{3+}-Mg}$ determinations in most experiments is of the order 0.02.

The observed scatter in the data at low $Fe^{3+}/\Sigma Fe$ (Fig. 9a) is curious. It cannot arise through olivine non-ideality or temperature. It may arise instead from the failure of the Borisov et al (2018) algorithm to capture precisely $Fe^{3+}/\Sigma Fe$ at low fO_2 , as suggested by Fig. 5b. Such a situation likely has its origins in the difficulty of determining $Fe^{3+}/\Sigma Fe$ precisely by spectroscopic or wet chemical means when the Fe^{3+} content is very low (O'Neill et al. 2018). This problem warrants further investigation, with additional data on $Fe^{3+}/\Sigma Fe$ at very reducing conditions. For the time being we consider that Eq. (8) provides an adequate description of $Kd_{Fe^{3+}-Mg}$ for basaltic magmas under most terrestrial redox conditions.

The advantage that Eq. (8) offers over that of Toplis (2005) is that it contains no empirical fit parameters to describe the effect of melt non-ideality on $Kd_{Fe^{3+}-Mg}$. Any

$$Kd_{Mn-Mg} = \exp \left[\frac{-4\pi N_A E_M^{2+}}{RT} \left\{ \frac{r_{0(M)}^{2+}}{2} (r_{Mg}^2 - r_{Mn}^2) - \frac{1}{3} (r_{Mg}^3 - r_{Mn}^3) \right\} \right], \quad (9)$$

melt compositional dependencies arise exclusively from those in the algorithm used for $Fe^{3+}/\Sigma Fe$, in this case Borisov et al (2018); the term for olivine compositional dependence is independently derived. Equation (8) offers a straightforward means to determine the composition of olivine crystallising from a melt at known temperature and fO_2 . Conversely, from a measured value of $Kd_{Fe^{3+}-Mg}$ at known temperature and olivine composition (X_{Fo}), $Fe^{3+}/\Sigma Fe$ (and fO_2) can be recovered by rearrangement of Eq. (8) and use of an algorithm such as that of Borisov et al (2018) or Putirka (2016).

Our data do not suggest a pressure dependence of $Kd_{Fe^{3+}-Mg}$ in contrast to several previous studies (e.g., Ulmer 1989; Herzberg and O'Hara 1998; Putirka 2005, 2016; Toplis 2005). We speculate above that changing $Fe^{3+}/\Sigma Fe$ in the melt with increasing pressure may account for some apparent pressure dependence. Unfortunately there are no high pressure experimental data with measured $Fe^{3+}/\Sigma Fe$ at known fO_2 with which to test this idea, and our experimental dataset does not extend above 1.7 GPa. For this reason we would

advocate caution in applying Eq. (8) at pressures higher than this. Likewise, as noted above, we do not see an apparent increase of $Kd_{Fe^{3+}-Mg}$ with melt SiO₂ content, in contrast to Toplis (2005) and Putirka (2016). This again likely reflects the limited compositional range of experimental glasses from our olivine-bearing experiments (45.9–56.9 wt% SiO₂ on an anhydrous basis; Table 4) and those in the other data listed in Supplementary Table 2. For this reason we would not recommend using Eq. (8) for olivine-bearing andesitic liquids with more than ~60 wt% SiO₂.

A model for Mn–Mg partitioning in basaltic melts

Unlike Fe^{2+} , Mn is a minor (or trace) element in most natural olivines, allowing for a different thermodynamic treatment. Based on the observations in Fig. 8, we will deploy the lattice strain model for trace element partitioning (Blundy and Wood 1994), as recast for the case of a 'proxy' element (Eq. 8 of Blundy and Wood 2003). In this formulation, which is well suited to describing exchange coefficients (Kds) between trace and major elements, the proxy is Mg and the trace is Mn. This yields

where N_A is Avogadro's number, R is the gas constant, T is temperature in Kelvin, E_M^{2+} is the effective Young's Modulus of the VI-fold M-site in olivine, and $r_{0(M)}^{2+}$ is the optimum radius of that site. r_{Mg} and r_{Mn} are the ionic radii of Mg^{2+} and Mn^{2+} in VI-fold coordination, 0.72 and 0.83 Å, respectively (Shannon 1976). The ideal M-site cation radius changes along the forsterite–fayalite solid solution, because Fe^{2+} (0.78 Å) is larger than Mg^{2+} (0.72 Å). Thus $r_{0(M)}^{2+}$ is not constant. In principle we can use the experimental data, from this study and from the literature, to derive values for E_M^{2+} and for $r_{0(M)}^{2+}$ as a function of olivine composition. However, as noted by Wood and Blundy (1997), there is considerable trade-off between these two parameters from least squares fitting. For that reason, we fix $E_M^{2+} = 150$ GPa, following Beattie (1994) and Purton et al. (2000), and fit only for $r_{0(M)}^{2+}$. We do this by assuming that $r_{0(M)}^{2+}$ increases linearly from forsterite ($r_{0(Fo)}^{2+}$) to fayalite ($r_{0(Fa)}^{2+}$). Thus, Eq. (9) can be rewritten and linearised in such a way that a plot of $RT \ln Kd_{Mn-Mg}$ versus X_{Fo} can be used to obtain $r_{0(Fo)}^{2+}$ and $r_{0(Fa)}^{2+}$:

$$RT \ln Kd_{Mn-Mg} = -150 \times 4\pi N_A \left\{ \left(\frac{X_{Fo} r_{0(Fo)}^{2+} + (1 - X_{Fo}) r_{0(Fa)}^{2+}}{2} \right) (r_{Mg}^2 - r_{Mn}^2) - \frac{1}{3} (r_{Mg}^3 - r_{Mn}^3) \right\}. \quad (10)$$

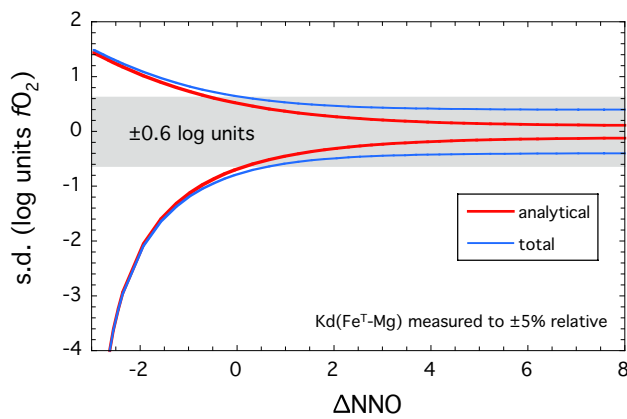


Fig. 10 Fully propagated uncertainty estimates for ΔNNO calculations using $\text{Kd}_{\text{Fe}^{\text{T}}-\text{Mg}}$. Calculated values are strongly dependent on ΔNNO , and greatly magnified at low $f\text{O}_2$. Shown are curves for the typical, propagated analytical uncertainty (red), assuming 5% relative error in $\text{Kd}_{\text{Fe}^{\text{T}}-\text{Mg}}$, and the total uncertainty (blue) that includes 0.38 log units in $f\text{O}_2$ as given by Borisov et al. (2018) for their $\text{Fe}^{3+}/\Sigma\text{Fe}$ algorithm. The shaded region illustrates an uncertainty of ± 0.6 log units in $f\text{O}_2$

Using the literature experimental dataset described above, as well as the new data presented here, we find that this equation describes well the Mn–Mg exchange coefficient for the entire experimental dataset (Fig. 9b), returning values of $r_{0(\text{Fo})}^{2+} = 0.565 \pm 0.002 \text{ \AA}$ and $r_{0(\text{Fa})}^{2+} = 0.713 \pm 0.007 \text{ \AA}$. A more complex expression, that takes into account the possible temperature dependence of $r_{0(\text{Fo})}^{2+}$ and $r_{0(\text{Fa})}^{2+}$ is not warranted. There is no evidence for strong melt compositional dependence of $RT\ln\text{Kd}_{\text{Mn}-\text{Mg}}$; most of the scatter in Fig. 9b arises through analytical uncertainty on the MnO contents of experimental olivines, which are more difficult to measure precisely than major elements (for instance MnO is usually reported to two significant figures compared to four for MgO). For example, a typical uncertainty on $\text{Kd}_{\text{Mn}-\text{Mg}}$ of 15% relative, translates to an uncertainty of $\pm 2 \text{ kJ mol}^{-1}$ in $RT\ln\text{Kd}_{\text{Mn}-\text{Mg}}$, which encompasses over 80% of the observed scatter in Fig. 9b. Note that this approach takes into account both the temperature and olivine composition dependence of $\text{Kd}_{\text{Mn}-\text{Mg}}$, in contrast to the expression of Matzen et al (2017) that considers only the effect of melt MgO content. For olivine-saturated systems, the latter is, of course, a function of both temperature and olivine composition.

Regarding the influence of melt composition on Mn–Mg partitioning, there is no evidence for such an effect in our basaltic experimental dataset. In contrast, Kohn and Schofield (1994) in their study of Mn partitioning between olivine (Fo_{100}) and melt in the system forsterite–albite–anorthite show that $RT\ln\text{Kd}_{\text{Mn}-\text{Mg}}$ varies with the degree of melt polymerisation, increasing from ~ 0.12 to 0.23 over a wide range in NBO/T (0.09–0.37). However, the overall variation in $RT\ln\text{Kd}_{\text{Mn}-\text{Mg}}$ for their experiments is -20.6 to

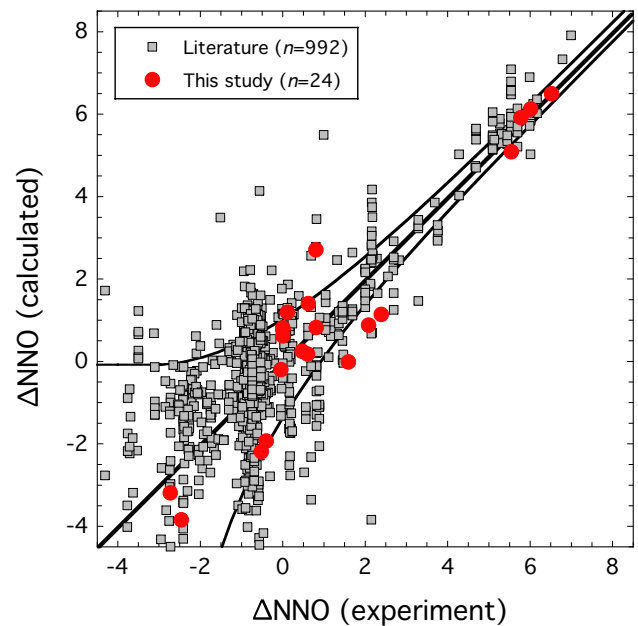


Fig. 11 Calculated ΔNNO for olivine-melt pairs from Table 2 and in the dataset of published experiments introduced in Fig. 8a. Only experiments run at $f\text{O}_2$ above $\text{NNO} - 4.5$ are plotted. The 1:1 line and error envelopes from Fig. 10 are shown as black lines

$-22.9 \text{ kJ mol}^{-1}$, compared to the value of $-20.4 \text{ kJ mol}^{-1}$ calculated for Fo_{100} olivine using Eq. (10). The mean deviation of Kohn and Schofield's (1994) data from this value is only $\pm 1.3 \text{ kJ mol}^{-1}$, despite the wide range in NBO/T. This gives a sense of the relatively small influence of melt composition on $RT\ln\text{Kd}_{\text{Mn}-\text{Mg}}$ compared to olivine composition, which changes by 4.3 kJ mol^{-1} from Fo_{100} to Fo_{70} (Fig. 9b).

Applications

Equation (8) obviously has wide utility in modelling the crystallisation and melting of olivine-bearing systems. By way of example, we focus on two novel oxybarometry applications using the derived expressions for $\text{Kd}_{\text{Fe}^{\text{T}}-\text{Mg}}$ and $\text{Kd}_{\text{Mn}-\text{Mg}}$. The first involves determination of $f\text{O}_2$ for experimental, olivine-bearing melts using $\text{Kd}_{\text{Fe}^{\text{T}}-\text{Mg}}$; the second involves determination of $\text{Fe}^{3+}/\Sigma\text{Fe}$ in olivine-hosted melt inclusions that have first been corrected for post-entrapment modification (crystallisation or dissolution) by the host olivine using $\text{Kd}_{\text{Mn}-\text{Mg}}$.

Oxygen fugacity estimates from olivine-bearing experiments

Equation (8) can be rearranged to obtain $\text{Fe}^{3+}/\Sigma\text{Fe}$ of an experimental glass in equilibrium with olivine of a known

Table 6 Calculated fO_2 for Lesser Antilles experiments using olivine Fe–Mg exchange oxybarometry

Source	Run	T °C	P, GPa	H_2O^c	ΔNNO				
					$\mu XANES^a$	Ol-Sp ^a	AuPd ^a	KC91 ^b	BBH18 ^b
Stamper et al. (2014)	W-1	1150	0.7	4.99 (21)	3.6		2.0	1.7	1.5
Stamper et al. (2014)	W-3	1200	0.7	3.62 (18)	5.2			4.7	4.1
Stamper et al. (2014)	W-7-J	1175	0.7	5.48 (25)	5.5			5.3	4.9
Stamper et al. (2014)	AN-1	1400	0.7	0.28 (4)	5.3	4.3	3.7	5.7	4.8
Stamper et al. (2014)	AN-3	1400	1.0	0.38 (6)	5.5			5.5	4.4
Stamper et al. (2014)	R-5	1280	1.0	2.56 (22)	4.9			4.0	3.1
Stamper et al. (2014)	30	1280	1.3	3.73 (14)	6.1	3.8	1.2	5.2	4.0
Stamper et al. (2014)	35	1200	0.2	2.93 (12)	6.6	5.3	3.2	6.4	6.2
Stamper et al. (2014)	41	1200	0.7	3.70 (14)	5.4			4.2	3.8
Stamper et al. (2014)	23	1275	0.7	3.15 (15)	4.2			3.9	3.3
Stamper et al. (2014)	25	1280	0.7	3.42 (18)	4.7	3.8	3.0	4.6	4.0
Stamper et al. (2014)	R-2	1265	1.0	3.26 (31)	3.7			3.0	2.3
Stamper et al. (2014)	22	1265	1.0	2.90 (17)	5.3	4.2	2.8	5.2	4.4
Stamper et al. (2014)	R-1	1300	1.0	2.78 (21)	3.2			1.8	1.1
Stamper et al. (2014)	28	1300	1.0	3.10 (14)	5.7			4.9	3.9
Stamper et al. (2014)	R-6	1325	1.0	2.90 (23)	3.9			3.0	2.1
Stamper et al. (2014)	12	1200	1.3	3.77 (37)	4.4	3.1	2.6	3.7	2.8
Stamper et al. (2014)	10	1250	1.3	3.59 (56)	3.7	1.7	2.2	2.0	1.2
Stamper et al. (2014)	15	1265	1.3	3.63 (15)	4.0	2.3	2.9	2.9	1.9
Stamper et al. (2014)	32	1280	1.7	2.89 (19)	6.0	3.7	3.1	5.2	3.8
Stamper et al. (2014)	40	1200	0.1	1.90 (10)	4.6			4.5	4.6
Stamper et al. (2014)	24	1280	1.0	2.74 (15)	4.8			5.0	4.2
Stamper et al. (2014)	19	1265	1.7		4.0			4.3	2.9
Stamper et al. (2014)	34	1325	1.7		3.7			0.5	0.0
Stamper et al. (2014)	37	1350	1.7	3.78 (20)	3.8			4.2	2.8
Melekhova et al. (2015)	RSV49_4	1270	1.0	0.6	− 0.2	1.9		− 1.8	− 2.2
Melekhova et al. (2015)	RSV49_11	1250	1.0	0.7		2.3		3.2	2.5
Melekhova et al. (2015)	bmn1	1080	0.4	2.8		− 0.9		1.6	2.0
Melekhova et al. (2015)	BM38	1200	0.7	2.50 (8)	2	2.2		2.6	2.2
Melekhova et al. (2015)	BM40	1150	0.7	3.05 (9)	2.9	1.7		2.5	2.3
Melekhova et al. (2015)	BM43	1100	0.7	3.02 (9)		2.5		3.0	2.9
Melekhova et al. (2015)	BM3	1200	1.0	2.94 (3)	2.3			− 0.1	− 0.4
Melekhova et al. (2015)	BM6	1100	1.0	4.42 (35)	2.8	− 0.4			
Melekhova et al. (2015)	bmn2	1080	0.4	8.3		0.1		3.6	3.9
Melekhova et al. (2015)	BM37	1150	0.7	5.2 (14)	4.2	4.0		4.4	4.2
Melekhova et al. (2015)	BM34	1100	0.7	7.2 (21)	4.9	3.9		4.6	4.8
Melekhova et al. (2015)	BM24	1030	1.0	9.3 (98)		1.8		2.0	1.9
Melekhova et al. (2015)	BM17	1080	1.0	6.7 (5)	4.4	3.4		3.2	2.9
Melekhova et al. (2015)	BM9	1100	1.0	5.34 (48)	3.2	0.6		0.5	0.4
Melekhova et al. (2015)	BM49	1150	1.3	6.00 (17)		3.0		4.1	3.5

^a ΔNNO reported in the original source using the method indicated: $\mu XANES$; olivine-spinal oxybarometry; Fe in AuPd alloy

^b ΔNNO calculated using method described in text in combination with algorithm of Kress and Carmichael (1991) or Borisov et al. (2018)

^cwt% H_2O by SIMS, except where calculated by mass balance (italics). Figure in parentheses is 1 sd in terms of least significant figures

composition at a known (experimental) temperature. This value of $Fe^{3+}/\Sigma Fe$ can then be used to derive fO_2 using the algorithm of Borisov et al (2018), which we adopt here in light of its slightly greater ability to recover experimental

fO_2 for our sample set (Fig. 5b). Determination of fO_2 for experiments is particularly useful at high pressure, when buffering redox and/or preventing the egress or ingress of hydrogen are perennial problems.

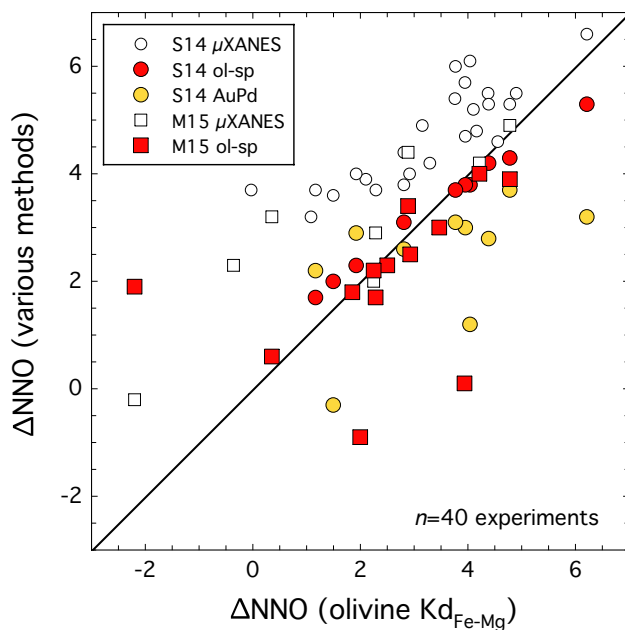


Fig. 12 Calculated ΔNNO for 40 high-pressure experiments on hydrous Lesser Antilles basalts from Melekhova et al. (2015) noted as M15 and Stamper et al. (2014) noted as S14. The horizontal axis shows the values determined from olivine-melt Fe–Mg exchange, while the vertical axis shows values obtained by three independent methods, described in the text and reported by the original authors. μXANES analyses suffer from oxidation due to the high photon flux used (see also Fig. 4)

Before testing our approach against the experimental olivine-melt pairs produced at known redox conditions, it is instructive to gauge the likely precision of the method. The uncertainty on the calculation is not linear with $f\text{O}_2$. The method relies, in effect, on the difference between $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ and $\text{Kd}_{\text{Fe}^{3+}\text{-Mg}}$, after first accounting for olivine non-ideality. As $\text{Fe}^{3+}/\Sigma\text{Fe}$ approaches zero, so $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ approaches $\text{Kd}_{\text{Fe}^{3+}\text{-Mg}}$. This leads to significant uncertainty on $\text{Fe}^{3+}/\Sigma\text{Fe}$, which propagates to considerable uncertainty on calculated $f\text{O}_2$. The same problem is not encountered under more oxidising conditions, when $\text{Fe}^{3+}/\Sigma\text{Fe}$ approaches 1 and $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$ tends to zero. To capture this non-linearity in the uncertainty we have propagated the errors from the various fits performed on the data through the analytical uncertainty, assuming a 5% relative uncertainty on the measured $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$, as well as that arising from the Borisov et al (2018) calibration (0.38 log units in $f\text{O}_2$). The resulting behaviour is shown in Fig. 10. As expected, uncertainty is greatly magnified under reducing conditions, exceeding 0.6 log units around $\text{NNO} - 1$, and clearly becoming meaningless below $\text{NNO} - 4$. The uncertainty contracts considerably at more oxidising conditions, attaining the limit provided by the Borisov et al (2018) calibration above $\text{NNO} + 2$. Over almost all of the $f\text{O}_2$ range, this calibration uncertainty dominates over that due to analytical precision, emphasising the

need for continuous refinement of the $\text{Fe}^{3+}/\Sigma\text{Fe}$ algorithm, especially at very low $f\text{O}_2$.

In Fig. 11, we plot the calculated $f\text{O}_2$ (relative to NNO) for all experiments in the dataset conducted above $\text{NNO} - 4$; we eliminate only the subset of data where $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}} > \text{Kd}_{\text{Fe}^{3+}\text{-Mg}}$ equating to a spurious negative value of $\text{Fe}^{3+}/\Sigma\text{Fe}$. The observed behaviour is in line with the expectations from Fig. 10, namely that precision deteriorates dramatically below $\text{NNO} - 1$. Nonetheless, in 72% of all experiments at $\text{NNO} - 2$ and above we recover $f\text{O}_2$ to within ± 1.2 log units; 44% are recovered within ± 0.6 log units. In addition to the factors discussed above, uncertainty also accrues from the effects of alkalis on $\text{Kd}_{\text{Fe}^{2+}\text{-Mg}}$, either directly through melt non-ideality, or indirectly through the algorithm used to recover $f\text{O}_2$ from $\text{Fe}^{3+}/\Sigma\text{Fe}$. Once again we emphasise that our method is best applied only to relatively oxidised melts (above $\sim\text{NNO} - 1$) with less than about 8 wt% $\text{Na}_2\text{O} + \text{K}_2\text{O}$.

We test our approach on a set of real high-pressure experiments where the $f\text{O}_2$ was either not constrained directly, e.g., by solid-state buffers, or may have been compromised by hydrogen diffusion through the capsule walls. We have selected 40 experiments from Stamper et al. (2014) and Melekhova et al. (2015) on magnesium-rich basalts from the Lesser Antilles with varying amounts of added H_2O (Table 6). In these experiments various alternative strategies were employed to recover $f\text{O}_2$, including μXANES , olivine-spinel oxybarometry (O'Neill and Wall 1987), and the solubility of iron in AuPd alloy capsules (Barr and Grove 2010). In Fig. 12, we compare these different methods. As expected, we find that the μXANES analyses of the glasses from these hydrous experiments yield higher $f\text{O}_2$ estimates than all other methods, due to the oxidative effects of the high photon flux used in the analyses. We can also see the wide variation in $f\text{O}_2$ that results from varying amounts of Fe redox due to hydrogen diffusion, a phenomenon hard to avoid in most piston-cylinder experiments where, unlike with internally-heated gas-pressure vessels, $f\text{H}_2$ cannot be easily maintained without external (solid-state) buffers. The methodology developed here reproduces very well the estimates from olivine-spinel barometry in those runs where spinel was large enough to analyse. The Fe-in-AuPd approach also yields results that lie close to our new method, albeit with much greater scatter, primarily due to the difficulty of analysing Fe at very low concentrations in Au–Pd close to the melt–capsule interface where secondary fluorescence can be a problem. We conclude that our olivine-melt oxybarometer has the potential to recover $f\text{O}_2$ from olivine-bearing experiments that are either lacking spinel or where the run-product spinel is too small to analyse. However, care must be taken to screen for Fe-loss to the capsule material during the experiment. This problem is especially acute under reducing conditions and in Au alloy or Pt capsules (Barr and Grove

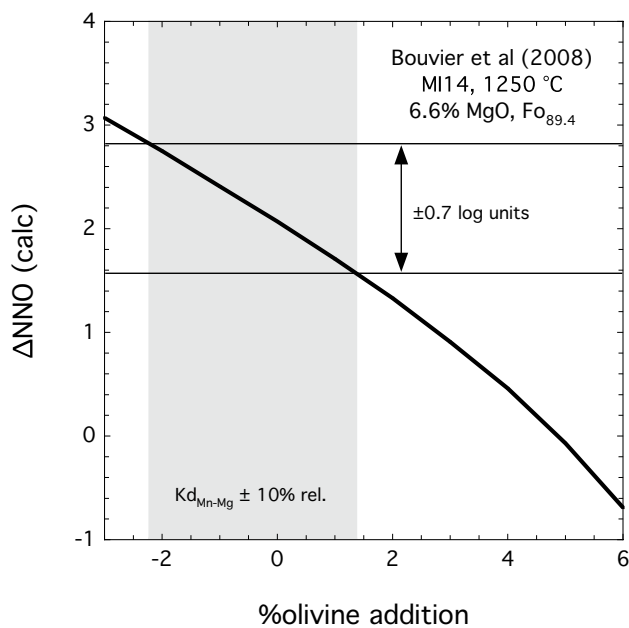


Fig. 13 Illustration of the effect of olivine addition on calculated fO_2 (expressed as ΔNNO) for a melt inclusion from St. Vincent (MI14 of Bouvier et al. 2008). The optimal correction to match the calculated Kd_{Mn-Mg} is -0.5 wt% olivine (i.e., olivine dissolution). An analytical uncertainty of $\pm 10\%$ relative on this value is shown as the grey bar, which translates to an uncertainty in fO_2 of ± 0.7 log units. With increasing olivine addition the calculated fO_2 drops significantly, emphasising the need for precise Mn measurements of olivine and glass for this method

2010). Uptake of metallic iron (Fe^0) by the capsule occurs via disproportionation of melt Fe^{2+} to $Fe^0 + Fe^{3+}$ leading to an apparent increase in glass $Fe^{3+}/\Sigma Fe$ and hence calculated fO_2 . To ensure reliable application of our oxybarometer the effects of Fe-loss must be fully accounted for.

$Fe^{3+}/\Sigma Fe$ estimates from olivine-hosted melt inclusions

Olivine-hosted melt inclusions are widely used to determine volatile contents of pre-eruptive magmas, with implications for volatile recycling at subduction zones or magma storage conditions, for example. Most olivine-hosted melt inclusions have experienced some degree of post-entrapment modification, for example by crystallisation of olivine on the inclusion wall, dissolution of the olivine host, or diffusive exchange between melt and host (Danyushevsky et al. 2002). Standard practice in these situations is to correct the melt inclusion composition for these effects by adding (or subtracting) some amount of host olivine (or FeO and MgO) to the melt inclusion to bring the pair back into equilibrium. This inevitably leads to some modification to $Kd_{Fe^{2+}-Mg}$, the parameter required for oxybarometry. To obviate this circularity, we

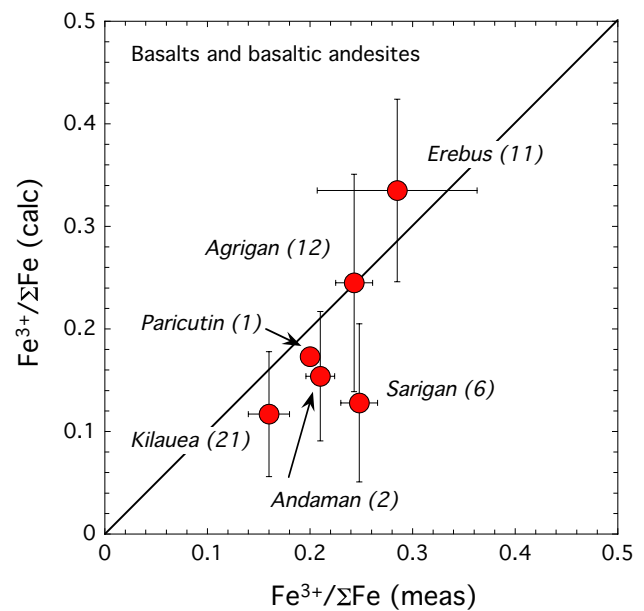


Fig. 14 Calculated $Fe^{3+}/\Sigma Fe$ for basaltic melt inclusions using the technique described in the text for six volcanoes for which $Fe^{3+}/\Sigma Fe$ was determined by $\mu XANES$. The average and sd for each volcano are plotted; the number of individual analyses is given in parentheses. Data sources are: Erebus (Moussallam et al. 2014); Agrigan, Mariana (Kelley and Cottrell 2012; Brounce et al. 2014); Sarigan, Mariana (Brounce et al. 2014); Kilauea (Moussallam et al. 2016); Andaman Islands, and Paricutin, Mexico (Kelley and Cottrell 2009)

propose to use the systematics of redox-insensitive Mn–Mg exchange to perform the post-entrapment corrections, and then use the $Kd_{Fe^{2+}-Mg}$ of the corrected melt and its host olivine to recover $Fe^{3+}/\Sigma Fe$. To make the post-entrapment correction requires some knowledge of the equilibrium temperature, which can be obtained, for example, through olivine-melt thermometry (e.g., Beattie 1993; Putirka et al. 2007).

Before testing our approach on natural melt inclusions, it is instructive once again to get a sense of the expected uncertainty of the method. In addition to the other factors considered above, the correction for post-entrapment modification adds further uncertainty; the more olivine that is added back into the inclusion, the higher the resulting $Kd_{Fe^{2+}-Mg}$ and the lower the calculated $Fe^{3+}/\Sigma Fe$ (and hence fO_2). To illustrate this we have calculated the effect on calculated fO_2 due to varying amounts of olivine addition (and subtraction) from an Mg-rich basaltic melt inclusion (#14) from St. Vincent (Bouvier et al. 2008). We use a temperature of $1200^\circ C$ and an initial (measured) $Kd_{Fe^{2+}-Mg} = 0.205$ for the calculations (Fig. 13). The calculated, equilibrium $Kd_{Fe^{2+}-Mg}$, after taking account of olivine (Fo_{89}) non-ideality is 0.31; deviation of $Kd_{Fe^{2+}-Mg}$ from this value enables us to calculate $Fe^{3+}/\Sigma Fe$ and thence fO_2 . It is clear that addition (or subtraction) of just a few percent olivine can lead to dramatic reduction (or

increase) in $Kd_{\text{Fe}^{2+}\text{-Mg}}$ and hence in calculated $f\text{O}_2$. Using Eq. (10), alongside the reported MnO contents of olivine and melt inclusion, the required correction is a subtraction of just 0.5 wt% olivine, i.e., due to dissolution of the host olivine. The calculated $f\text{O}_2$ ($\Delta\text{NNO}=2.2$) accords well with that estimated for St. Vincent high-Mg basalt ($\Delta\text{NNO}+1.5$ to $+1.8$) using spinel oxybarometry (Heath et al. 1998). Within the uncertainty of the measurement of MnO in olivine and glass, a range of olivine corrections is permissible. In Fig. 13, we show that a relative uncertainty of $\pm 10\%$ in $Kd_{\text{Mn-Mg}}$ translates to uncertainty of $\pm 1.3\%$ in the olivine correction, or ± 0.7 log units in $f\text{O}_2$. Evidently, having precise measurements of olivine and melt MnO contents is critical for this method, yet is often not a priority in melt inclusion studies. For comparison, using the method of Danyushevsky et al. (2000, 2002), Bouvier et al. (2008) estimate post-entrapment crystallisation of 6.5 wt% olivine, well outside the permissible bounds based on Mn–Mg exchange (Fig. 13).

Having established what is possible with our melt inclusion oxybarometer we have tested it against five olivine-hosted melt inclusions studies from the literature: Brounce et al (2014), Kelley and Cottrell (2009, 2012) and Moussallam et al (2014, 2016). In all of these cases melt $\text{Fe}^{3+}/\Sigma\text{Fe}$ was determined by μXANES , but using a lower flux than that used in our analyses. For these reasons the measured $\text{Fe}^{3+}/\Sigma\text{Fe}$ is considered more reliable; however, the presence of various amounts sulphur in all of the analysed glasses raises the prospect of Fe redox during melt inclusion quenching through Fe–S redox couples. This is a perennial problem with microbeam analysis of $\text{Fe}^{3+}/\Sigma\text{Fe}$ in sulphur-bearing glasses, but not for our methodology, as olivine-melt Fe–Mg exchange by diffusion is unlikely to have taken place on quenching timescales; if it did, there would be evidence in the form of thin overgrowth rims on the walls of the melt inclusion.

To calculate $\text{Fe}^{3+}/\Sigma\text{Fe}$ in each of the melt inclusion sets we first correct for post-entrapment modification using Eq. (10) with the measured $Kd_{\text{Mn-Mg}}$ and an equilibrium temperature from olivine-melt thermometry (or other petrological method) provided in the original sources. An iterative procedure was used. The corrected melt composition for each inclusion, following olivine addition or subtraction, was then used to calculate $\text{Fe}^{3+}/\Sigma\text{Fe}$, using Eq. (8). For each volcano studied we present the average value of $\text{Fe}^{3+}/\Sigma\text{Fe}$ and its standard deviation in Fig. 14. For five of the studied volcanoes our method reproduces the mean μXANES $\text{Fe}^{3+}/\Sigma\text{Fe}$ values within 1 s.d. The only exception is Sarigan, where our method consistently underestimates $\text{Fe}^{3+}/\Sigma\text{Fe}$. Notably these were the melt inclusions that required the greatest post-entrapment calculation (2–7 wt% olivine addition). Nonetheless, our method appears to have an accuracy of about ± 0.04 in $\text{Fe}^{3+}/\Sigma\text{Fe}$ and captures the broad variation from one sample suite

to the next. It is a much simpler analytical method than μXANES (or SMS), requiring much less sample preparation, and can be performed easily on large numbers of melt inclusions, as a means to explore broad-scale variations in $\text{Fe}^{3+}/\Sigma\text{Fe}$ (and $f\text{O}_2$) in space and in time. Moreover, as noted above, it is not susceptible to Fe–S redox exchange during quenching. However, our method does not take account of any diffusive Fe–Mg exchange between melt inclusion and host olivine during cooling (e.g., Danyushevsky et al. 2002), a problem that also afflicts in situ measurements of $\text{Fe}^{3+}/\Sigma\text{Fe}$. As diffusive re-equilibration with the host olivine lowers the Fe^{2+} content of the melt inclusion, but not its Fe^{3+} content, such a process will lead to erroneously high estimated $\text{Fe}^{3+}/\Sigma\text{Fe}$ (and hence $f\text{O}_2$) unless it is explicitly accounted for.

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